

CBMS Structural Biology Workbenches
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Molecular Replacement

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Lawrence Berkeley Laboratory

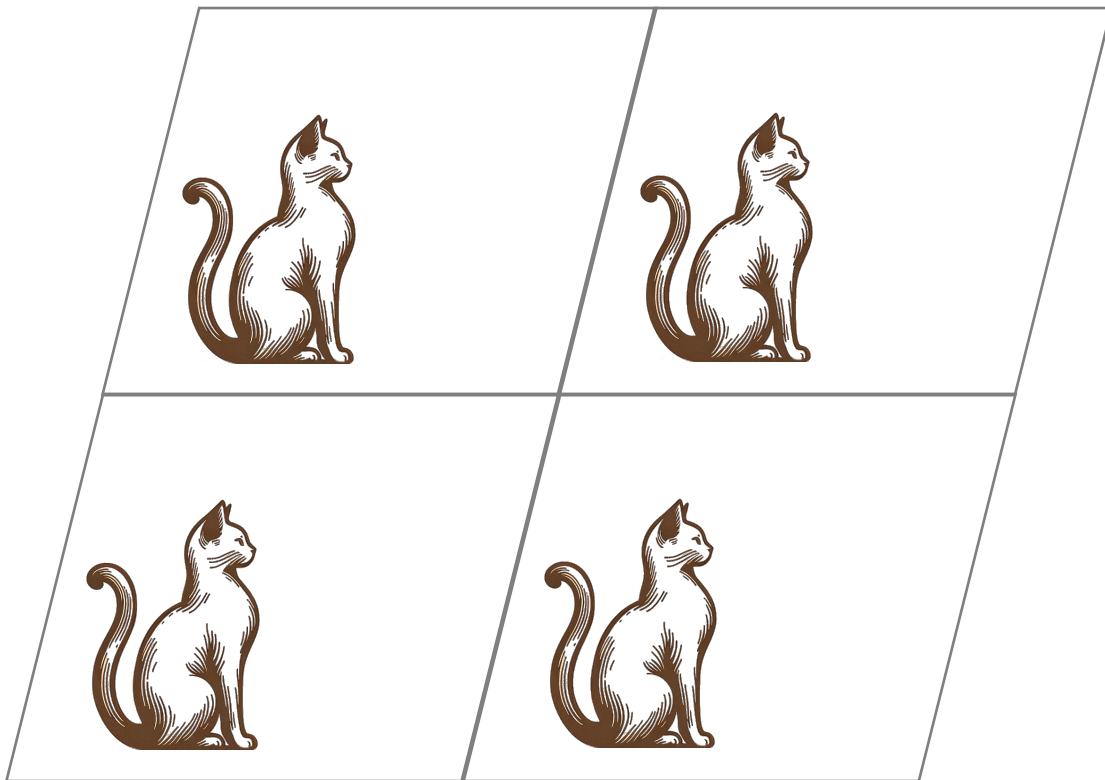
Molecular Replacement (MR)

MR = solve the **unknown** crystal structure of a molecule using a related **known molecular model**.

