

*AsCA meeting,  
6 December 2025*

# Refinement

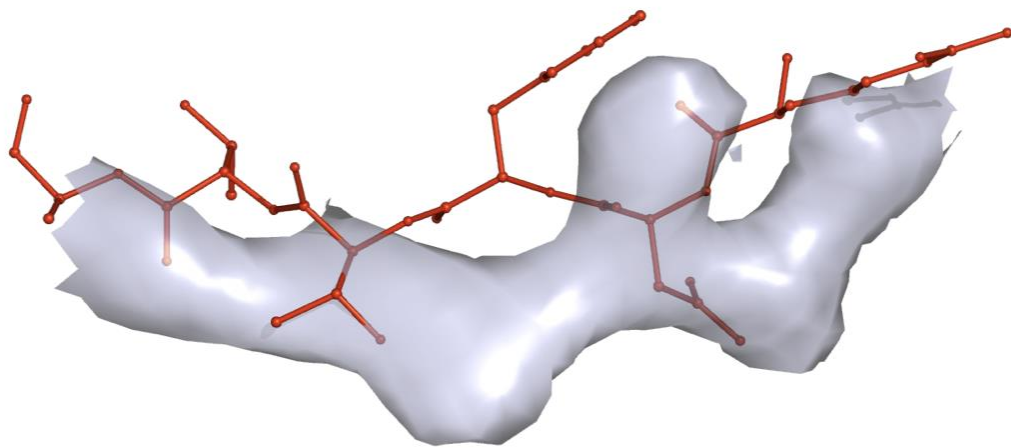


Dorothee Liebschner  
Lawrence Berkeley Laboratory

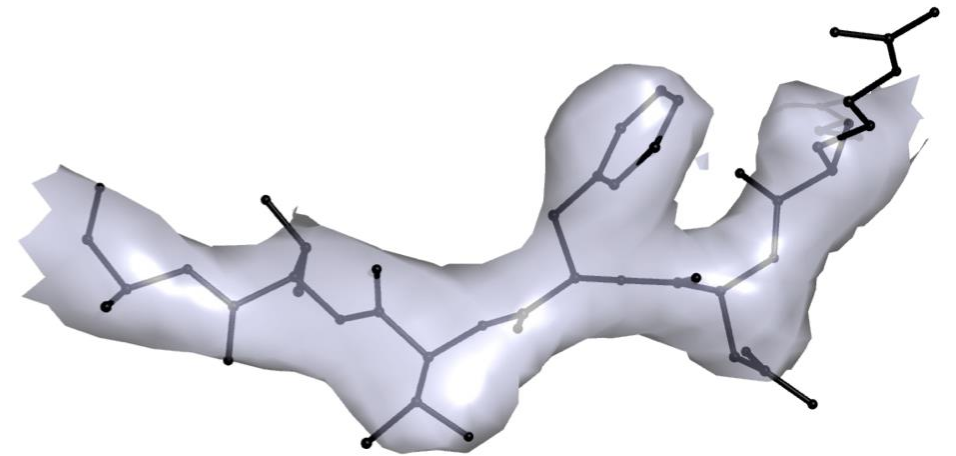
# Refinement

---

Initial model



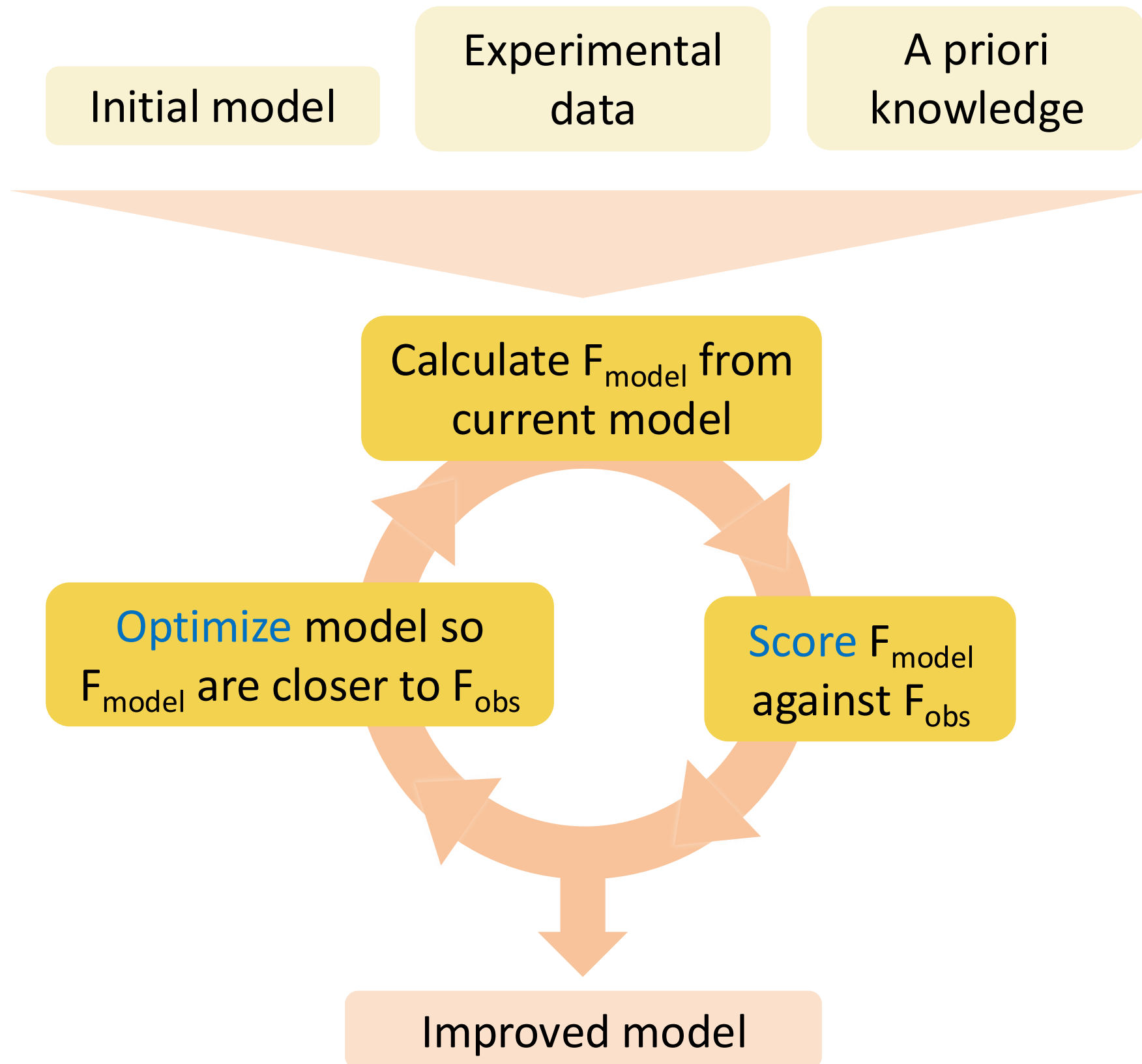
Improved model



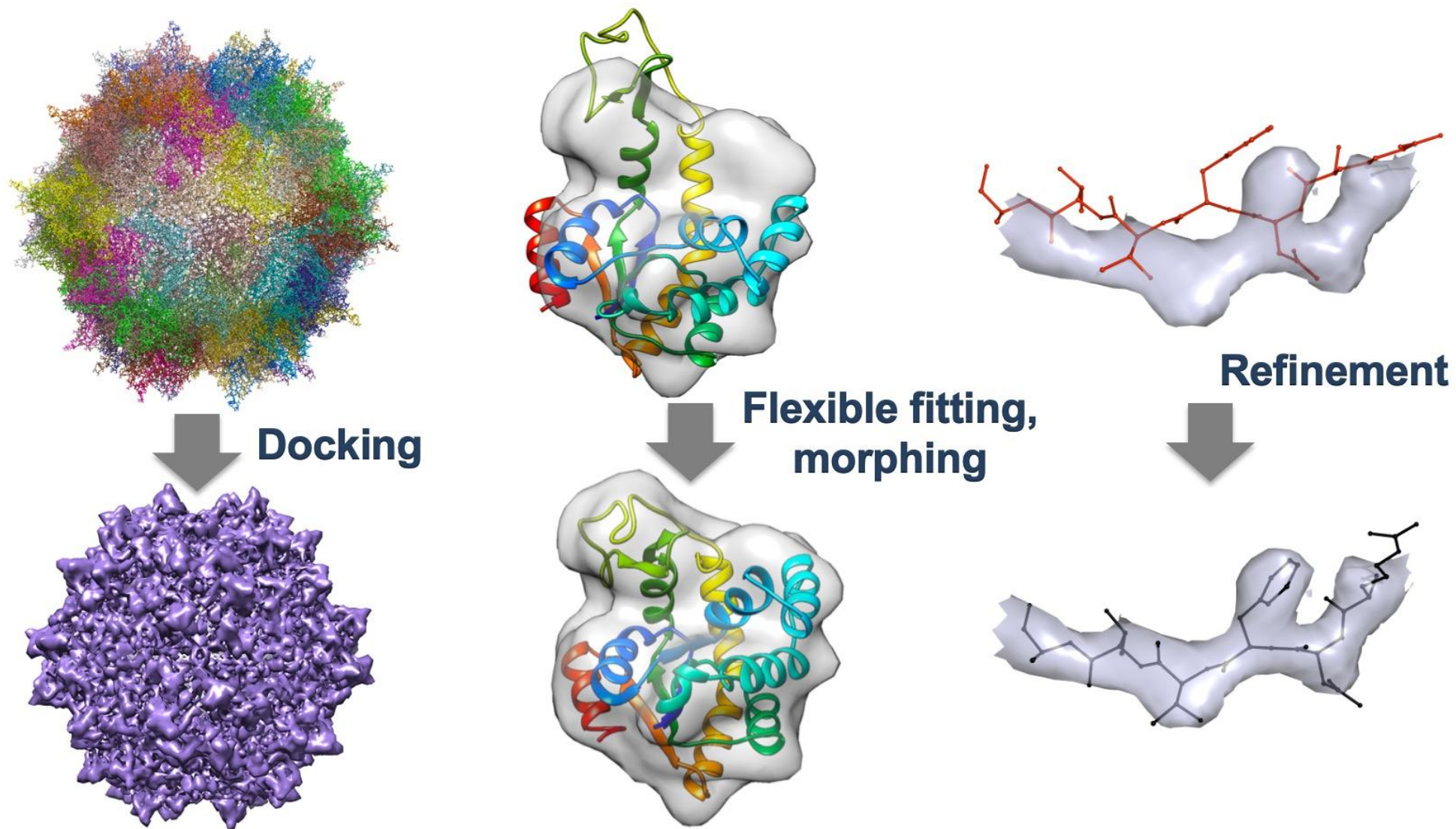
Fit atomic model to experimental data with the help of some known *a priori* information.

# Refinement

---



# Refinement



- Docking, morphing are **not** refinement
- Refinement is to fine-tune an already fine atomic model
- Refinement only applies small changes to the model (within the convergence radius of refinement,  $\sim 1\text{\AA}$ )



# Refinement: black box

---



- Does it always work?
- Is it always as easy as poor model in, better model out?

# Refinement: black box

---

- Does it always work?
- Is it always as easy as poor model in, better model out?

## **No. Because:**

- Model parameterization is not easy.
- Default settings suit most common scenario (typical data resolution, model reasonably fits data)
- Less typical situations need customizations
  - Low/high resolution data
  - Incomplete models
  - Novel ligands

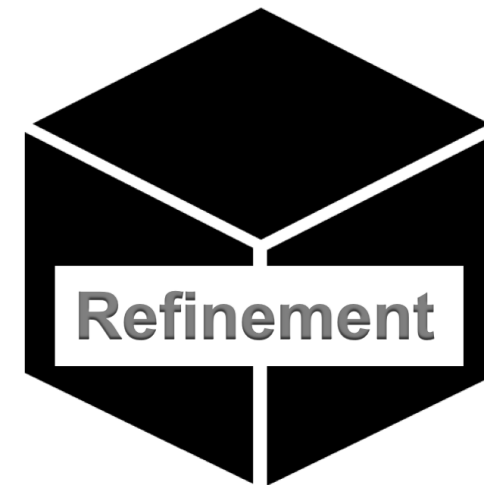


# Refinement: black box

---

How do you know if...

- ... refinement worked
- ... you did it correctly?
- ... the model is good enough to publish?



**Do validation!**

Standard validation protocols are designed to answer these questions.

# Refinement

---

Use an *optimization* algorithm to minimize a *target function* of a set of *observations* by changing the *parameters* of a model.

## research papers

---

Acta Crystallographica Section D  
**Biological  
Crystallography**  
ISSN 0907-4449

### Introduction to macromolecular refinement

**Dale. E. Tronrud**

Howard Hughes Medical Institute and Institute  
of Molecular Biology, University of Oregon,  
Eugene, OR 97403, USA

The process of refinement is such a large problem in function minimization that even the computers of today cannot perform the calculations to properly fit X-ray diffraction data. Each of the refinement packages currently under development reduces the difficulty of this problem by utilizing a unique combination of targets, assumptions, and optimization

Received 5 April 2004  
Accepted 21 September 2004

Tronrud, D. E. Introduction to macromolecular refinement. Acta Crystallogr. D Biol. Crystallogr. 60, 2156–2168 (2004).

# Refinement

---

Use an *optimization algorithm* to minimize a *target function* of a set of *observations* by changing the *parameters* of a model.

## research papers

---

Acta Crystallographica Section D  
**Biological  
Crystallography**  
ISSN 0907-4449

### Introduction to macromolecular refinement

**Dale. E. Tronrud**

Howard Hughes Medical Institute and Institute  
of Molecular Biology, University of Oregon,  
Eugene, OR 97403, USA

The process of refinement is such a large problem in function minimization that even the computers of today cannot perform the calculations to properly fit X-ray diffraction data. Each of the refinement packages currently under development reduces the difficulty of this problem by utilizing a unique combination of targets, assumptions, and optimization

Received 5 April 2004  
Accepted 21 September 2004

Tronrud, D. E. Introduction to macromolecular refinement. Acta Crystallogr. D Biol. Crystallogr. 60, 2156–2168 (2004).



# Refinement

---

- *parameters* of a model
- *target function*
- *optimization* algorithm
- *observations*

## research papers

---

Acta Crystallographica Section D  
**Biological  
Crystallography**  
ISSN 0907-4449

### Introduction to macromolecular refinement

**Dale. E. Tronrud**

Howard Hughes Medical Institute and Institute  
of Molecular Biology, University of Oregon,  
Eugene, OR 97403, USA

The process of refinement is such a large problem in function minimization that even the computers of today cannot perform the calculations to properly fit X-ray diffraction data. Each of the refinement packages currently under development reduces the difficulty of this problem by utilizing a unique combination of targets, assumptions, and optimization

Received 5 April 2004  
Accepted 21 September 2004

Tronrud, D. E. Introduction to macromolecular refinement. Acta Crystallogr. D Biol. Crystallogr. 60, 2156–2168 (2004).

# Refinement

---

- *parameters of a model*
- *target function*
- *optimization algorithm*
- *observations*

## research papers

---

Acta Crystallographica Section D  
**Biological  
Crystallography**  
ISSN 0907-4449

### Introduction to macromolecular refinement

**Dale. E. Tronrud**

Howard Hughes Medical Institute and Institute  
of Molecular Biology, University of Oregon,  
Eugene, OR 97403, USA

The process of refinement is such a large problem in function minimization that even the computers of today cannot perform the calculations to properly fit X-ray diffraction data. Each of the refinement packages currently under development reduces the difficulty of this problem by utilizing a unique combination of targets, assumptions, and optimization

Received 5 April 2004  
Accepted 21 September 2004

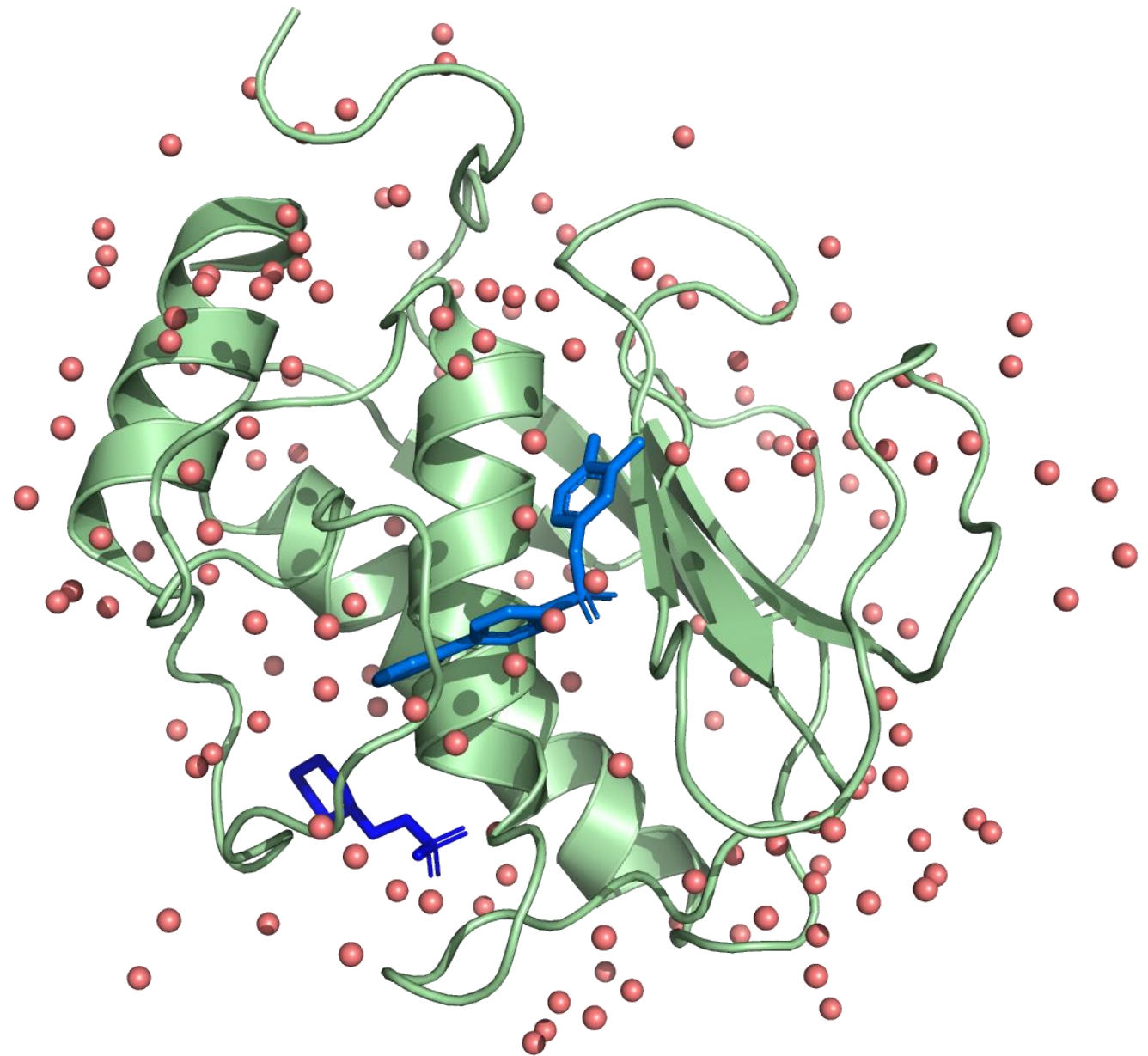
Tronrud, D. E. Introduction to macromolecular refinement. Acta Crystallogr. D Biol. Crystallogr. 60, 2156–2168 (2004).

# Parameters of a model

---

Our model has parameters that describe the crystal and its content.

- **Atomic:**
  - coordinates
  - B-factors
  - occupancies
- **Non-atomic:**
  - bulk-solvent
  - anisotropy
  - twinning



# Parameters of a model

---

Our model has parameters that describe the crystal and its content.

- **Atomic:**
    - coordinates
    - B-factors
    - occupancies
  - **Non-atomic:**
    - bulk-solvent
    - anisotropy
    - twinning
- } Saved in the model file (.pdb, .mmCIF)

# Parameters of a model

---

Our model has parameters that describe the crystal and its content.

- **Atomic:**
  - coordinates
  - B-factors
  - occupancies

- **Non-atomic:**
  - bulk-solvent
  - anisotropy
  - twinning



Taken into account automatically by  
refinement program (e.g., bulk solvent)  
Set by the user (e.g., twinning).



# Atomic model parameters

---

To calculate a score (compare measured and model-based structure factor amplitudes), we need to compute structure factors from model parameters.

Ca atom in a Pro residue:

ATOM	25	CA	PRO	A	4	31.309	29.489	26.044	1.00	57.79	C
------	----	----	-----	---	---	--------	--------	--------	------	-------	---

$$F_{calc(atoms)}(hkl) = \sum_n^{N_{atoms}} \left( q_n f_n(\mathbf{s}) e^{-B_n \frac{\sin^2 \theta}{\lambda^2}} e^{2\pi i \mathbf{s} \mathbf{r}_n} \right)$$


# Atomic model parameters

To calculate a score (compare measured and model-based structure factor amplitudes), we need to compute structure factors from model parameters.

Ca atom in a Pro residue:

ATOM	25	CA	PRO	A	4	31.309	29.489	26.044	1.00	57.79		C
------	----	----	-----	---	---	--------	--------	--------	------	-------	--	---

31.309 29.489 26.044  
Atomic coordinates  
(position)

$$F_{calc(atoms)}(hkl) = \sum_n^{N_{atoms}} \left( q_n f_n(\mathbf{s}) e^{-B_n \frac{\sin^2 \theta}{\lambda^2}} e^{2\pi i \mathbf{s} \cdot \mathbf{r}_n} \right)$$


# Atomic model parameters

To calculate a score (compare measured and model-based structure factor amplitudes), we need to compute structure factors from model parameters.

Ca atom in a Pro residue:

ATOM	25	CA	PRO	A	4	31.309	29.489	26.044	1.00	57.79		C
------	----	----	-----	---	---	--------	--------	--------	------	-------	--	---

$$F_{calc(atoms)}(hkl) = \sum_n^{N_{atoms}} \left( q_n f_n(\mathbf{s}) e^{-\overset{\text{ADP (B-factor)}}{\underset{\text{Local mobility (harmonic vibrations)}}{B_n}} \frac{\sin^2 \theta}{\lambda^2}} e^{2\pi i \mathbf{s} \cdot \overset{\text{Atomic coordinates (position)}}{\mathbf{r}_n}} \right)$$

31.309 29.489 26.044  
Atomic coordinates  
(position)

57.79  
ADP (B-factor)  
Local mobility (harmonic  
vibrations)

# Atomic model parameters

To calculate a score (compare measured and model-based structure factor amplitudes), we need to compute structure factors from model parameters.

Ca atom in a Pro residue:

ATOM	25	CA	PRO	A	4	31.309	29.489	26.044	1.00	57.79		C
------	----	----	-----	---	---	--------	--------	--------	------	-------	--	---

$$F_{calc(atoms)}(hkl) = \sum_n^{N_{atoms}} \left( \overset{\substack{\text{Occupancy} \\ \text{Large-scale disorder}}}{q_n} f_n(\mathbf{s}) e^{-\overset{\substack{\text{ADP (B-factor)} \\ \text{Local mobility (harmonic vibrations)}}}{B_n} \frac{\sin^2 \theta}{\lambda^2}} e^{2\pi i \mathbf{s} \cdot \overset{\substack{\text{Atomic coordinates} \\ \text{(position)}}}{\mathbf{r}_n}} \right)$$

1.00

31.309 29.489 26.044

57.79

# Atomic model parameters

To calculate a score (compare measured and model-based structure factor amplitudes), we need to compute structure factors from model parameters.

Ca atom in a Pro residue:

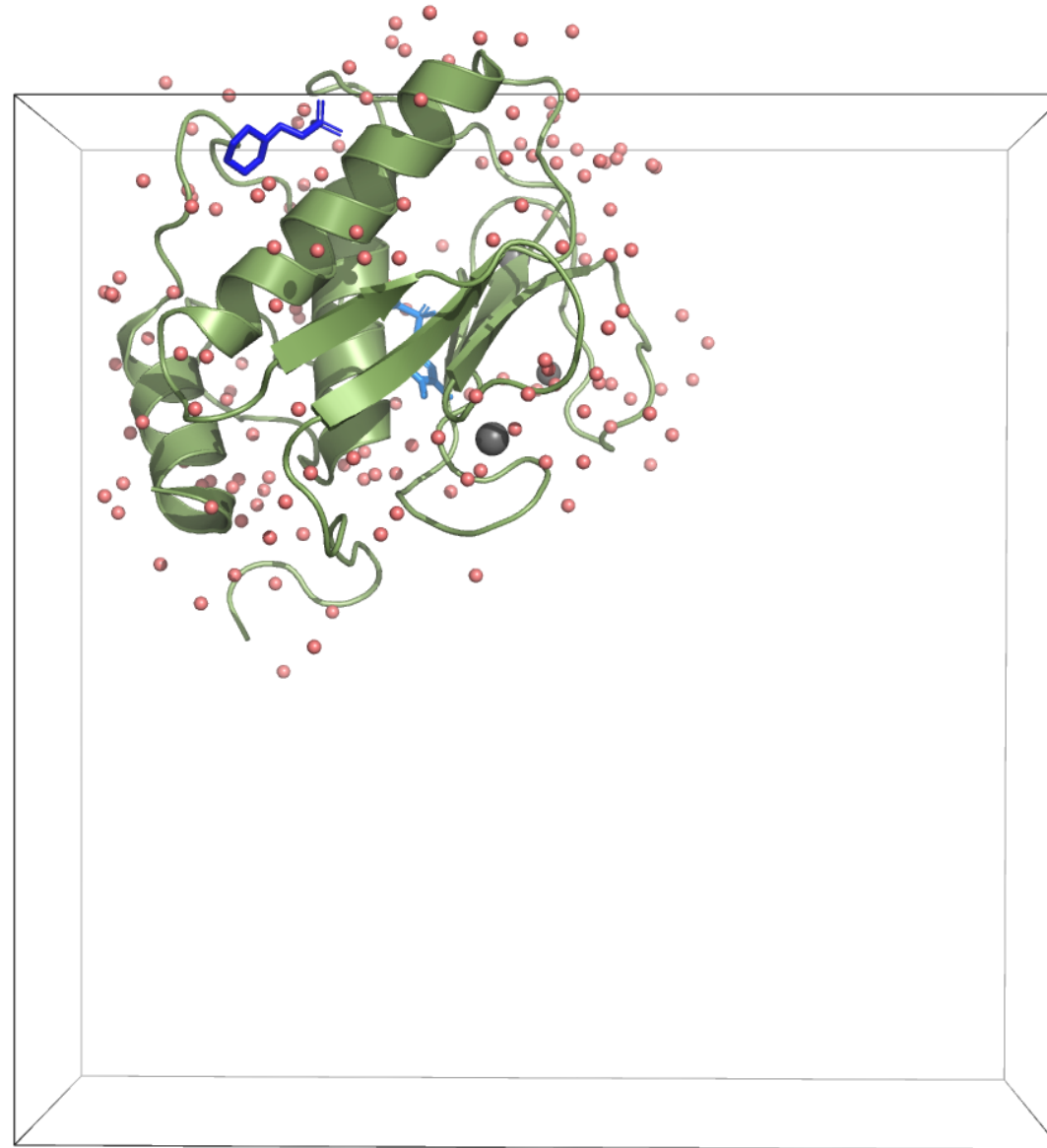
ATOM	25	CA	PRO	A	4	31.309	29.489	26.044	1.00	57.79		C
------	----	----	-----	---	---	--------	--------	--------	------	-------	--	---

$$F_{calc(atoms)}(hkl) = \sum_n^{N_{atoms}} \left( \overset{\substack{\text{Occupancy} \\ \text{Large-scale disorder} \\ 1.00}}{\downarrow} q_n \overset{\substack{\text{Atom type} \\ c}}{\uparrow} f_n(\mathbf{s}) e^{-\overset{\substack{\text{ADP (B-factor)} \\ \text{Local mobility (harmonic vibrations)} \\ 57.79}}{\uparrow} B_n \frac{\sin^2 \theta}{\lambda^2}} e^{2\pi i \mathbf{s} \overset{\substack{\text{Atomic coordinates} \\ \text{(position)}}{\downarrow} \mathbf{r}_n}} \right)$$



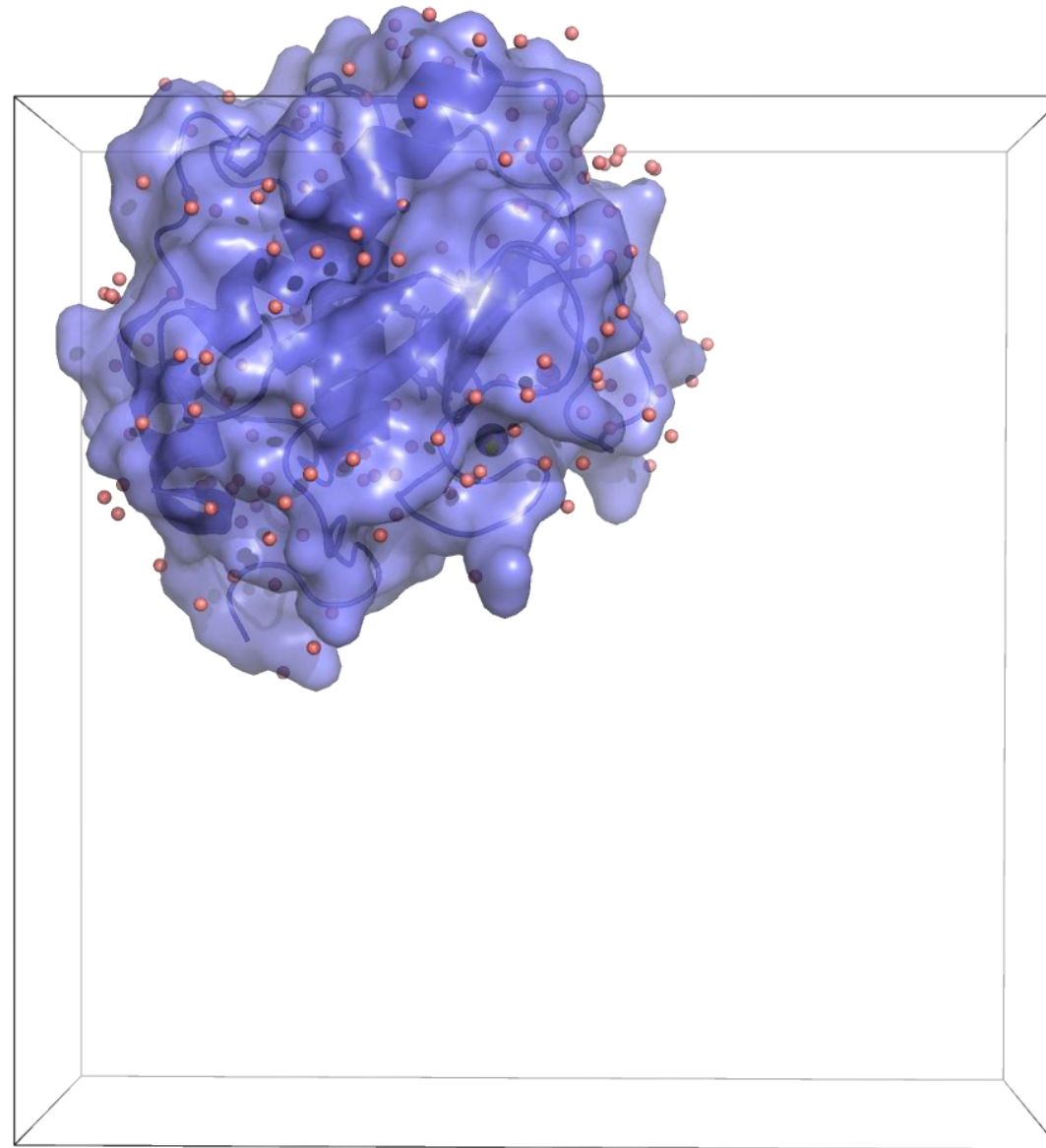
# bulk solvent : non-atomic model parameter

---



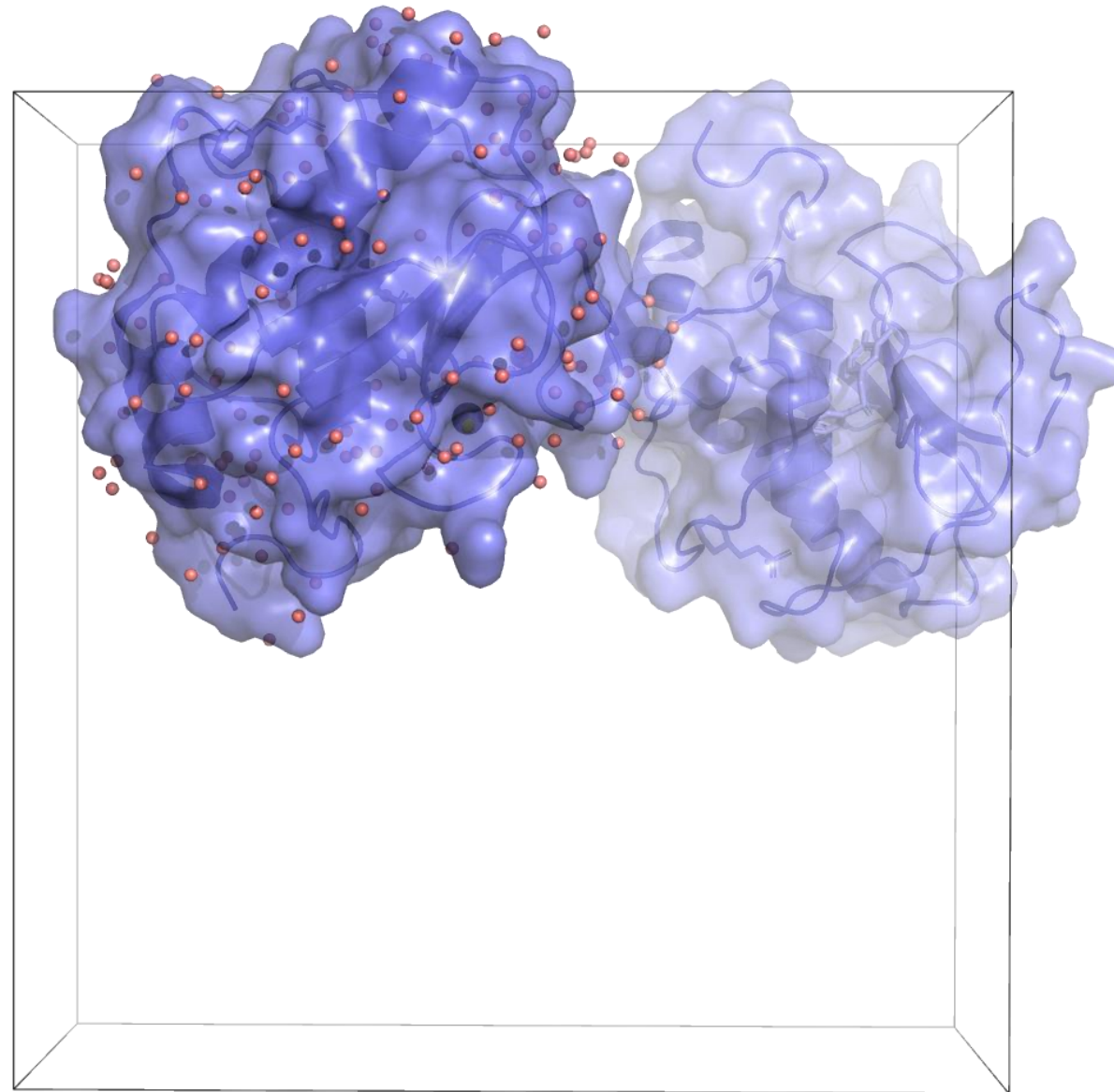
# bulk solvent : non-atomic model parameter