Known model



Crystal of unknown structure



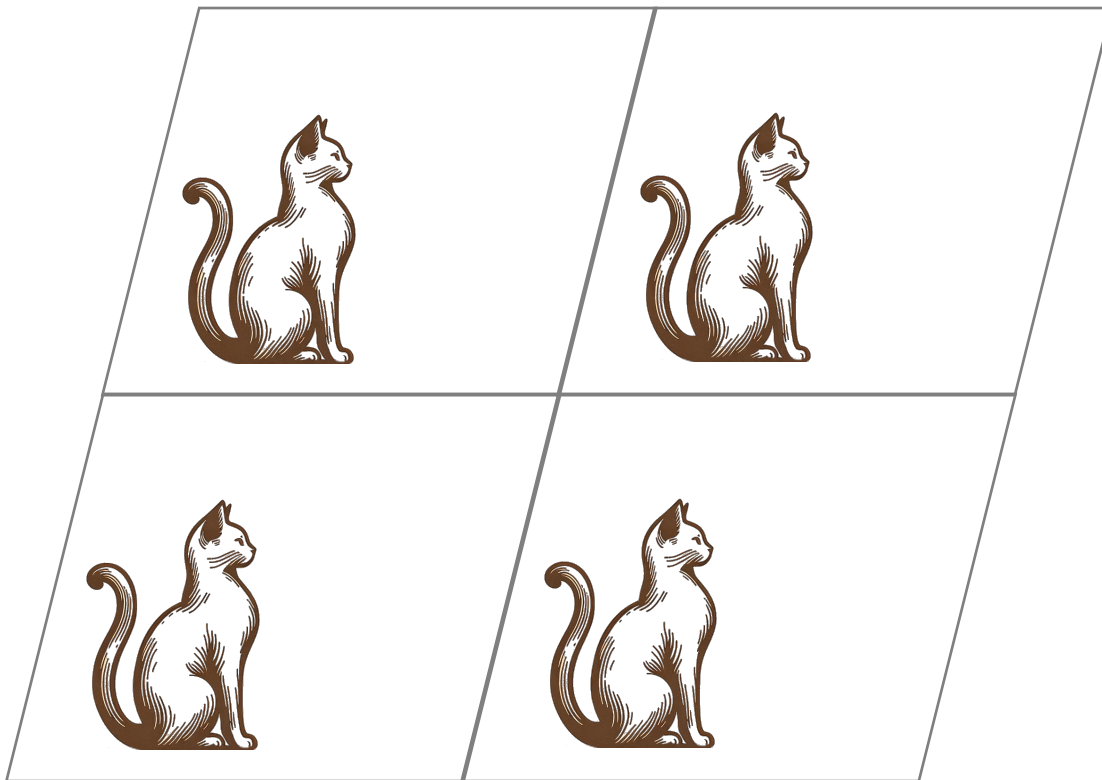
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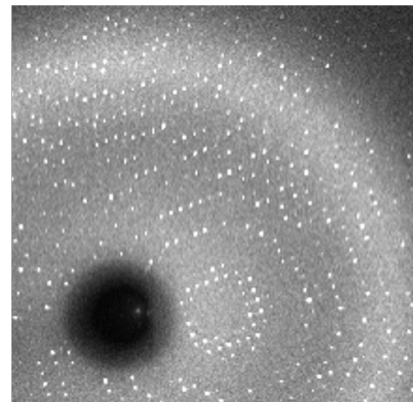
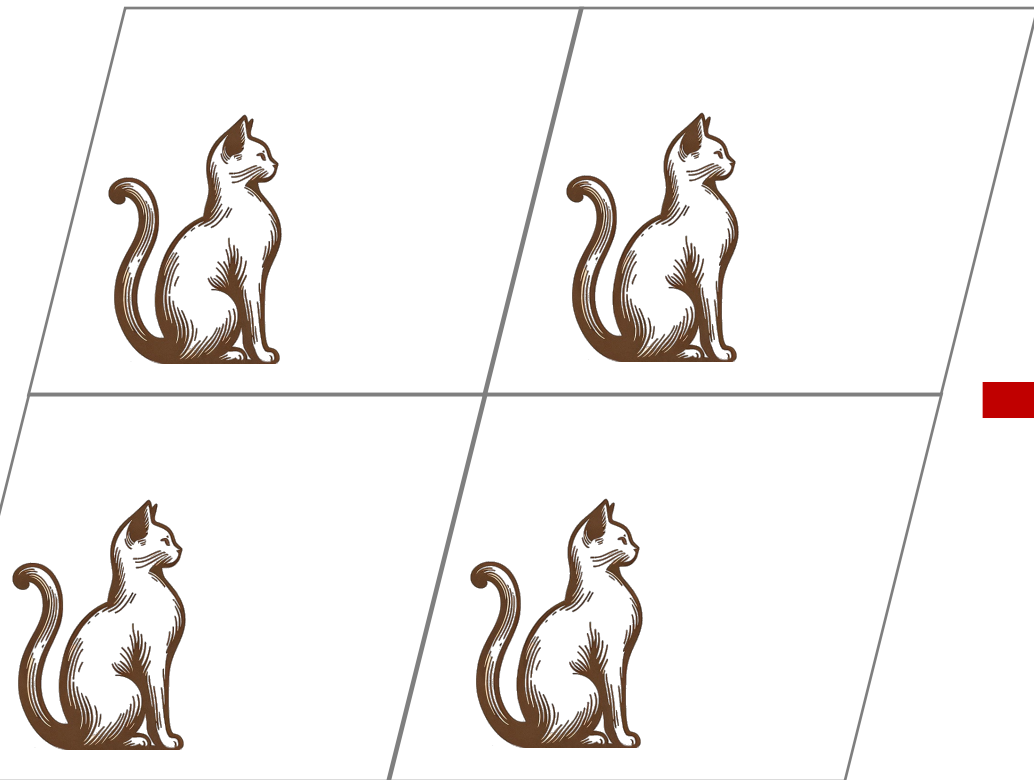
Crystal of unknown structure



Known model provides initial estimates of the phases of the unknown structure.

Molecular Replacement (MR)

Crystal of unknown structure

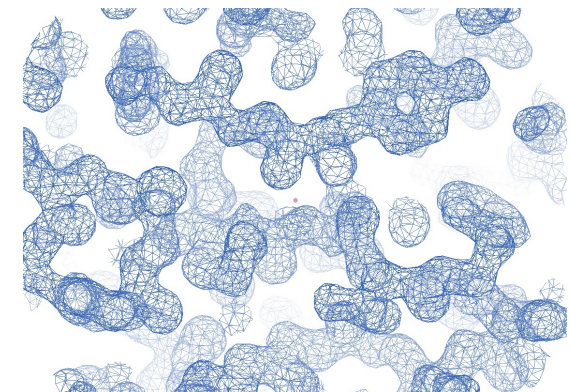


Intensities (hkl)



$$|F| e^{i\phi}$$

Known model



Density map

Molecular replacement: Approach

Try to match the known model with the unknown structure.



Search model

Crystal of unknown structure



Find the **rotation** and **translation** of the search model so that it matches the unknown structure.

The search model

- Finding a suitable search model is critical step in MR.
- Should provide a high proportion of the scattering from the target structure with high accuracy (low r.m.s.d.).



Not similar to the target

Crystal of unknown structure



Molecular replacement: Scoring

Compare observed and calculated diffraction.



Poor score



Good score

Different approaches:

- Patterson function
- Maximum-likelihood Methods (Phaser)

MR Scoring: Maximum Likelihood Method

“For any postulated orientation and position of the model, what is the probability of obtaining the structure amplitudes that we observe?”