---



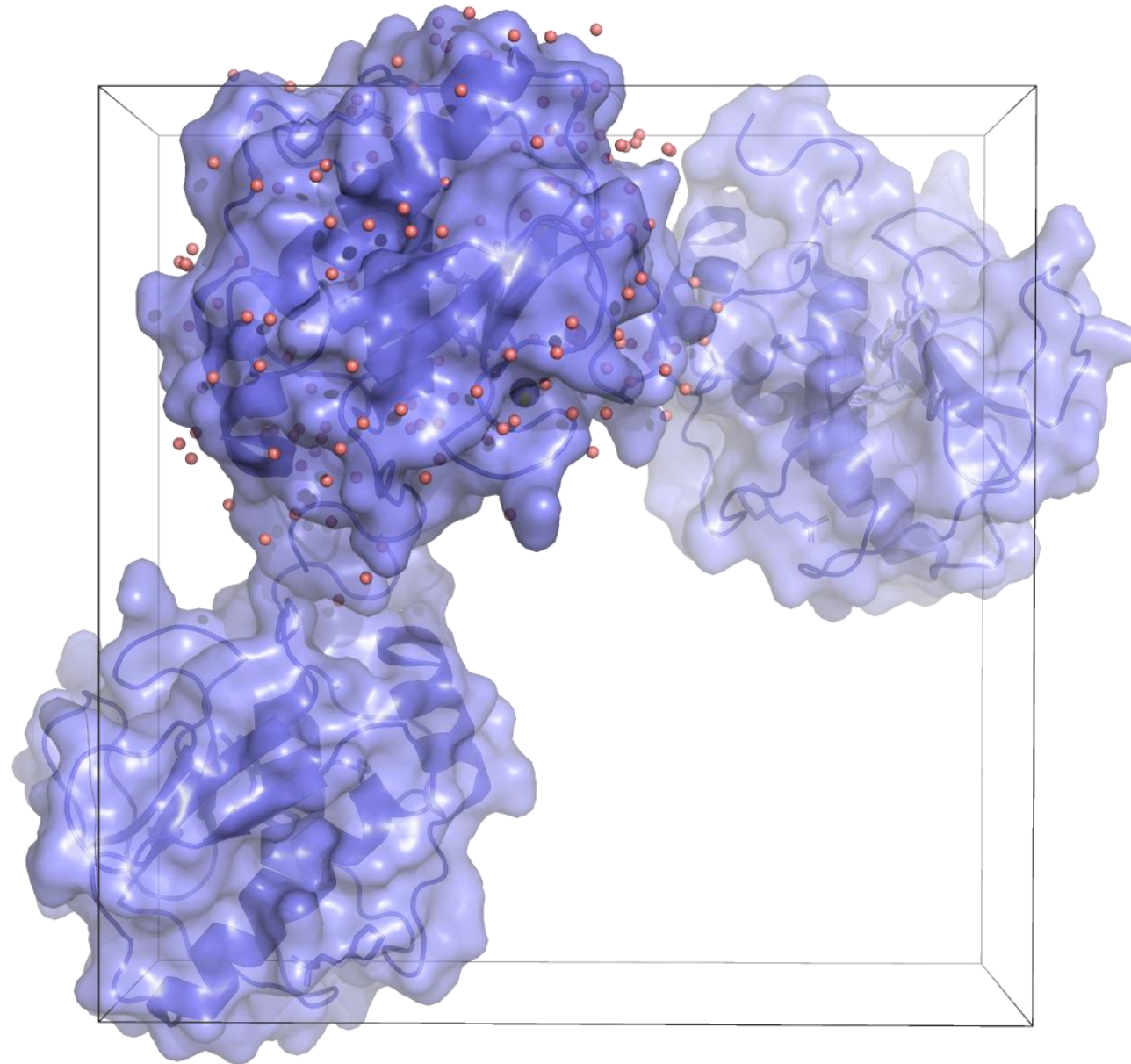
# bulk solvent : non-atomic model parameter

---



# bulk solvent : non-atomic model parameter

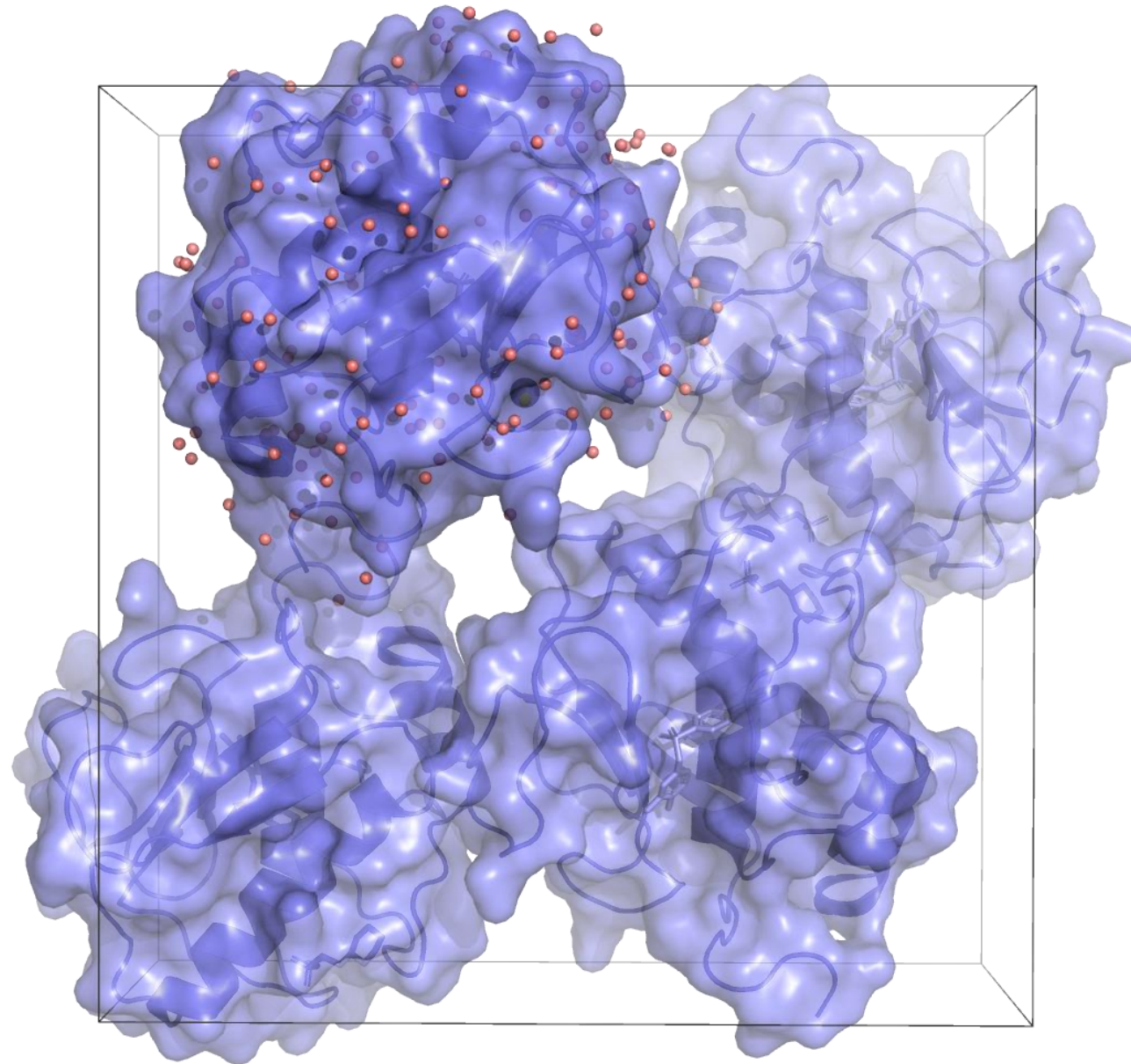
---





# bulk solvent : non-atomic model parameter

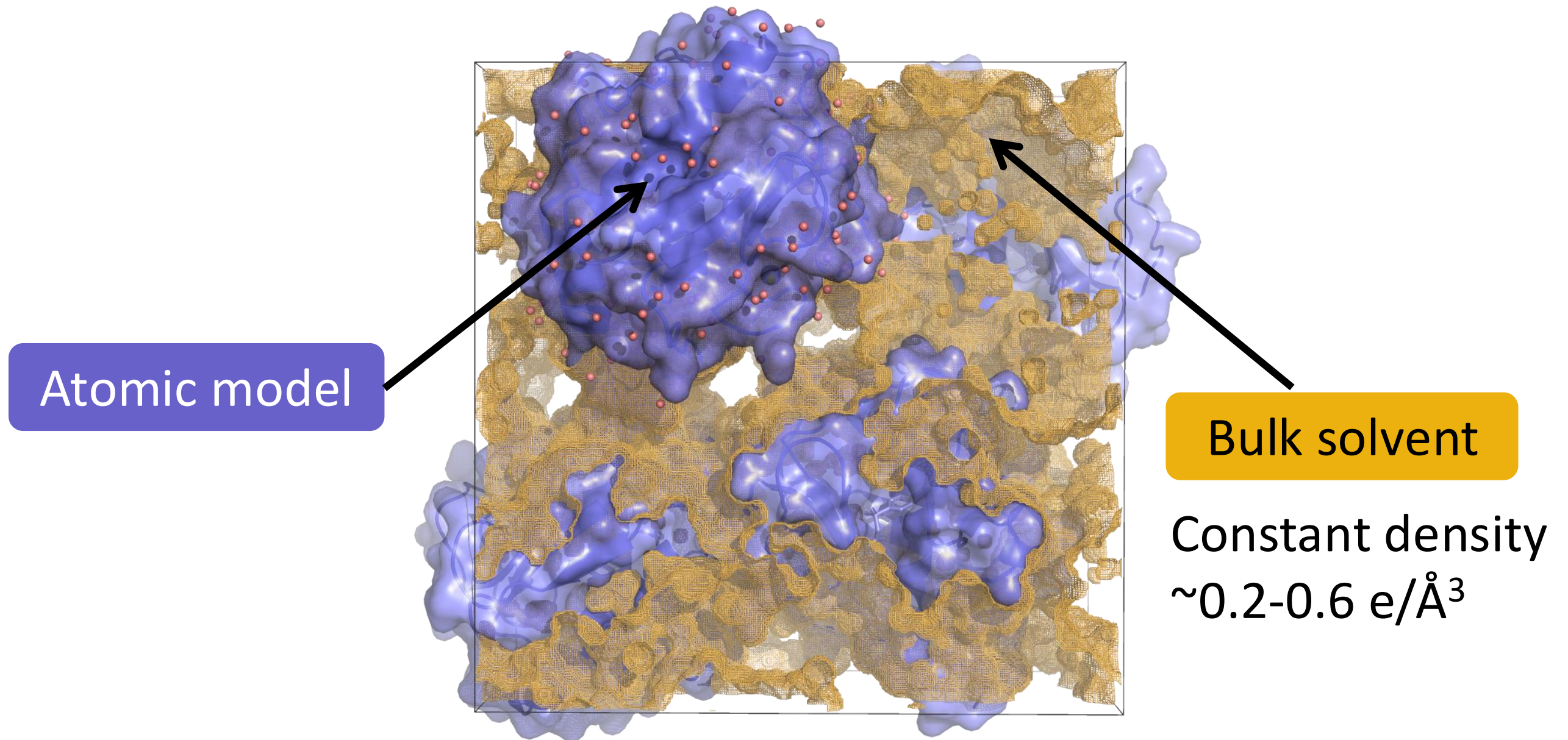
---





# bulk solvent : non-atomic model parameter

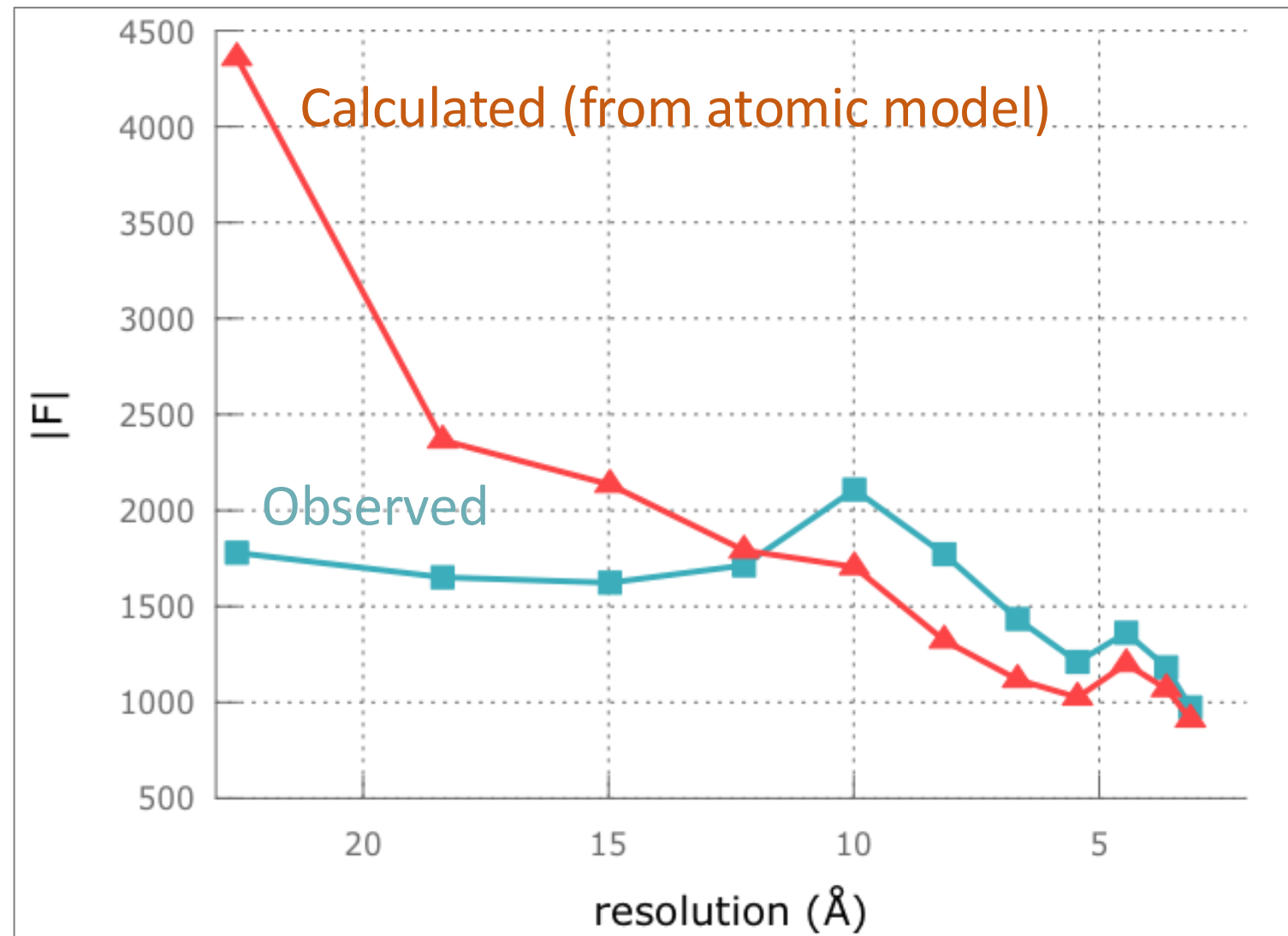
---



Account for the bulk solvent in calculated structure factors:

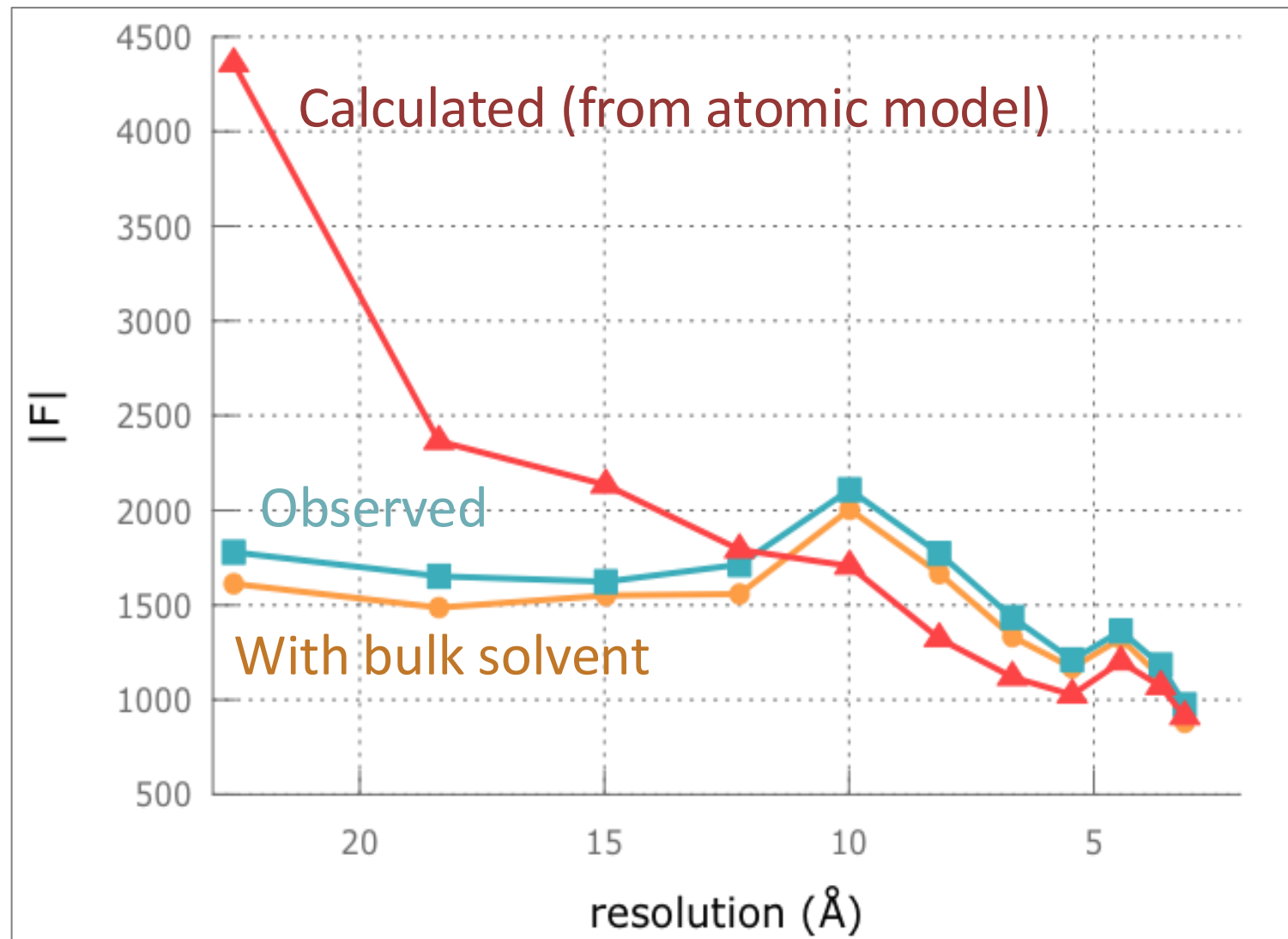
$$\mathbf{F}_{\text{model}} = k_{\text{overall}} (\mathbf{F}_{\text{calc(atoms)}} + \mathbf{F}_{\text{bulk solvent}})$$

# Why model the bulk solvent?



Bulk solvent significantly affects structure factor amplitudes at low resolution.

# Why model the bulk solvent?



**Without** bulk solvent       $R_{\text{work}} = 0.27$   $R_{\text{free}} = 0.31$

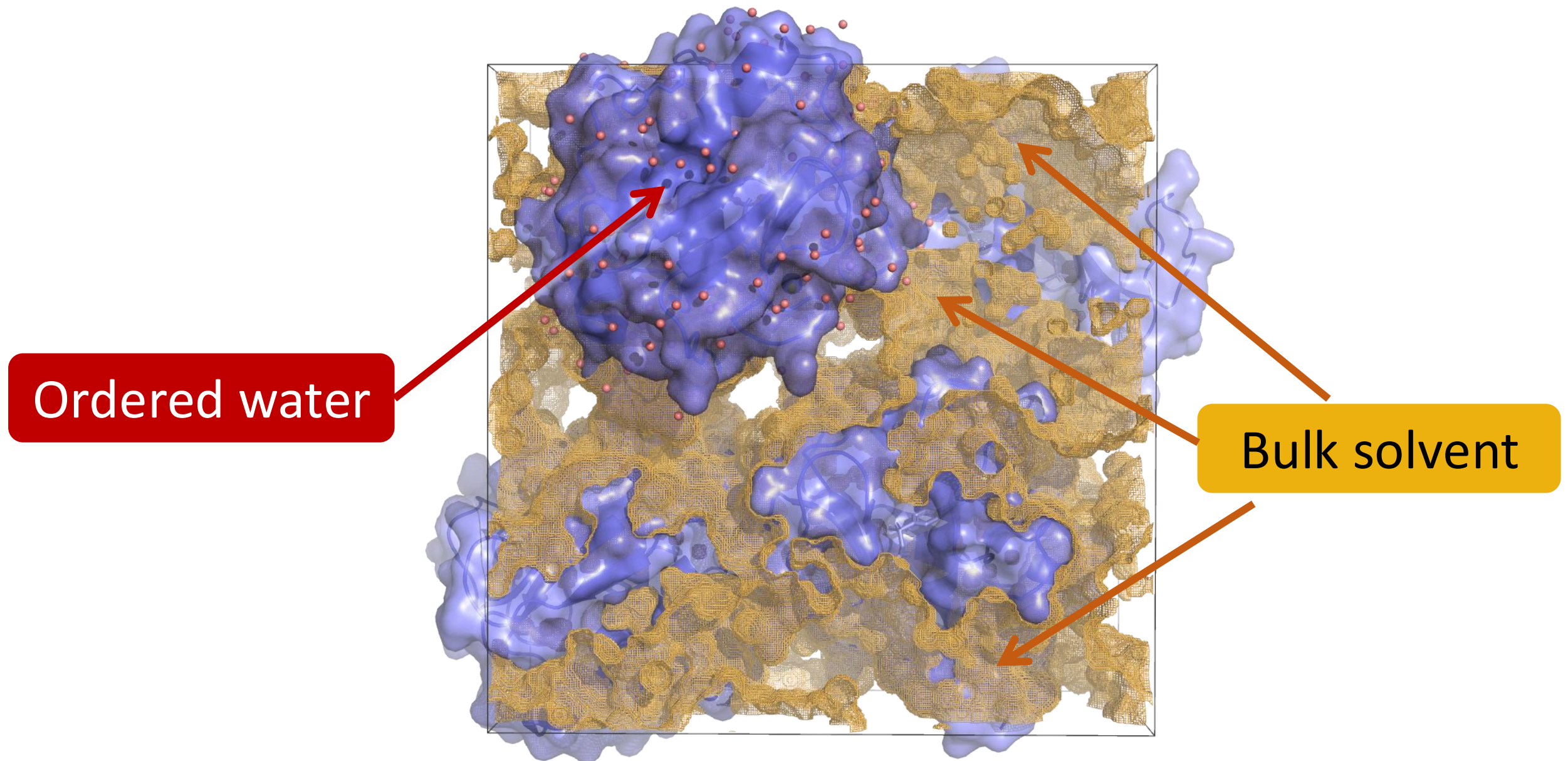
**Using** bulk solvent       $R_{\text{work}} = 0.21$   $R_{\text{free}} = 0.24$



# Bulk solvent vs ordered solvent

---

Bulk solvent is not the same as ordered solvent.



# Refinement

---

- *parameters* of a model
- *target function*
- *optimization* algorithm
- *observations*

## research papers

---

Acta Crystallographica Section D  
**Biological  
Crystallography**  
ISSN 0907-4449

### Introduction to macromolecular refinement

**Dale. E. Tronrud**

Howard Hughes Medical Institute and Institute  
of Molecular Biology, University of Oregon,  
Eugene, OR 97403, USA

The process of refinement is such a large problem in function minimization that even the computers of today cannot perform the calculations to properly fit X-ray diffraction data. Each of the refinement packages currently under development reduces the difficulty of this problem by utilizing a unique combination of targets, assumptions, and optimization

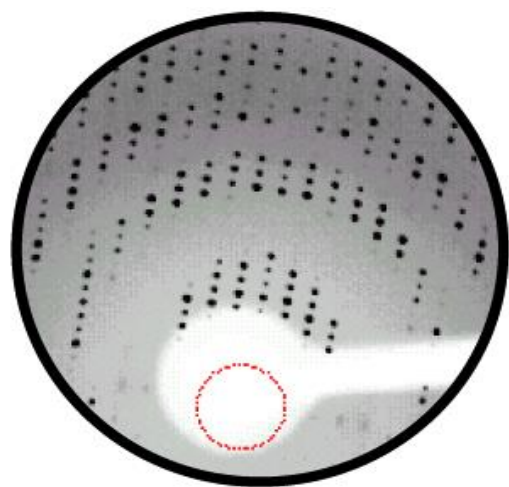
Received 5 April 2004  
Accepted 21 September 2004

Tronrud, D. E. Introduction to macromolecular refinement. Acta Crystallogr. D Biol. Crystallogr. 60, 2156–2168 (2004).

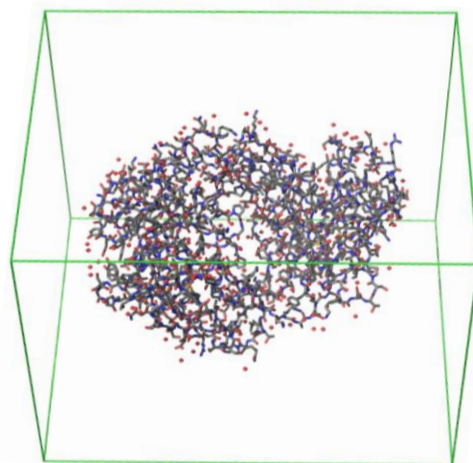
# Target function

Score the model against the experimental data,. i.e. compare model-based and measured structure factor amplitudes.

Experimental data

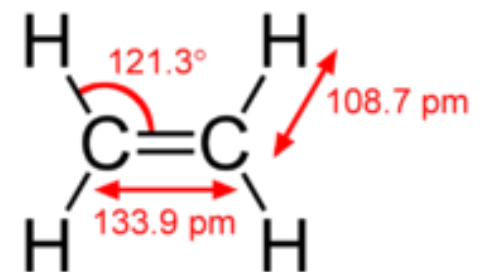


Model



A priori knowledge

Example:  
Covalent geometry



$$T = T_{Data}(F_{obs}, F_{Model}) + wT_{Restrains}$$

# Target function

---

Score the model against the experimental data,. i.e. compare model-based and measured structure factor amplitudes.

## 1. Least squares

$$T_{Data} = w_{xray} \sum_{hkl} \frac{1}{\sigma^2} (|F_{obs}| - |F_{model}|)^2$$

$\sigma$  = Standard deviation

- Large difference between observed and calculated structure factor  
→ The model is inaccurate.
- Small standard deviation  $\sigma$   
→ That observation will be important in the sum.

# Target function

---

Score the model against the experimental data,. i.e. compare model-based and measured structure factor amplitudes.

## 1. Least squares

$$T_{Data} = w_{xray} \sum_{hkl} \frac{1}{\sigma^2} (|F_{obs}| - |F_{model}|)^2$$

### **Assumptions of this approach:**

- Errors obey a Gaussian distribution.

It is impossible for any set of parameters of an imperfect model (e.g. missing domain) to reproduce all the observed structure factors.



# Target function

---

Score the model against the experimental data,. i.e. compare model-based and measured structure factor amplitudes.

## 2. Maximum Likelihood (ML)

“Maximize the probability (likelihood) that the observed data would be produced given the current model.”

Computing this exactly requires **fully modeling all sources of error**, but we cannot model all errors in complete generality.

→ Make assumptions about the nature of the uncertainties in the observations and the model parameters.

Method of choice for macromolecular crystallography.

# Refinement

---

- *parameters* of a model
- *target function*
- *optimization algorithm*
- *observations*

## research papers

---

Acta Crystallographica Section D  
**Biological  
Crystallography**  
ISSN 0907-4449

### Introduction to macromolecular refinement

**Dale. E. Tronrud**

Howard Hughes Medical Institute and Institute  
of Molecular Biology, University of Oregon,  
Eugene, OR 97403, USA

The process of refinement is such a large problem in function minimization that even the computers of today cannot perform the calculations to properly fit X-ray diffraction data. Each of the refinement packages currently under development reduces the difficulty of this problem by utilizing a unique combination of targets, assumptions, and optimization

Received 5 April 2004  
Accepted 21 September 2004

Tronrud, D. E. Introduction to macromolecular refinement. Acta Crystallogr. D Biol. Crystallogr. 60, 2156–2168 (2004).

# Optimization algorithm

The purpose of the optimization algorithm is to minimize the target function.

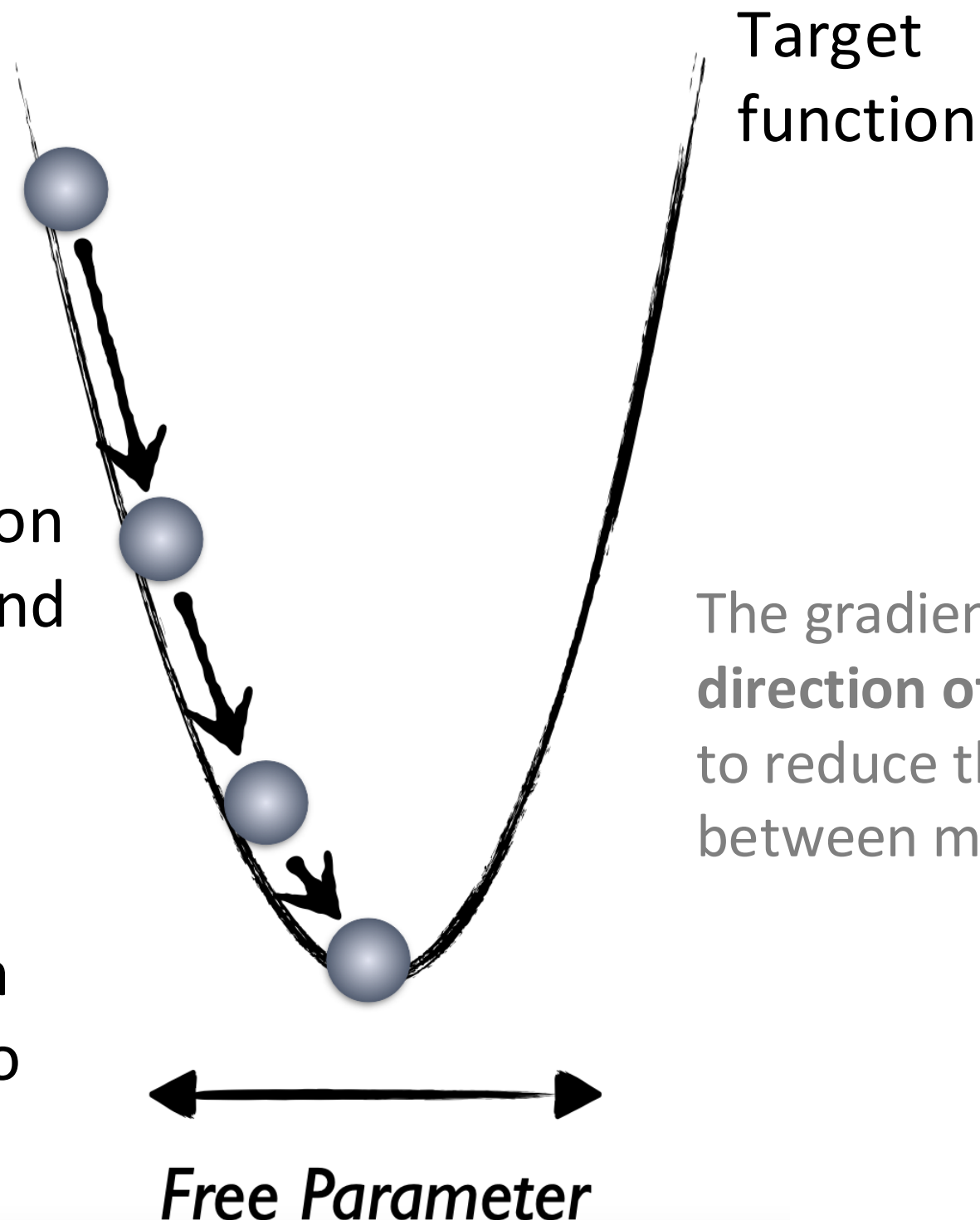
Starting model



- Evaluate target function
- Compute gradients (and second derivatives)



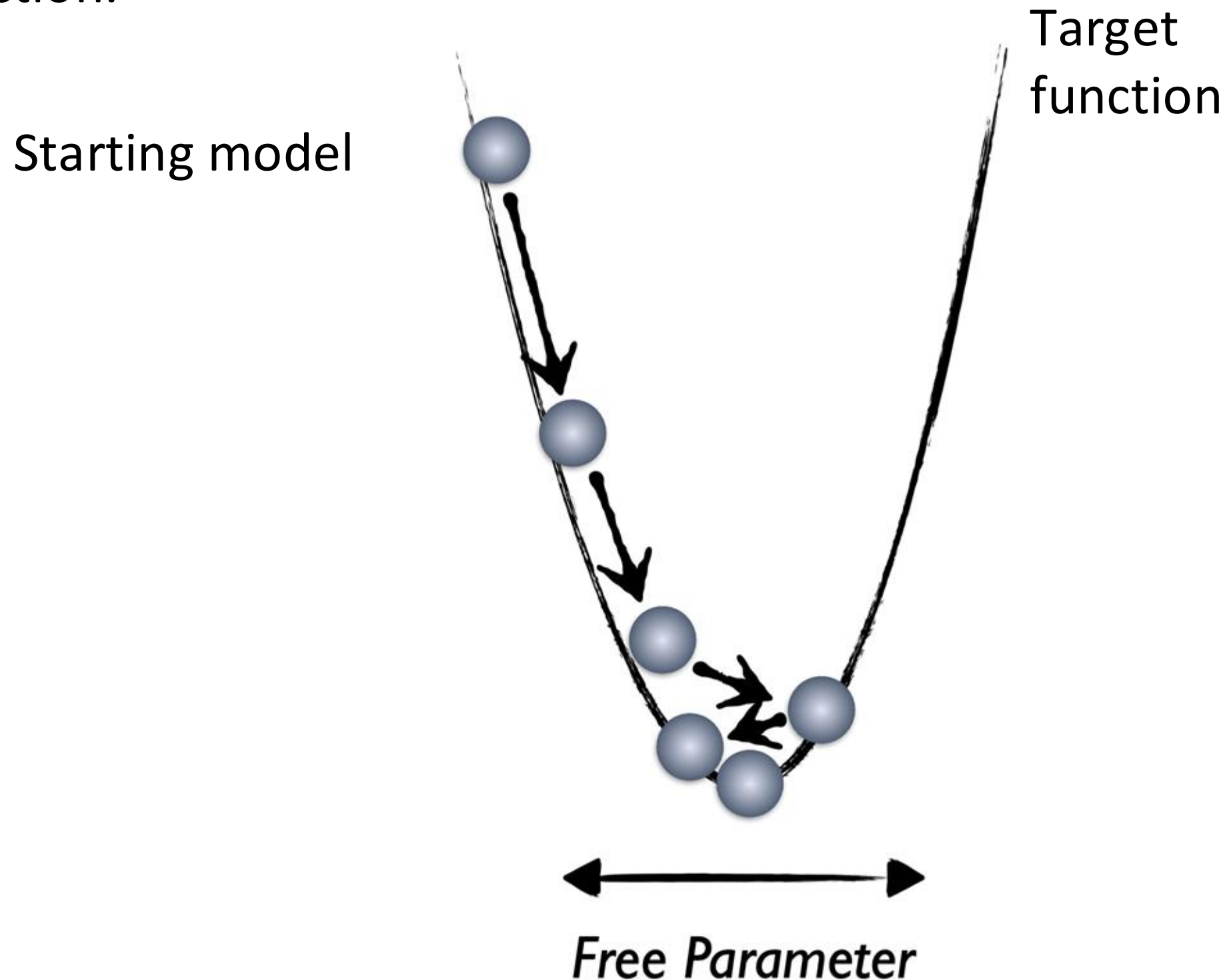
Optimization algorithm calculates how much to move each parameter.