Explicitly models errors

- Experimental uncertainties
- r.m.s. coordinate error of the search model

→ Likelihood methods are more robust and generally give clearer solutions in difficult cases

Maximum Likelihood Scoring in Phaser

LLG = Log Likelihood gain

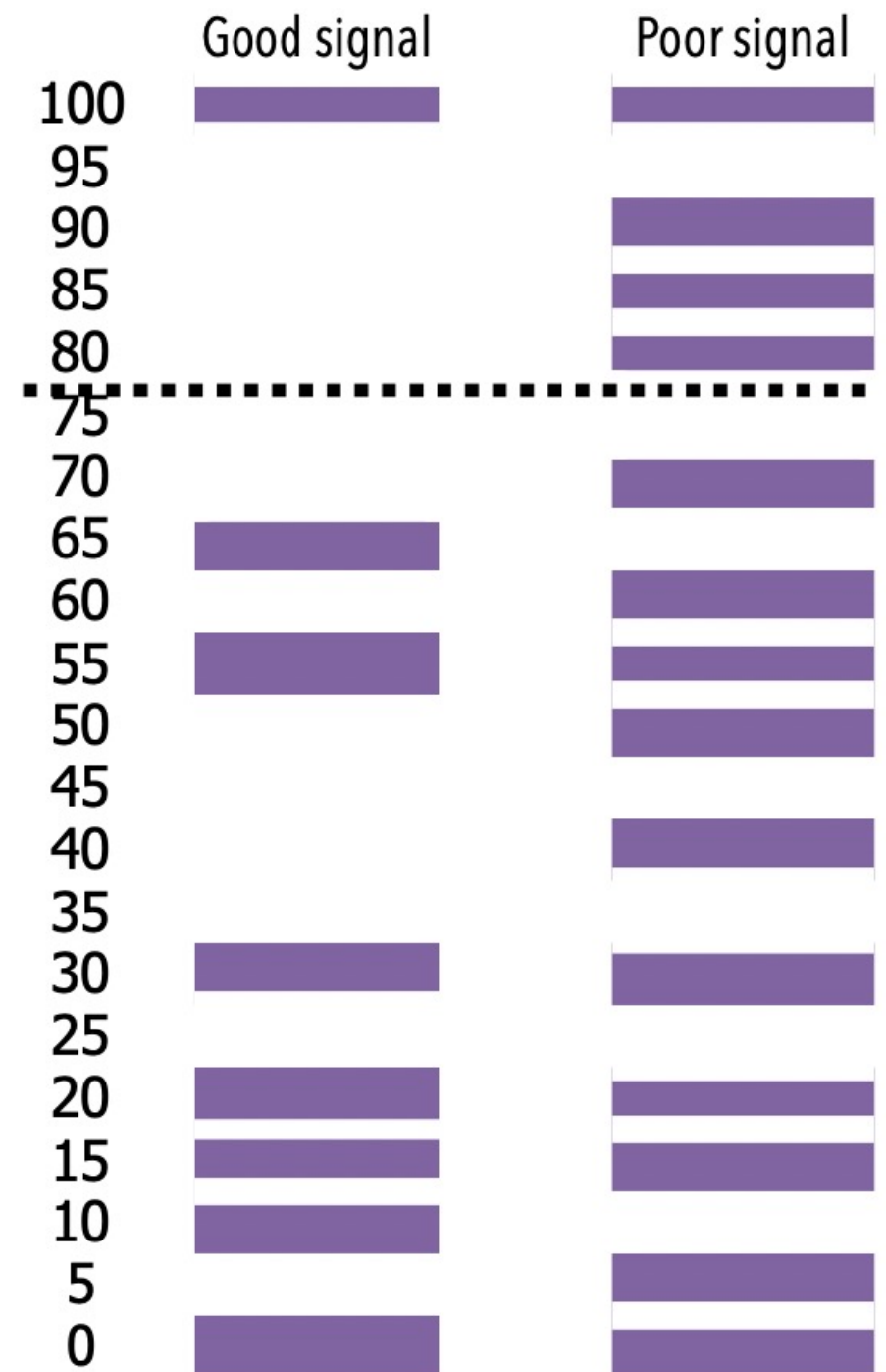
→ It measures how much better the data can be predicted with the search model than with a random distribution of the same atoms.

TF-Z = how many standard deviations your solution is above the mean (the higher the better).

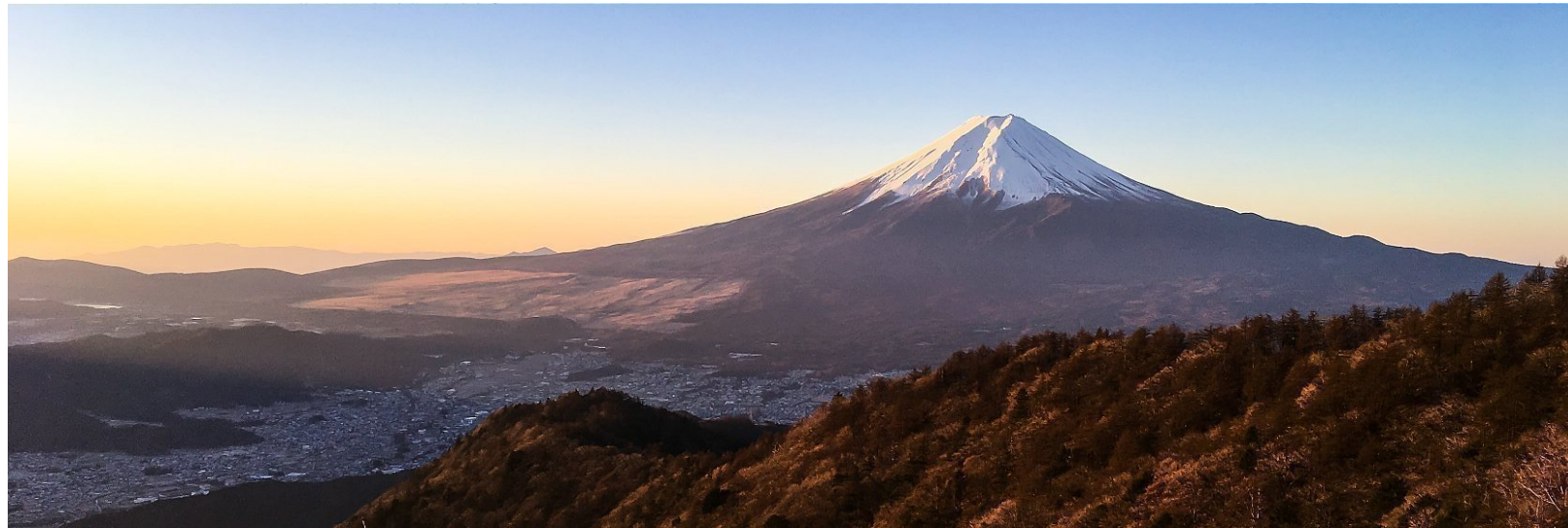
Maximum Likelihood Scoring in Phaser

Select solutions that are over 75% of the difference between the top peak and the mean.