# Optimization algorithm

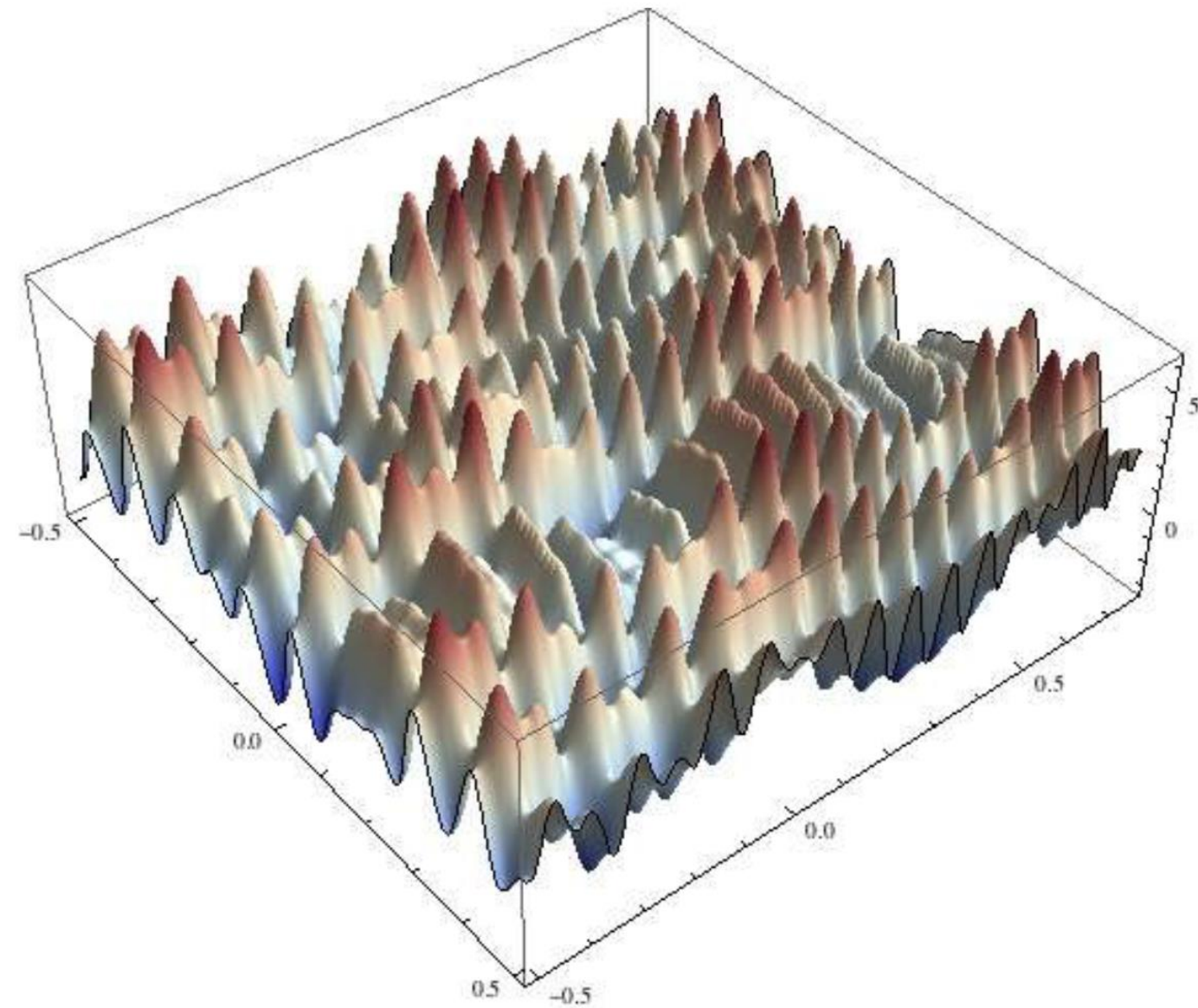
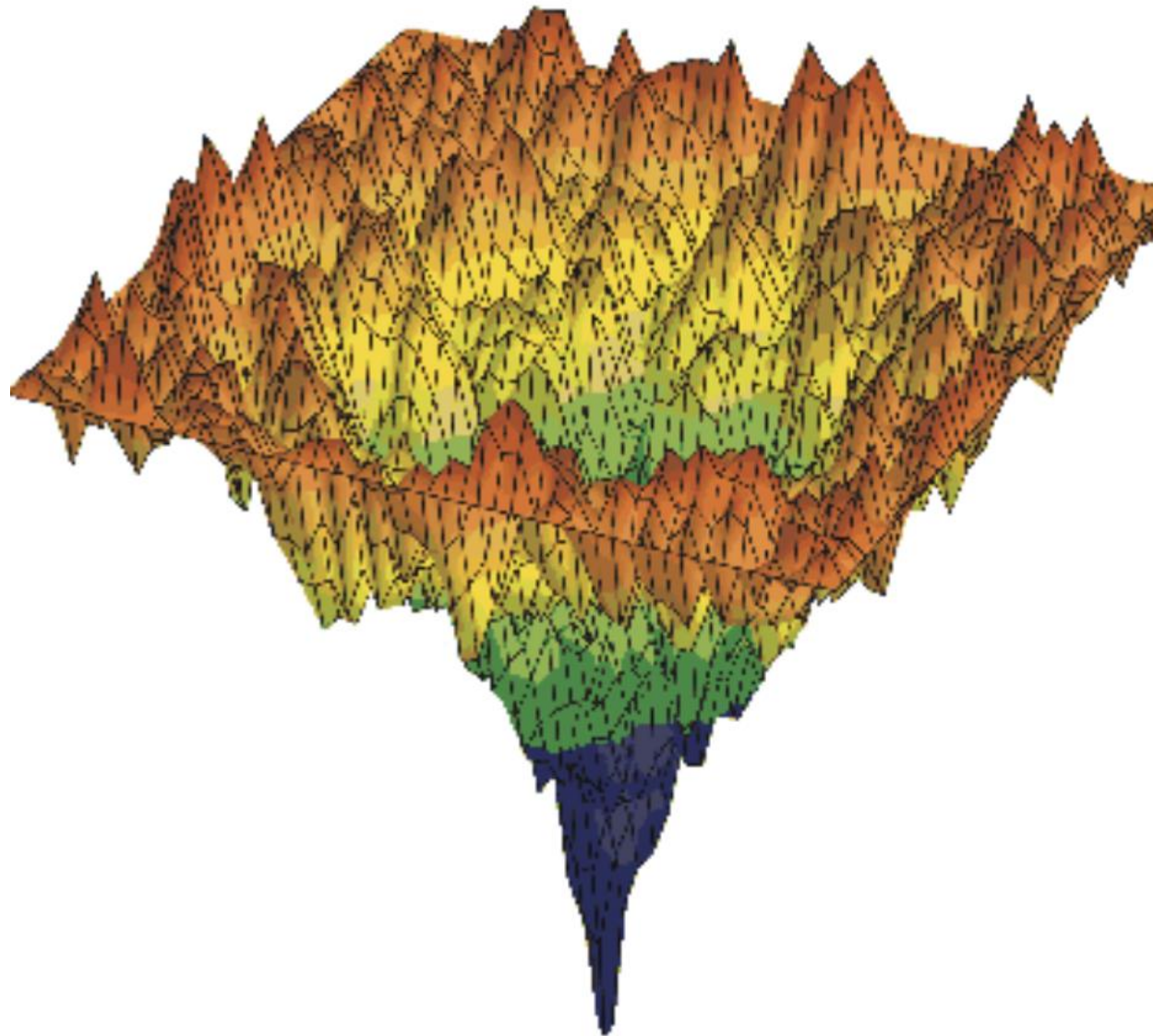
---

The purpose of the optimization algorithm is to minimize the target function.



# The target function is complex

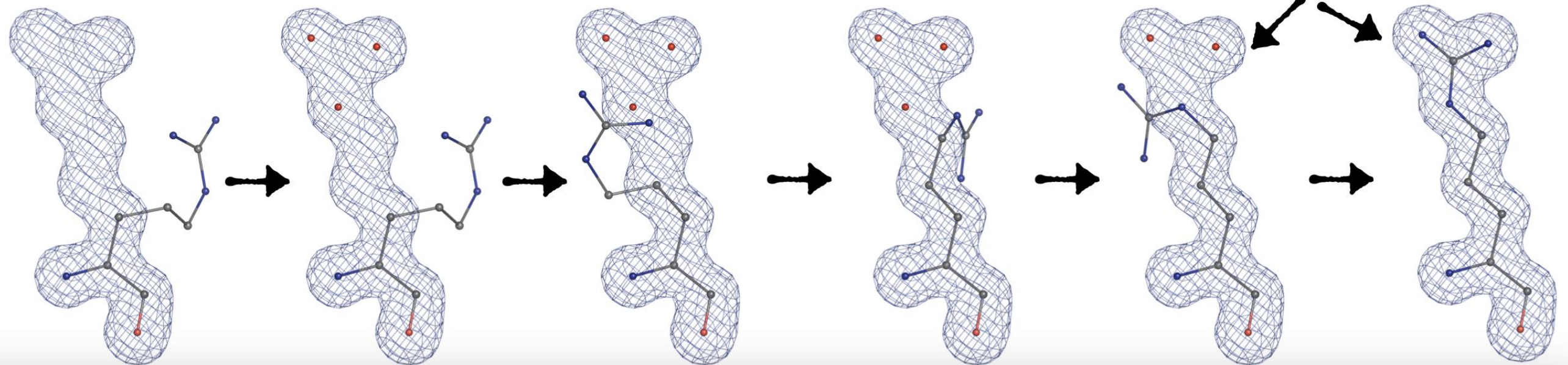
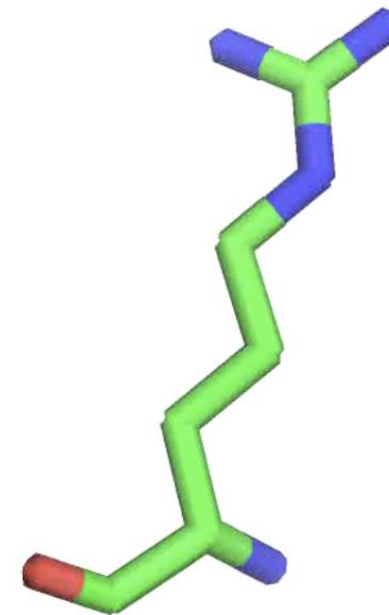
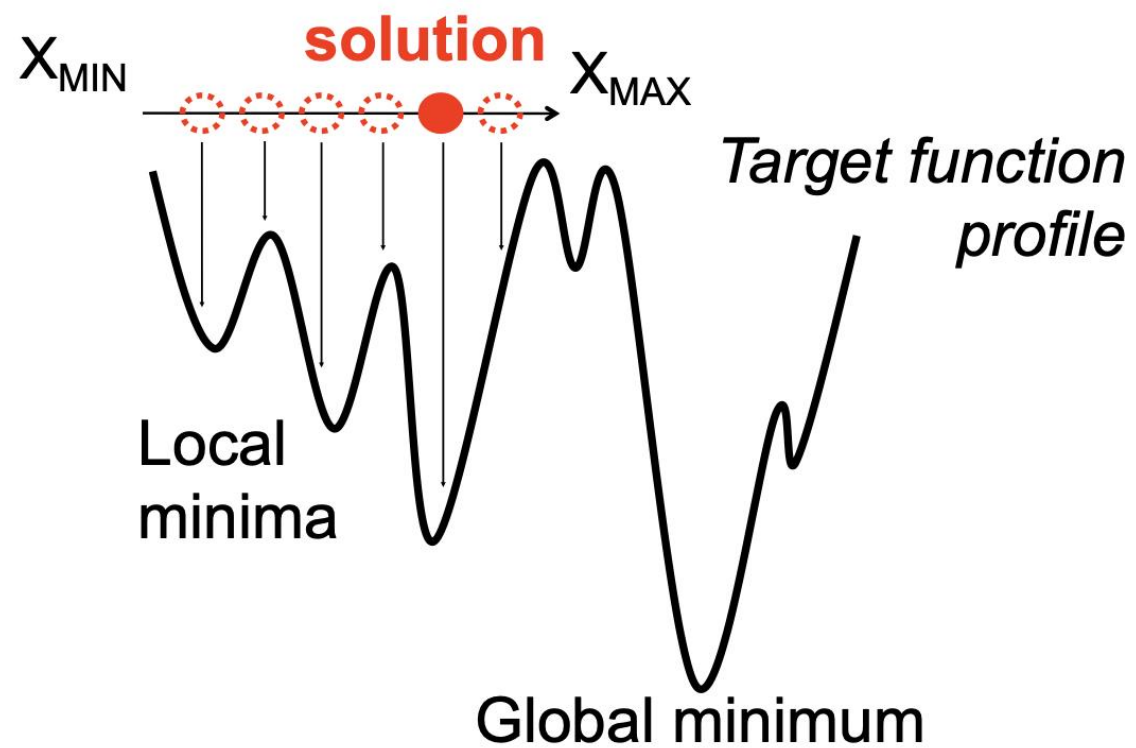
---



*From Robb Seaton's "The Ultimate Guide to Simulated Annealing"*



# Systematic searching



# Simulated Annealing

---

Physical process of **annealing** (metallurgy):

Heat a material and then slowly cool it so its atoms settle into a low-energy, stable structure.

In crystallographic refinement:

Introduce **controlled random changes** to model parameters (xyz, torsions). Introduce “heat” via a molecular dynamics simulation.

When to use:

- Poorly built structures early in refinement.
- Particular need to remove bias (changing Rfree).

# Refinement

---

- *parameters* of a model
- *target function*
- *optimization* algorithm
- *observations*

## research papers

---

Acta Crystallographica Section D  
**Biological  
Crystallography**  
ISSN 0907-4449

### Introduction to macromolecular refinement

**Dale. E. Tronrud**

Howard Hughes Medical Institute and Institute  
of Molecular Biology, University of Oregon,  
Eugene, OR 97403, USA

The process of refinement is such a large problem in function minimization that even the computers of today cannot perform the calculations to properly fit X-ray diffraction data. Each of the refinement packages currently under development reduces the difficulty of this problem by utilizing a unique combination of targets, assumptions, and optimization

Received 5 April 2004  
Accepted 21 September 2004

Tronrud, D. E. Introduction to macromolecular refinement. Acta Crystallogr. D Biol. Crystallogr. 60, 2156–2168 (2004).



# Observations

---

Observations = Everything known about the crystal

- structure-factor amplitudes
- unit-cell parameters
- standardized stereochemistry
- experimentally determined phase information

*Restraints* will add observations.

# What to change in refinement?

Strategy

Refinement strategy : ☒ XYZ (reciprocal-space) ☒ XYZ (real-space) ☐ Rigid body ☒ Individual B-factors ☐ Group B-factors ☐ TLS parameters ☒ Occupancies ☐ Anomalous groups ?

Number of cycles : 3

Select Atoms Note: selections can only be made for enabled options (e.g. NCS groups are available if "Use NCS" box is checked)

Targets and weighting

Target function : Automatic ☐ Optimize X-ray/stereochemistry weight ☐ Optimize X-ray/ADP weight

☐ Use NCS NCS type : torsion-angle Automatic linking options

☐ Reference model restraints ☐ Use secondary structure restraints ☒ Use experimental phase restraints

Refinement target weights... Model interpretation... NCS options ?

Other options

☐ Automatically add hydrogens to model ☐ Update waters Place elemental ions :

☐ Simulated annealing (Cartesian) ☐ Simulated annealing (Torsion angles) Scattering table : n\_gaussian

☒ Automatically correct N/Q/H errors Number of processors : 1 ?

Global refinement parameters... Modify start model... All parameters... ?

Which options shall I use? Which parameters shall I change?

phenix.refine has >1k parameters.

# What to change in refinement?

---

- *parameters* of a model
  - *target function*
  - *optimization* algorithm
  - *observations*
- } Set by refinement program

# What to change in refinement?

---

- *parameters of a model* ←
- *target function*
- *optimization* algorithm
- *observations* ←

In practice, you'll change the **model parameterization** and modify the a priori information (observations) via **restraints**.

There is no recipe for what to change. Needs to be adapted to each case.

Consider refinement like an experiment. You try and analyze the result.

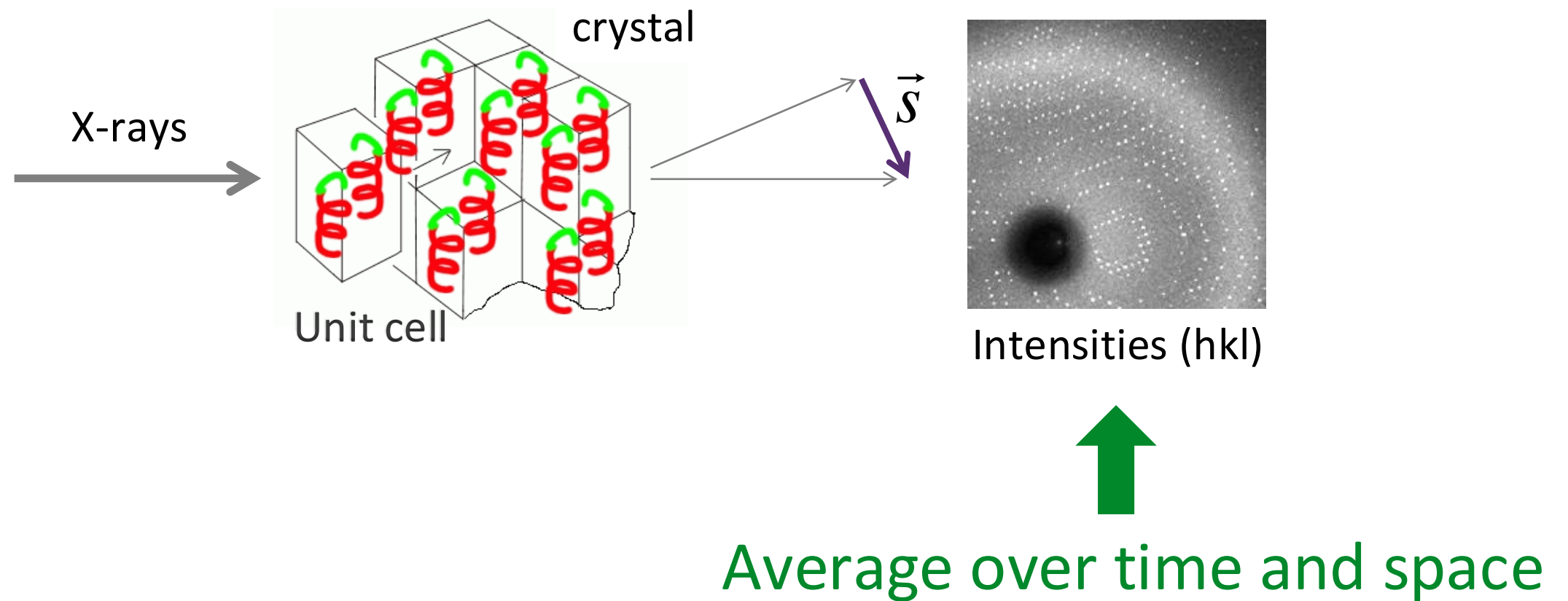
# What to change in refinement?

---

- *parameters of a model* ←
- *target function*
- *optimization* algorithm
- *observations* ←

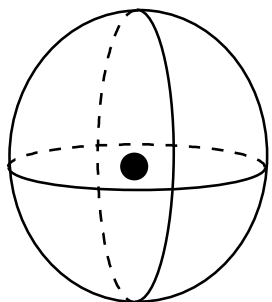
Some examples of *model parameterization* that can be changed.

# Atomic displacements



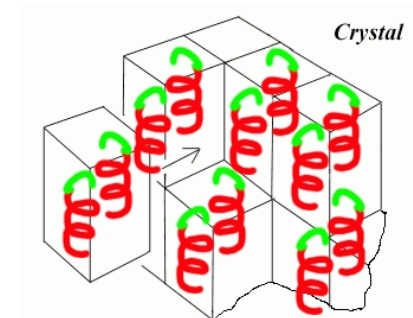
## Time:

Atoms are in thermal motions around mean positions.



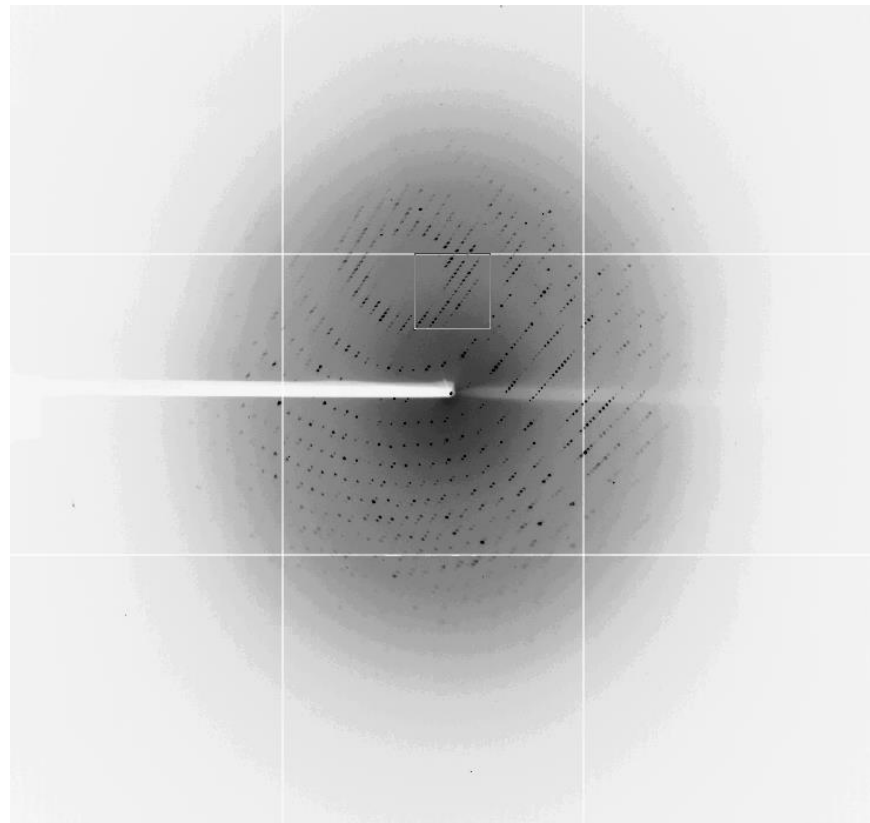
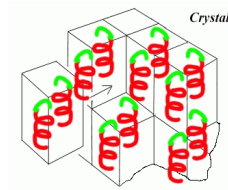
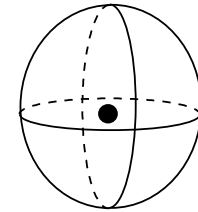
## Space:

Small differences between unit cells.



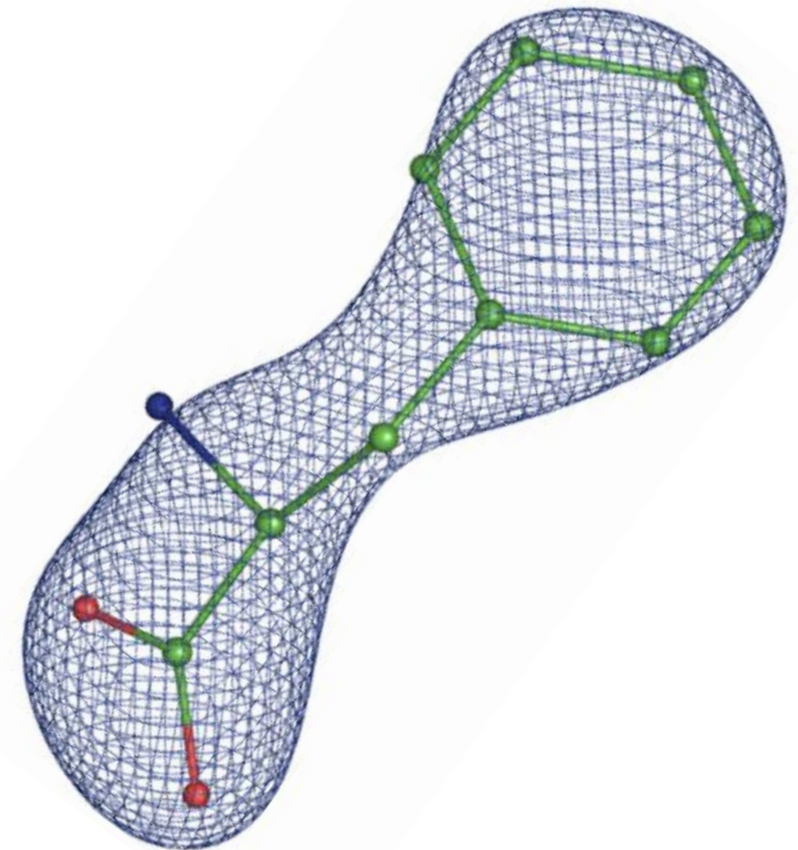
# Atomic displacements

Displacements of atoms in the sample



Reciprocal space:  
High-resolution data vanish

Real space:  
Density is blurred



Displacement need to be modelled

# Atomic displacements

---

**Superposition of several contributions:**

$$U_{\text{total}} = U_{\text{cryst}} + U_{\text{group}} + U_{\text{local}}$$



# Atomic displacements

---

**Superposition of several contributions:**

$$U_{\text{total}} = U_{\text{cryst}} + U_{\text{group}} + U_{\text{local}}$$

$U_{\text{cryst}}$  = displacement of the crystal as a whole

# Atomic displacements

---

**Superposition of several contributions:**

$$U_{\text{total}} = U_{\text{cryst}} + U_{\text{group}} + U_{\text{local}}$$

$U_{\text{cryst}}$  = displacement of the crystal as a whole

$U_{\text{group}}$  = concerted motions of multiple atoms (group motions)

# Atomic displacements

---

**Superposition of several contributions:**

$$U_{\text{total}} = U_{\text{cryst}} + U_{\text{group}} + U_{\text{local}}$$

$U_{\text{cryst}}$  = displacement of the crystal as a whole

$U_{\text{group}}$  = concerted motions of multiple atoms (group motions)

$U_{\text{local}}$  = small local atomic vibrations

# Atomic displacements

---

## Superposition of several contributions:

$$U_{\text{total}} = U_{\text{cryst}} + U_{\text{group}} + U_{\text{local}}$$

$U_{\text{cryst}}$  = displacement of the crystal as a whole

Done  
automatically

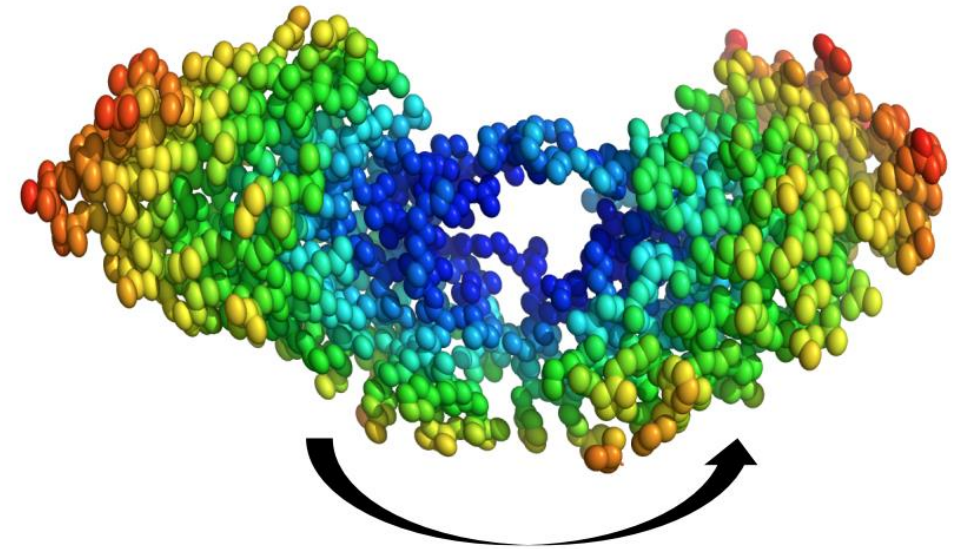
$U_{\text{group}}$  = concerted motions of multiple atoms (group motions)

$U_{\text{local}}$  = small local atomic vibrations

# Atomic displacements: $U_{\text{group}}$

---

- TLS: rigid body displacements of molecules, domains, secondary structure elements



Displacement of a **rigid body** can be described by

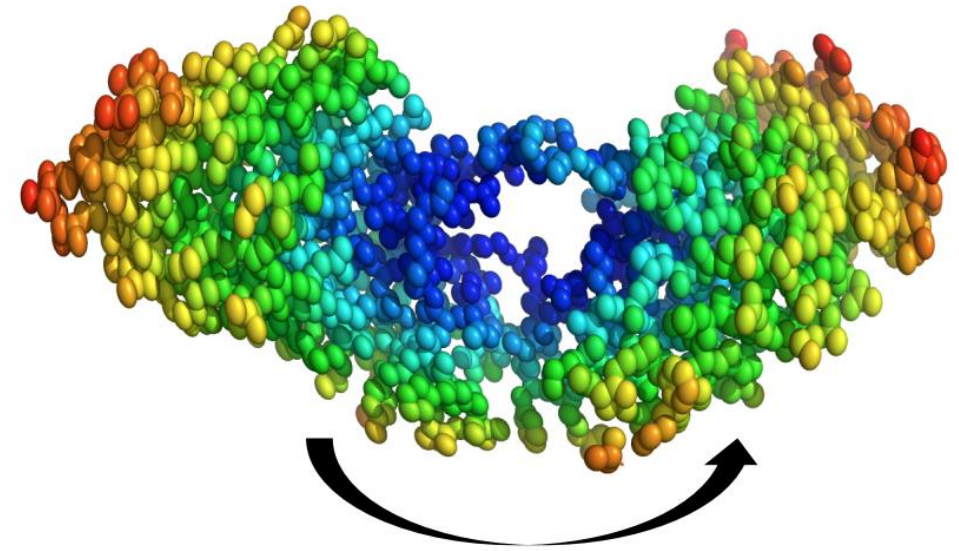
- **T**ranslation
- Rotation (**L**ibration)
- Correlation between them (**S**crew)

➡ Partition the model into TLS groups

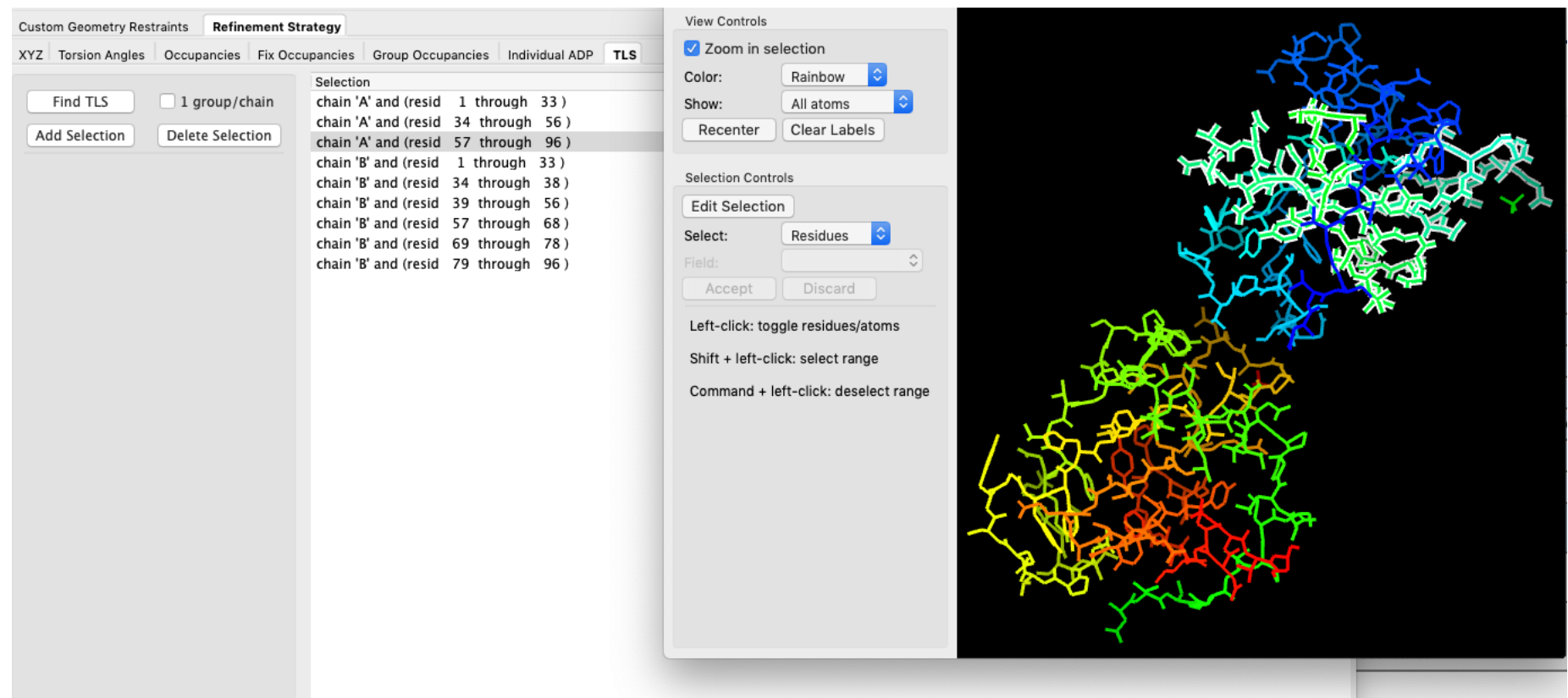
In phenix.refine, partitioning needs refined B-factors, so don't turn on right after MR.

# Atomic displacements: $U_{\text{group}}$

- TLS: rigid body displacements of molecules, domains, secondary structure elements



Can be done automatically in the Phenix GUI.



Custom Geometry Restraints   **Refinement Strategy**

XYZ   Torsion Angles   Occupancies   Fix Occupancies   Group Occupancies   Individual ADP   **TLS**

Find TLS   ☐ 1 group/chain  
Add Selection   Delete Selection

Selection

chain 'A' and (resid	1 through 33 )
chain 'A' and (resid	34 through 56 )
chain 'A' and (resid	57 through 96 )
chain 'B' and (resid	1 through 33 )
chain 'B' and (resid	34 through 38 )
chain 'B' and (resid	39 through 56 )
chain 'B' and (resid	57 through 68 )
chain 'B' and (resid	69 through 78 )
chain 'B' and (resid	79 through 96 )

View Controls

☒ Zoom in selection

Color: Rainbow

Show: All atoms

Recentre   Clear Labels

Selection Controls

Edit Selection

Select: Residues

Field:

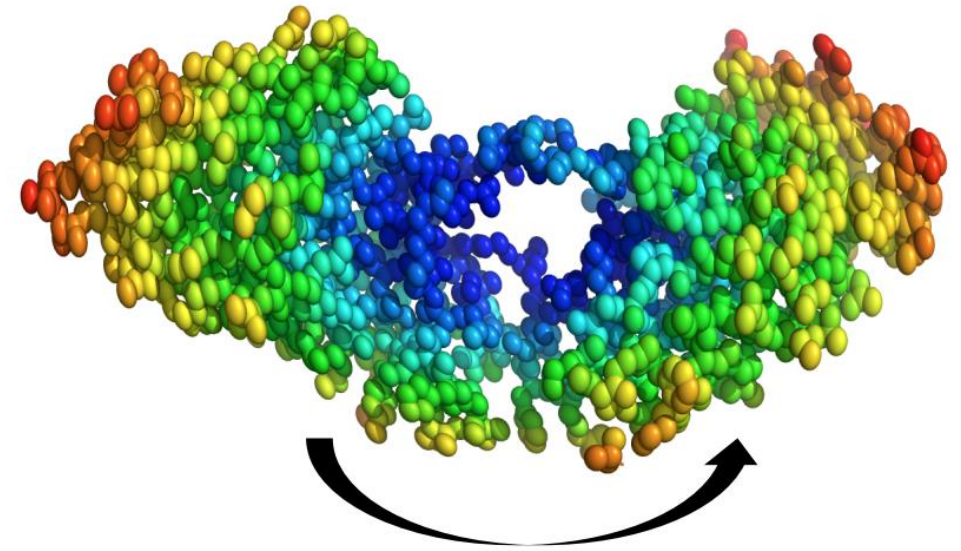
Accept   Discard

Left-click: toggle residues/atoms  
Shift + left-click: select range  
Command + left-click: deselect range

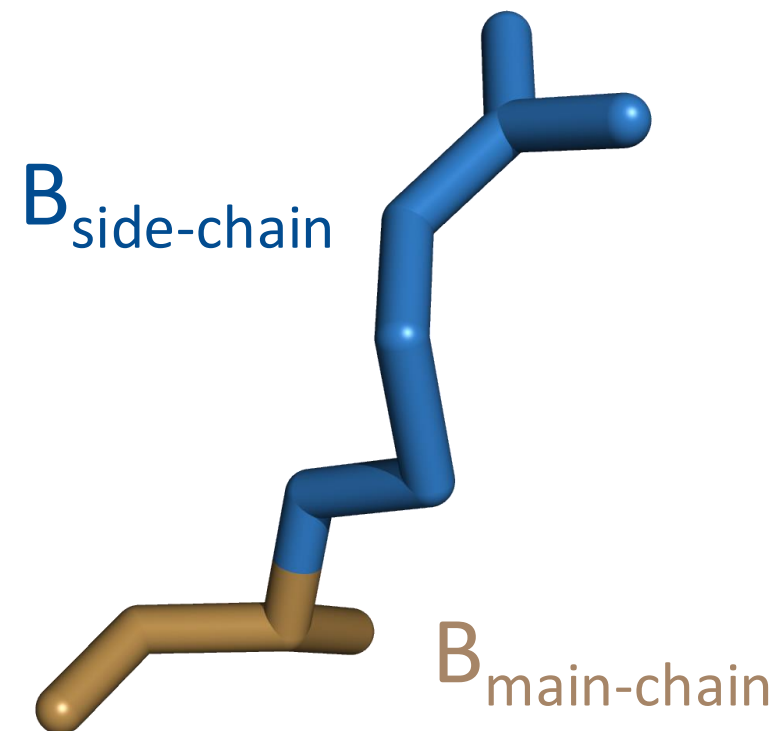
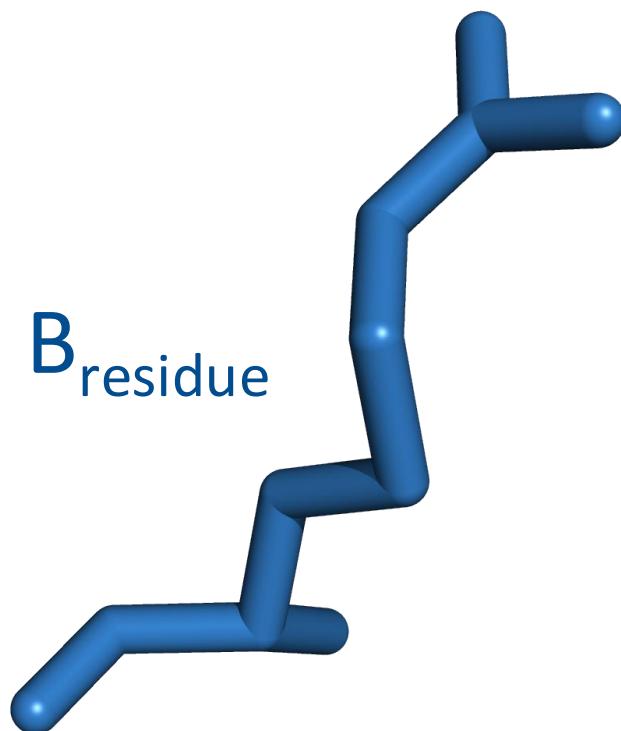
# Atomic displacements: $U_{\text{group}}$

---

- TLS: rigid body displacements of molecules, domains, secondary structure elements



- Simple group isotropic model (one single  $B_{\text{iso}}$ ), entire residue or main chain – side chain

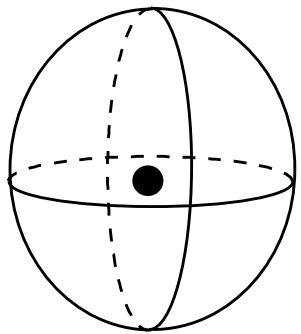




# Atomic displacements: $U_{\text{local}}$

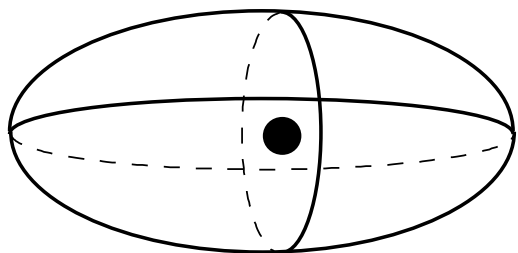
---

- Describe small local atomic vibrations
- "per atom"
- Represent both thermal vibration, and variation in the atomic positions from one unit cell to the next



**$B_{\text{iso}}$**

- related to the mean-square amplitude of vibration
- one isotropic displacement parameter per atom

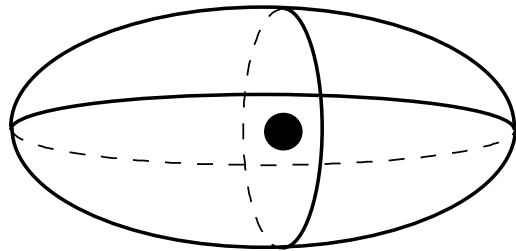


**$B_{\text{aniso}}$**

- describe a probability distribution for the electron density with a 3d Gaussian
- 3x3 symmetric tensor (6 parameters)

# Atomic displacements: $U_{\text{local}}$

---



- $B_{\text{aniso}}$  is more “realistic”.
- But they **double** the number of parameters.

xyz+ occ +  $B_{\text{iso}}$

3 + 1 + 1

xyz+ occ +  $B_{\text{aniso}}$

3 + 1 + 6

- Requires more observations to be feasible (resolution).