- Good signal, few potential solutions
- Poor signal, many potential solutions



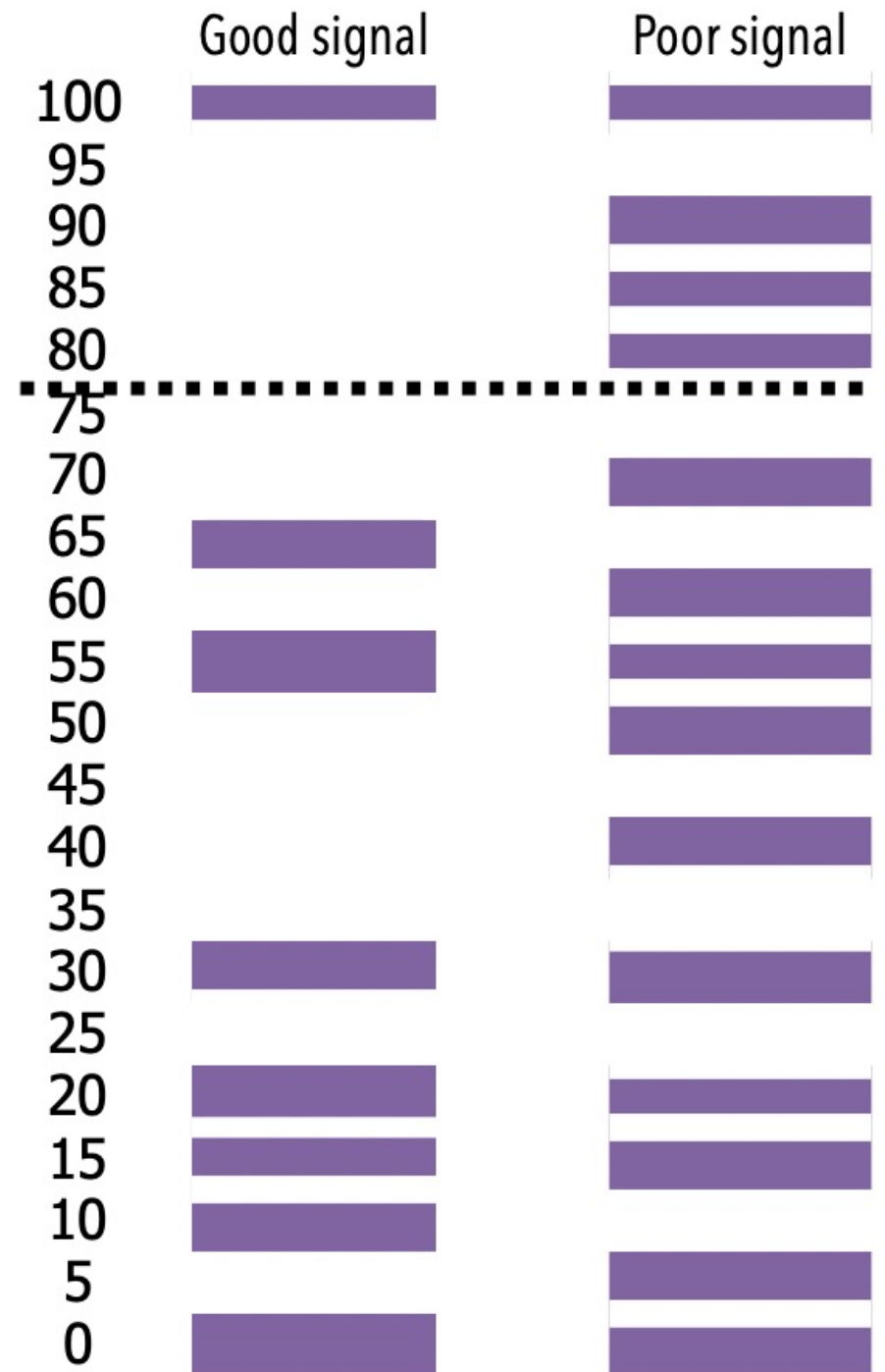
Maximum Likelihood Scoring in Phaser



Good signal



Poor signal



3) The scoring function: ML Method

TF Z-score	LLG score	Solved?
< 5	< 25	no
5 - 6	25 - 36	unlikely
6 - 7	36 - 49	possibly
7 - 8	49 - 64	probably
> 8	> 64	definitely

What is needed to run Phaser MR

- Reflection data
- Search model
- Error estimation of the search model
 - Homologue: sequence identity
 - Predicted model: r.m.s.d. (1.0 Å)
- ASU content
- Twinning
- (tNCS)

ASU content

- Sequence of your construct
- How many copies of the the molecule(s)?

$$N = 1$$

Asymmetric unit

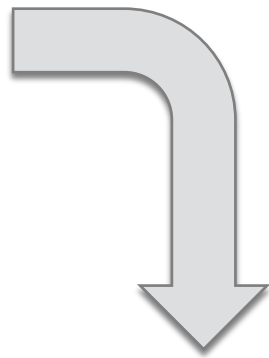
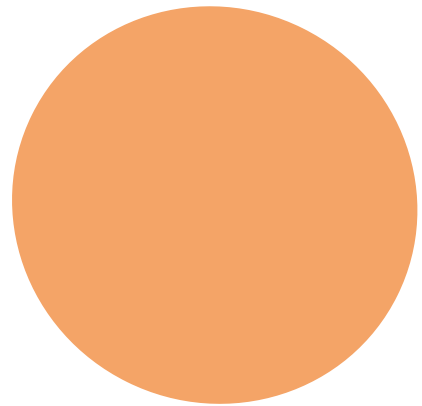


One copy in the asymmetric unit.