# Atomic displacements: which one to choose?

---

It depends...

(data resolution, data quality, data-to-parameter ratio,...)

Around 1.5Å: can try anisotropic B-factors  
(all non-H atoms or only protein?)

TLS: can be applied at most resolution ranges.  
(cannot do individual anisotropic ADP and TLS)

Group B-factors: low resolution  
(per residue or mainchain/sidechain?)

# Occupancy refinement

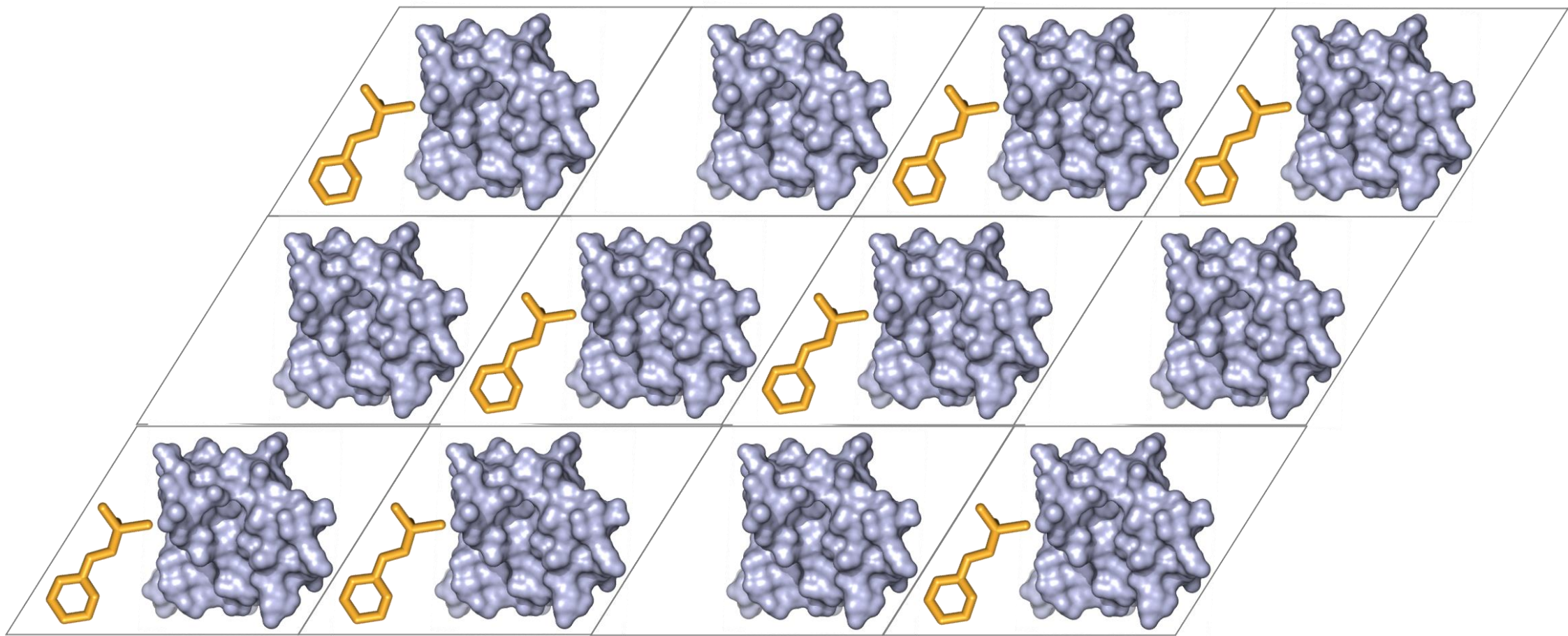
---

Occupancy models disorder beyond the harmonic approximation:

# Occupancy refinement

Occupancy models disorder beyond the harmonic approximation:

- Atoms are not present in every unit cell (e.g. ligand, ion)

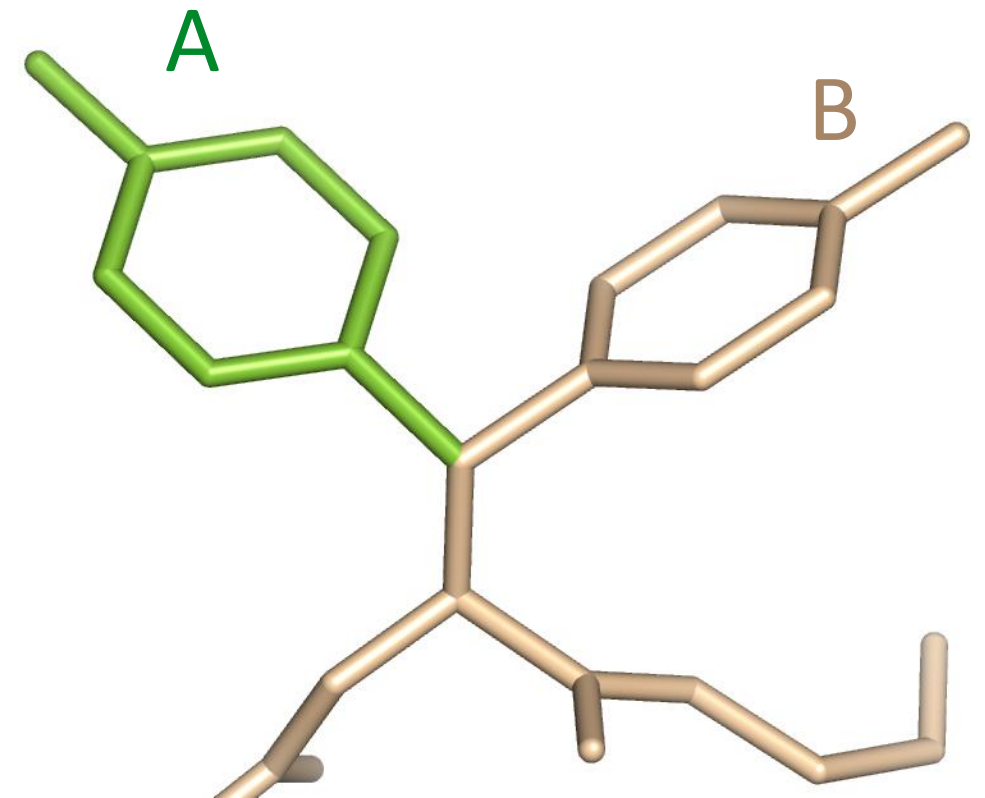
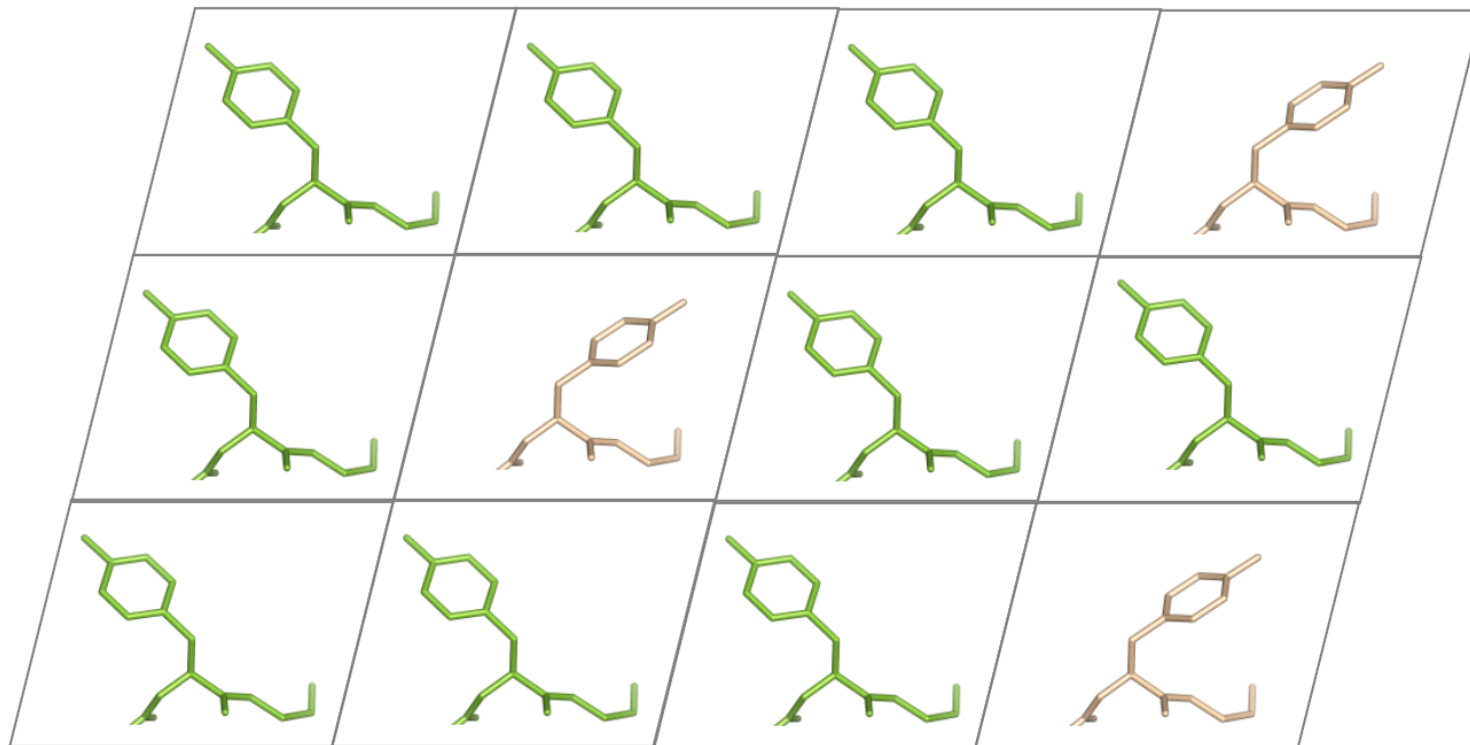


$$\text{OCC}_{\text{ligand}} < 1$$

# Occupancy refinement

Occupancy models disorder beyond the harmonic approximation:

- Atoms are not present in every unit cell (e.g. ligand, ion)
- Atoms are in alternative conformation



$$\text{OCC}_A + \text{OCC}_B = 1$$



# Occupancy refinement

---

## How to refine the occupancy :

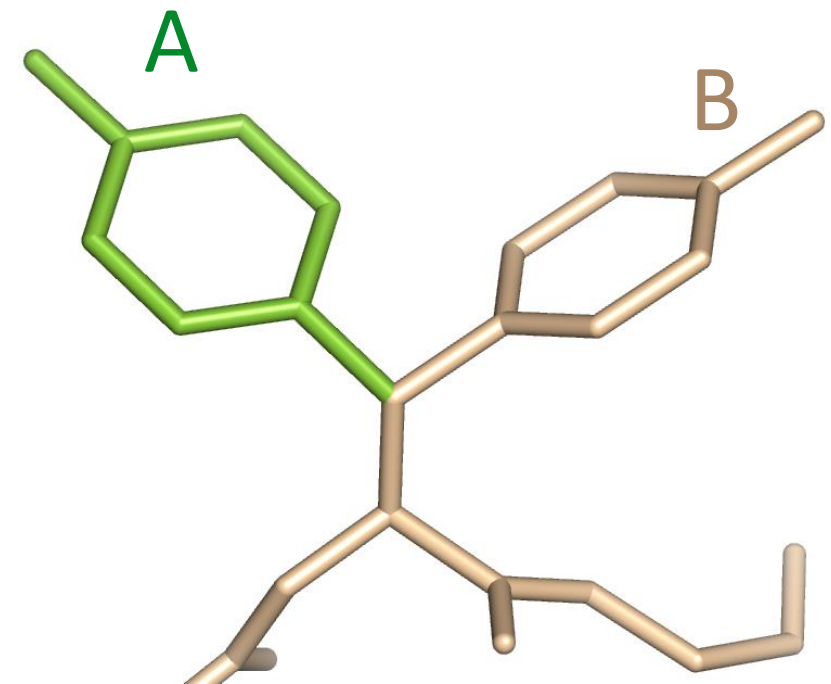
- Set the occupancy of atoms to a value  $< 1$  (Coot, PDB tools, ...)

## How to refine alternative conformations:

- Add alternative conformation in a molecular viewer (Coot)
- Activate occupancy refinement

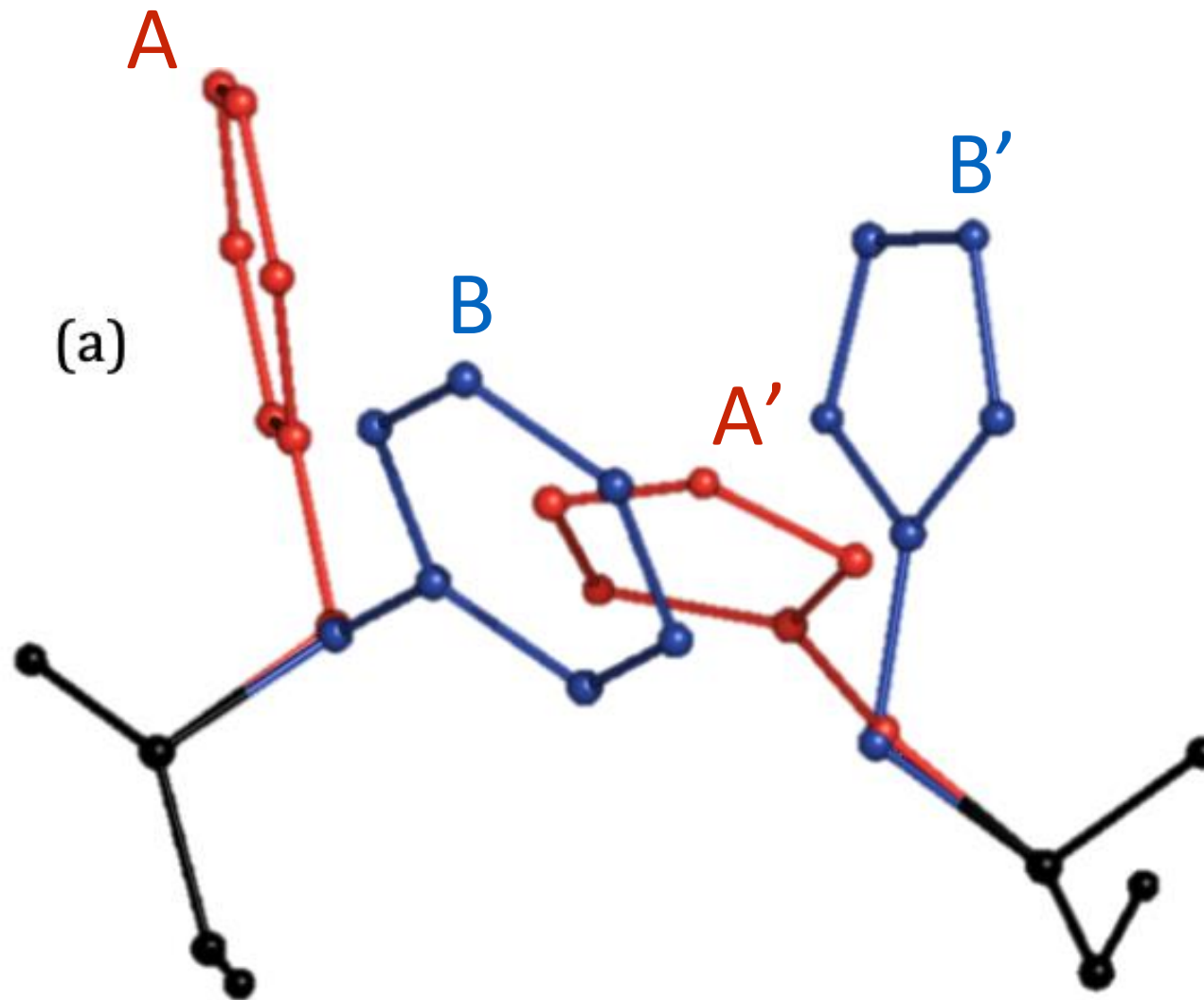
phenix.refine:

Occupancy refinement is on by default.  
Will only refine atoms with  $occ < 1$ .