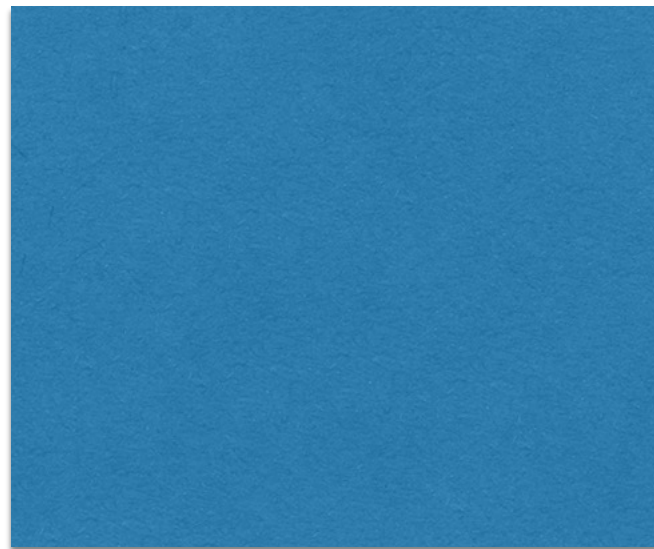
Estimating the number of molecules in the ASU

Matthews coefficient:

$$V_M = \frac{\text{volume of asymmetric unit}}{\text{molecular weight}}$$



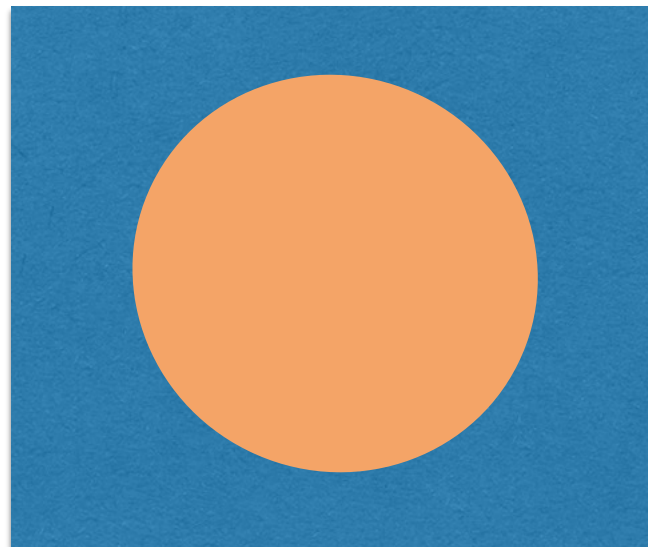
How many
spheres fit into
the square?



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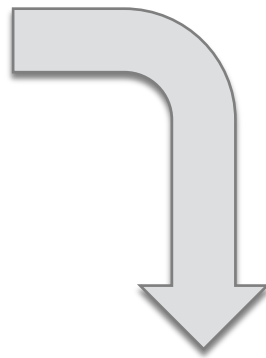
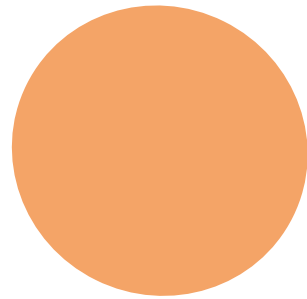


Clearly only one
sphere

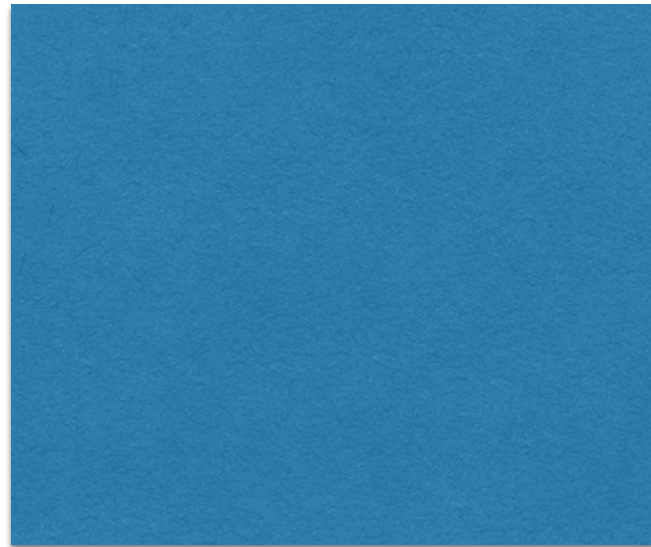
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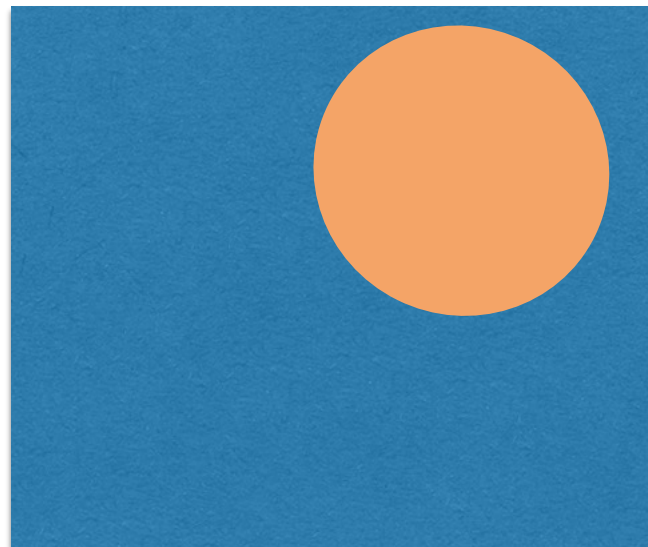
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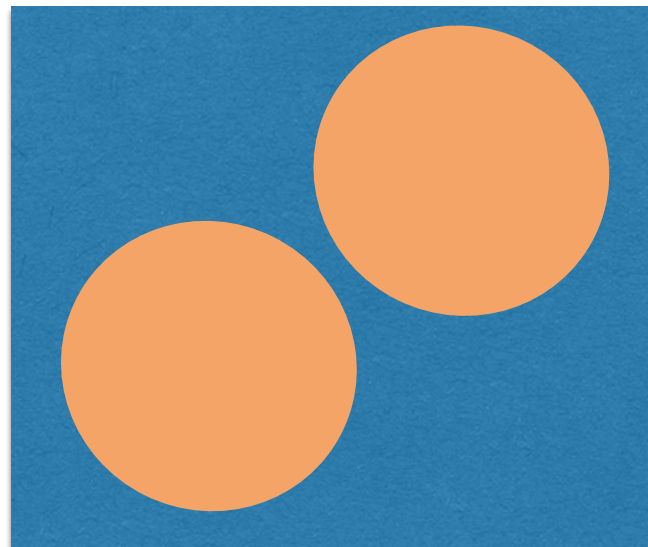


There could be
only one...

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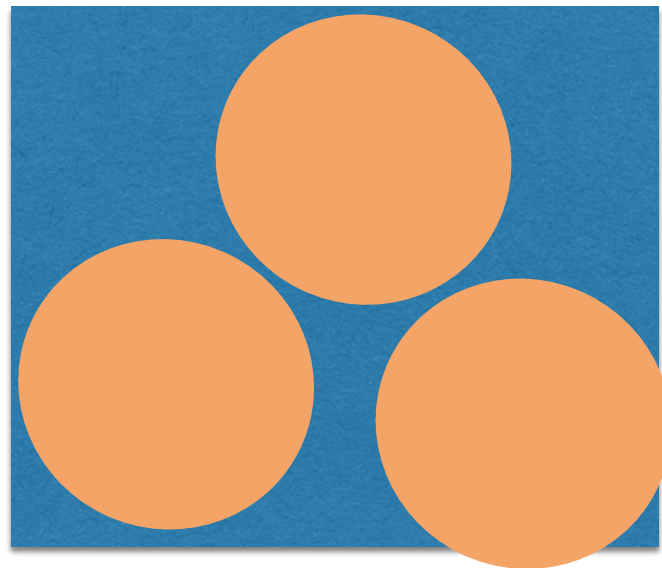


... or maybe two

Estimating the number of molecules in the ASU

Matthews coefficient: $V_M = \frac{\text{volume of asymmetric unit}}{\text{molecular weight}}$

How many
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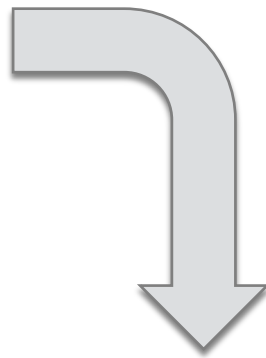
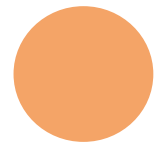


...but not three

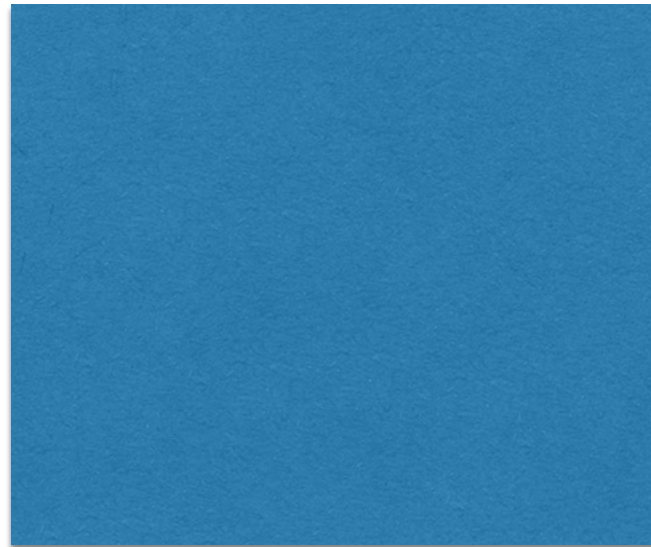
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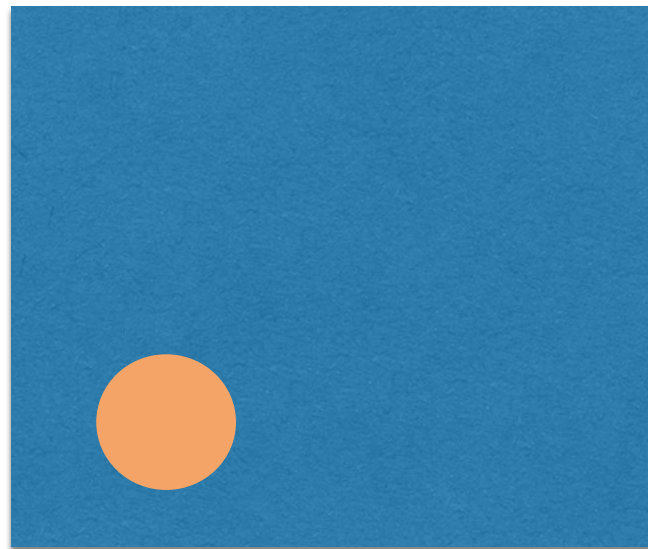
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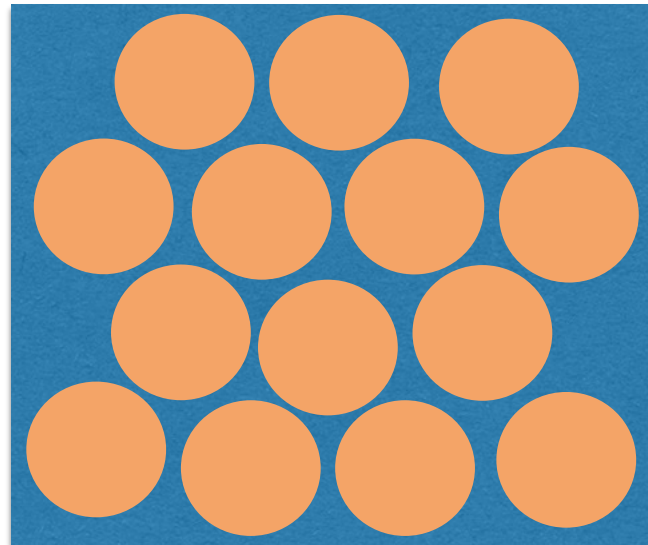


Only one

Estimating the number of molecules in the ASU

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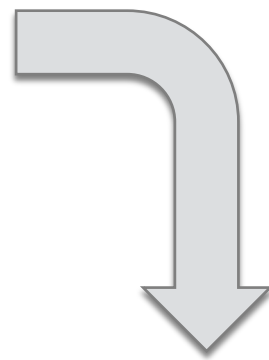


Many (14)

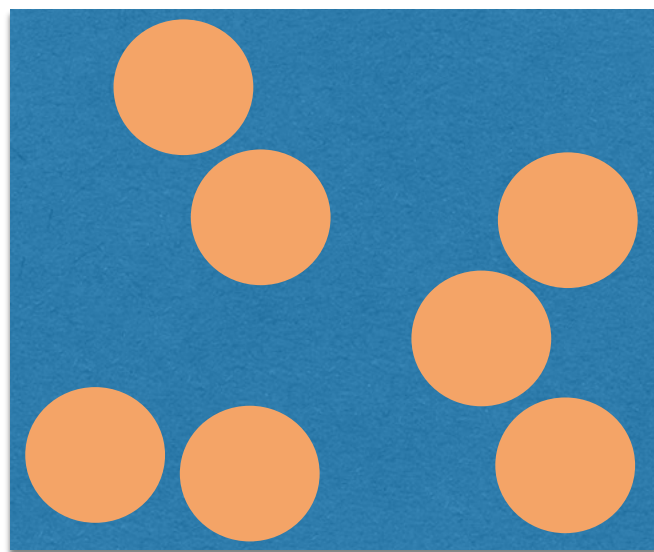
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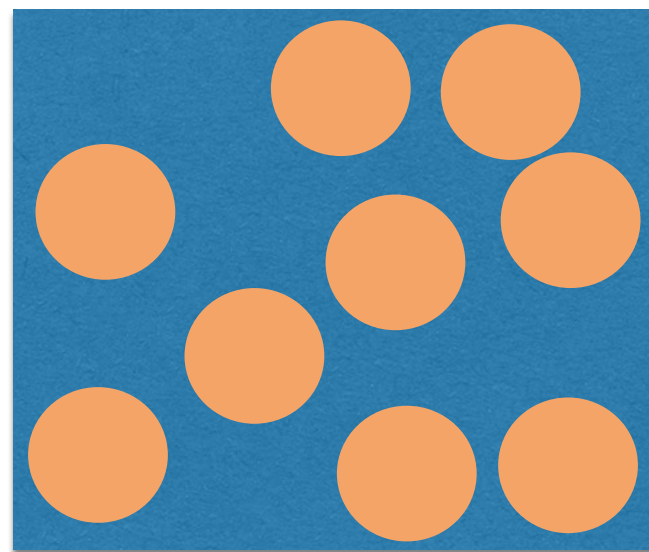
$$V_M = \frac{\text{volume of asymmetric unit}}{\text{molecular weight}}$$



How many
spheres fit into
the square?



7



9

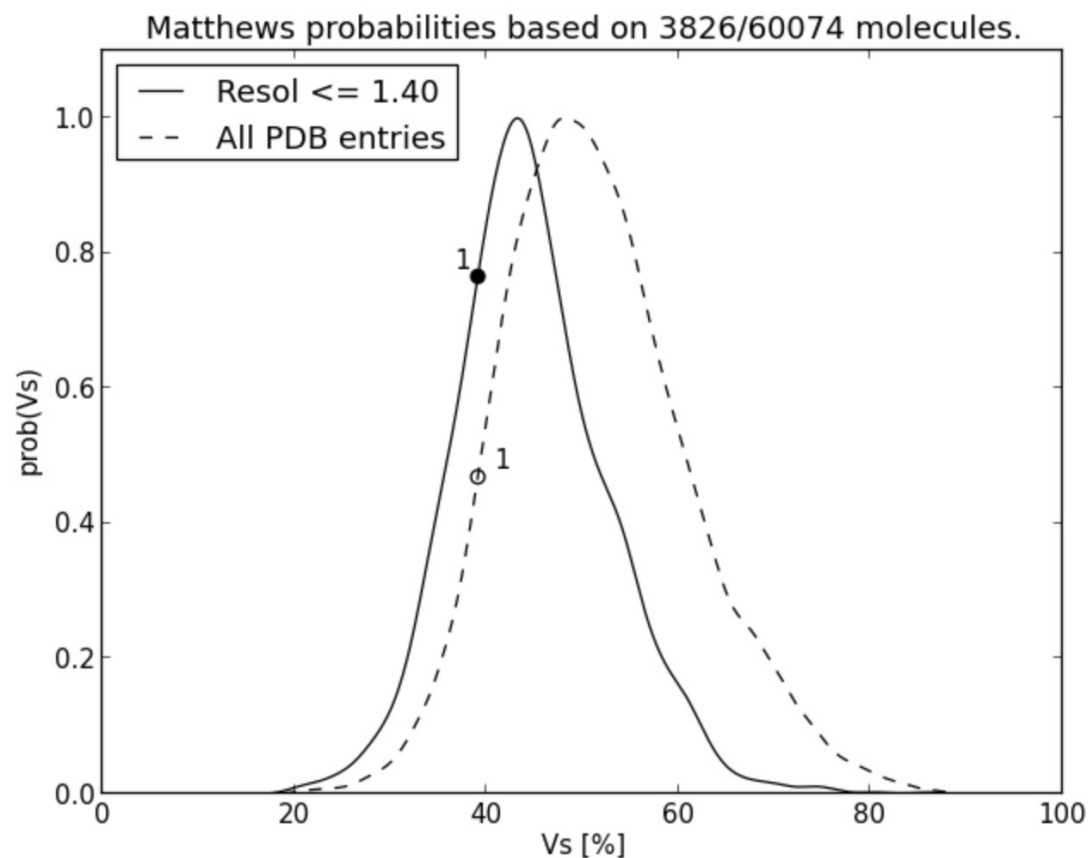
Most likely:
something in
between

Estimating the number of molecules in the ASU

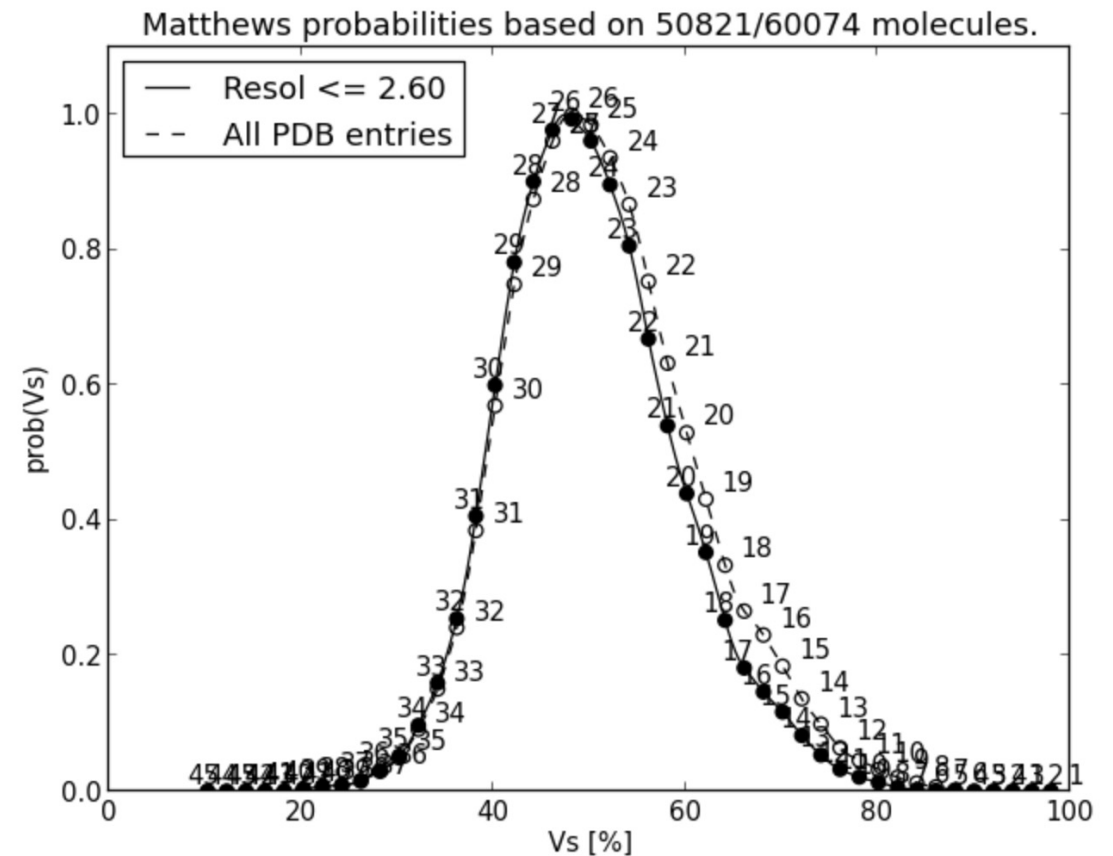
Matthews coefficient:
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Compare your value of V_M with histograms for known structures (from PDB) \rightarrow choose most probable.

Few possibilities



Many possibilities



Key points

- 1) MR: Use a previously known structure to solve a new structure
- 2) Known structure can be a homologue or a predicted model
- 3) Known structures may need to be modified
- 4) Estimate the ASU content
- 5) Be aware of data pathologies (twinning, tNCS)

The Project



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Los Alamos National Laboratory New Mexico Consortium

Tom Terwilliger, Li-Wei Hung



UTHealth

Matt Baker



Duke University

Jane & David Richardson,
Christopher Williams,
Vincent Chen



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Liebschner D, *et al.*, Macromolecular structure determination using X-rays, neutrons and electrons: recent developments in *Phenix*. *Acta Cryst.* 2019 **D75**:861–877