# Occupancy refinement

## Concerted (coupled) conformations



$$\text{OCC}_A + \text{OCC}_B = 1$$

$$\text{OCC}_{A'} + \text{OCC}_{B'} = 1$$

$$\text{OCC}_B + \text{OCC}_{A'} = 1$$

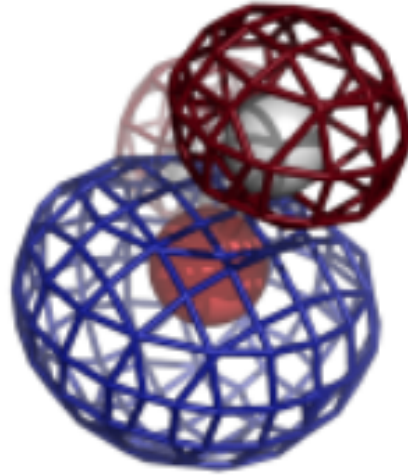
$$\text{OCC}_A = \text{OCC}_{A'}$$

You can couple the two alternative conformations.

```
refinement {  
  refine {  
    occupancies {  
      constrained_group {  
        selection = chain A and resseq 73 and altloc A or \  
                    chain B and resseq 90 and altloc A or \  
        selection = chain A and resseq 73 and altloc B or \  
                    chain B and resseq 90 and altloc B or  
      }  
    }  
  }  
}
```

# Occupancy refinement

VOLUME SIX



## COMPUTATIONAL CRYSTALLOGRAPHY NEWSLETTER

JULY MMXV

PHASER GUI, ALT. LOCS, BASE-PAIR STACKING

SHORT COMMUNICATIONS

**13 typical occupancy refinement scenarios and available options in  
*phenix.refine***

Pavel V. Afonine

*Lawrence Berkeley National Laboratory, Berkeley, CA 94720*

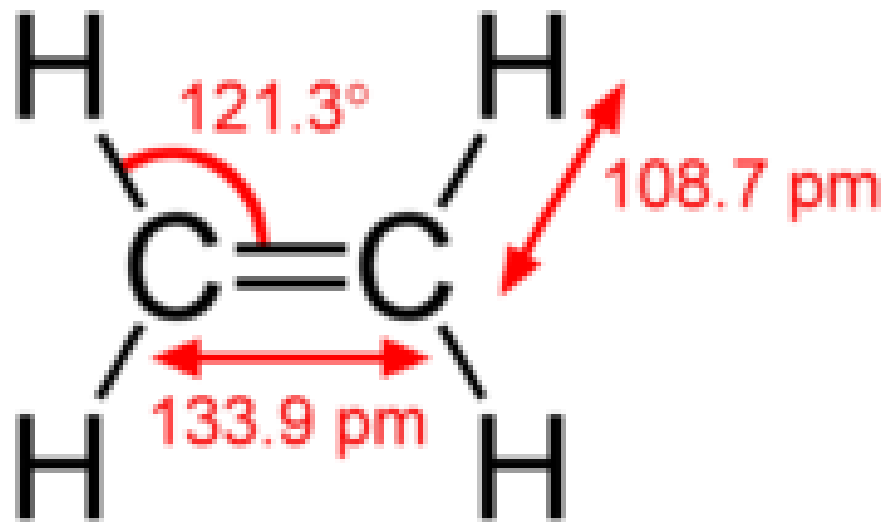
# Restraints: *a priori* knowledge

---

Restraints increase the number of observations.

Restraints modify the target function by creating relationships between independent parameters.

Example: restrained bond lengths



- the coordinates of the two atoms are independent
- restraint keeps their distance within a certain target value
- imposes a penalty if it deviates too much.

# What kind of restraints can you use?

---

## **All resolution ranges**

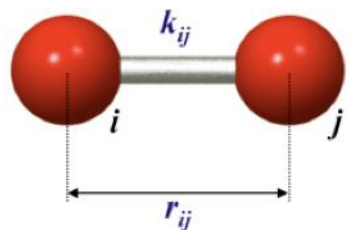
- Stereochemistry
- ADP

## **Low resolution**

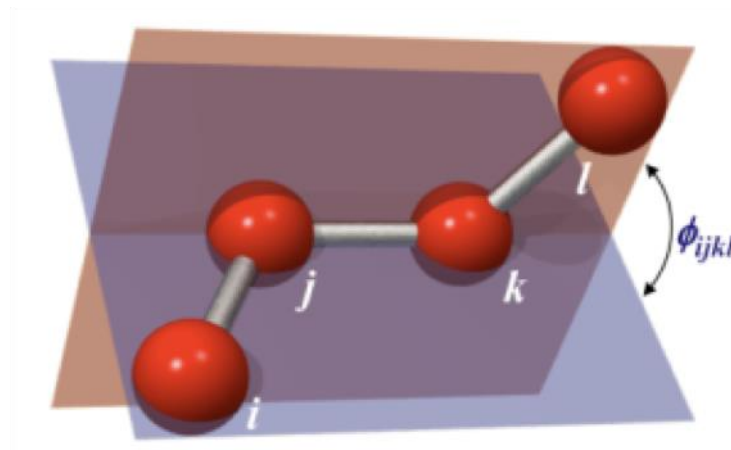
- Secondary structure restraints
- NCS
- Reference model
- Ramachandran

# Restraints: *a priori* knowledge

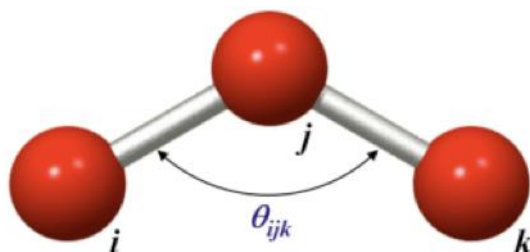
## Chemistry



$$\sum_{\text{bonds}} \omega (d_{\text{model}} - d_{\text{ideal}})^2$$



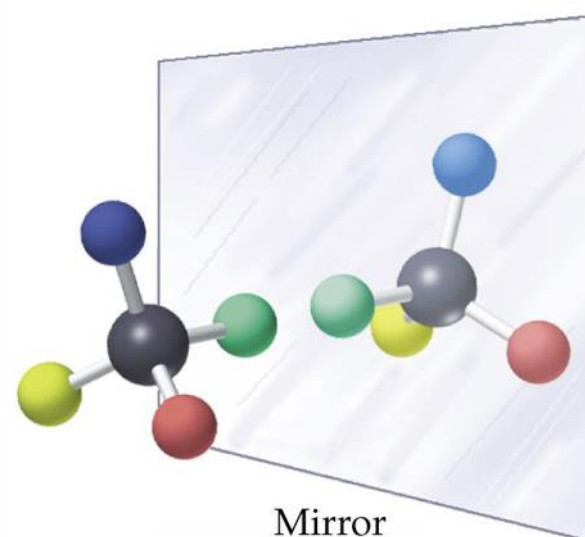
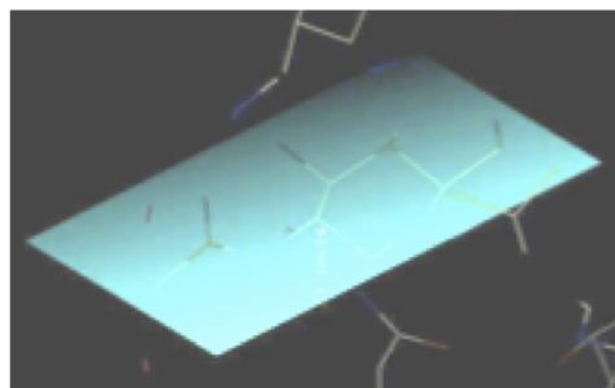
$$\sum_{\text{dihedrals}} \omega (1 + \cos(n\chi_{\text{model}} + \chi_{\text{shift}}))$$



$$\sum_{\text{angles}} \omega (\theta_{\text{model}} - \theta_{\text{ideal}})^2$$

Used  
automatically  
(no need to  
activate)

Images from PumMa web  
site (<http://www.pumma.nl>)



$$\text{Volume (V)} = (r_N - r_{CA}) \cdot [(r_C - r_{CA}) \times (r_{CB} - r_{CA})]$$

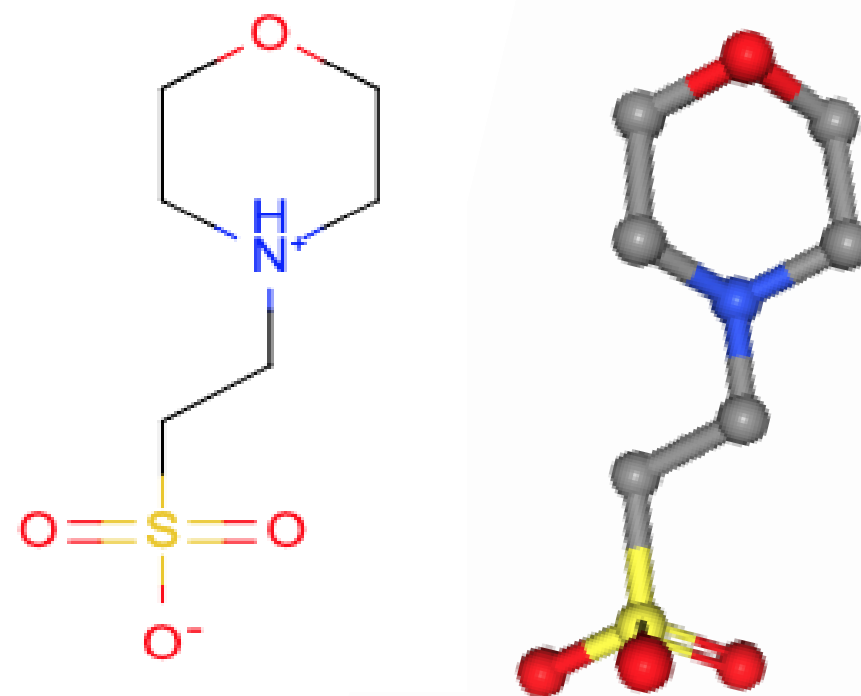
$$E = \sum_{\text{planes}} \sum_{\text{atoms}} w (m \cdot r - d)^2$$



# Restraints: Ligands

---

Restraints of common ligands are included in libraries.



If novel ligand:

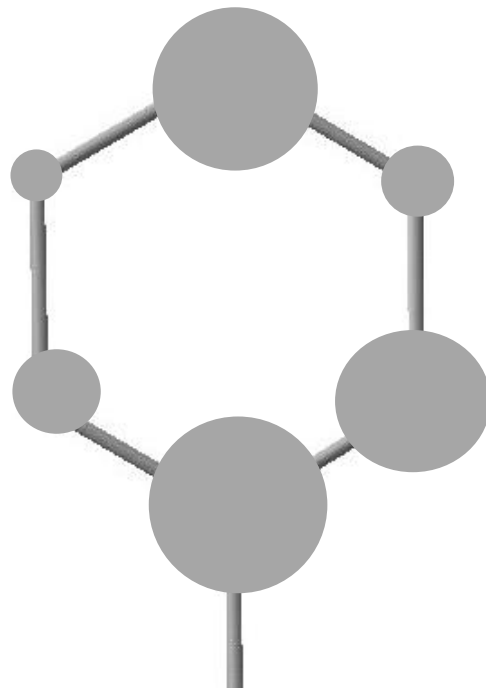
restraints need to be generated with a restraints generator

# Restraints: ADP

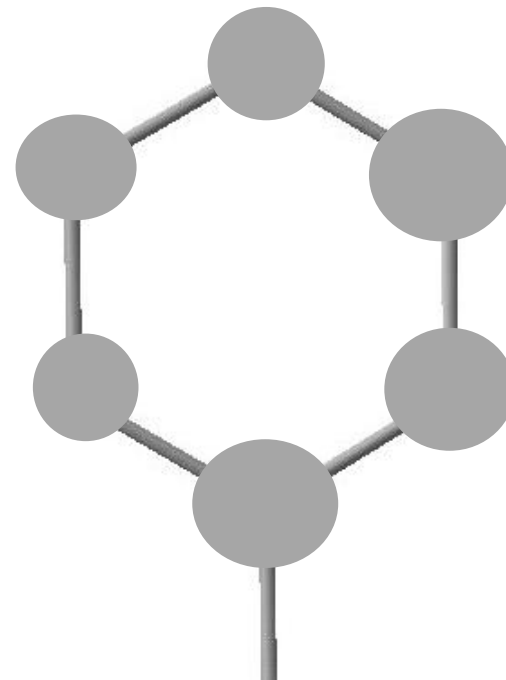
---

## Isotropic ADPs

Unlikely



Reasonable



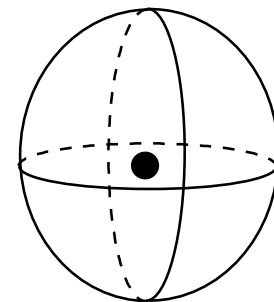
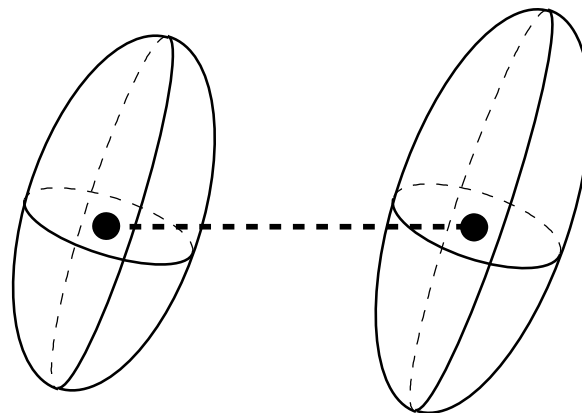
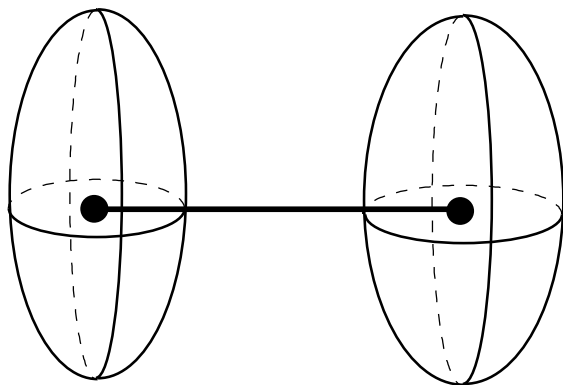
Used automatically (no need to activate).

# Restraints: ADP

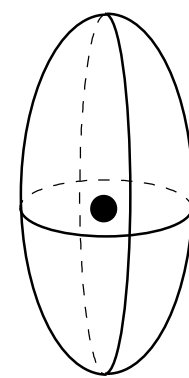
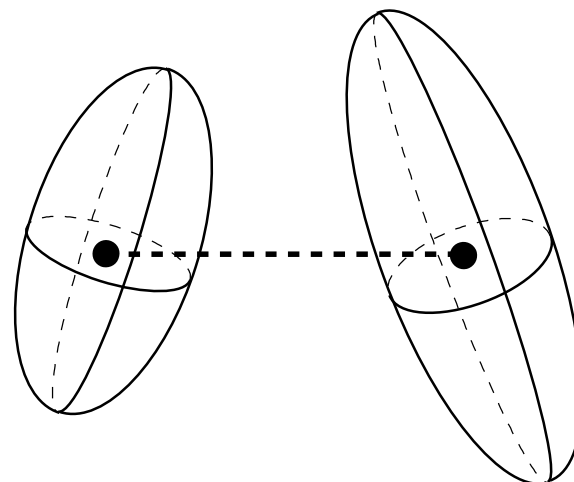
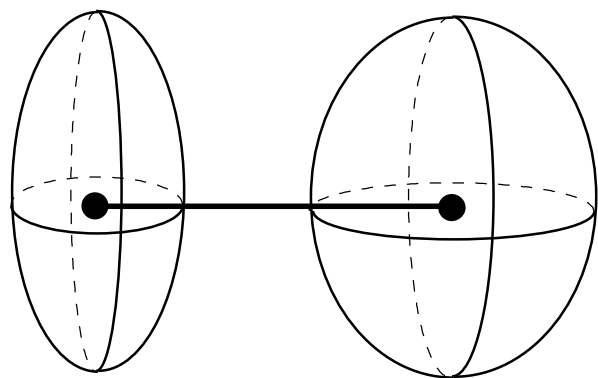
---

## Anisotropic ADPs

Reasonable



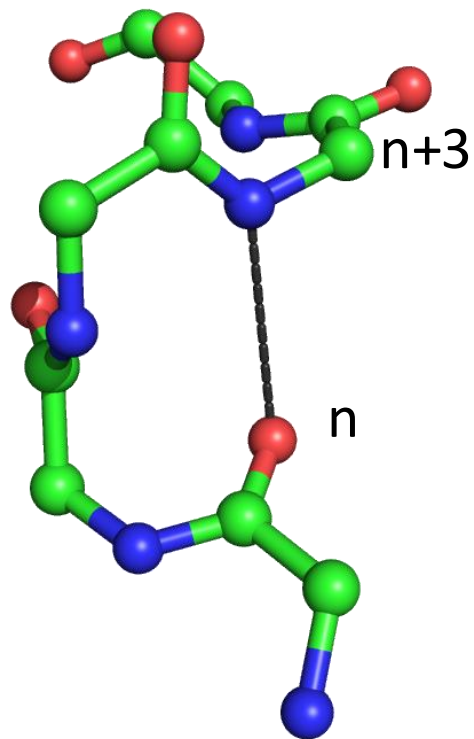
Unlikely



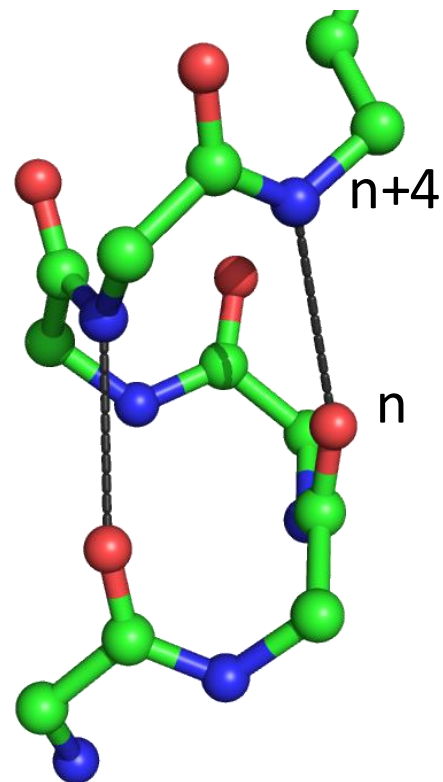
# Secondary Structure Restraints

---

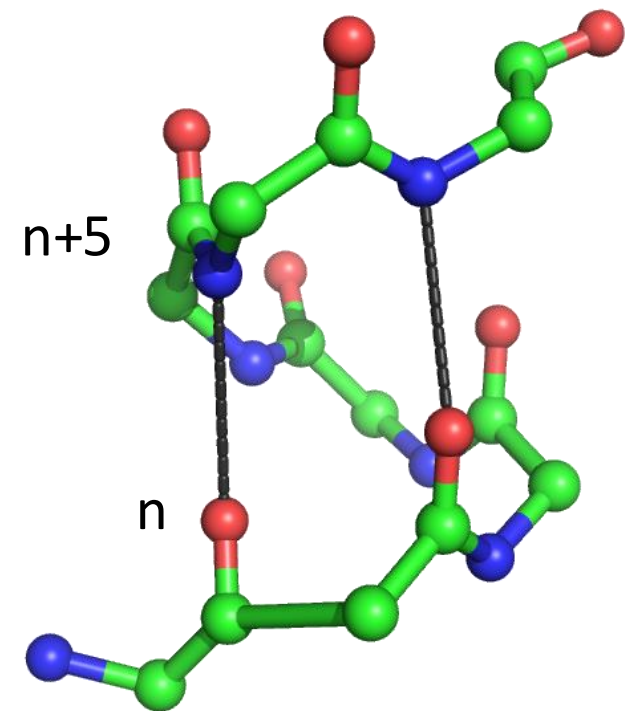
## Helices



$3_{10}$  helix



$\alpha$  helix

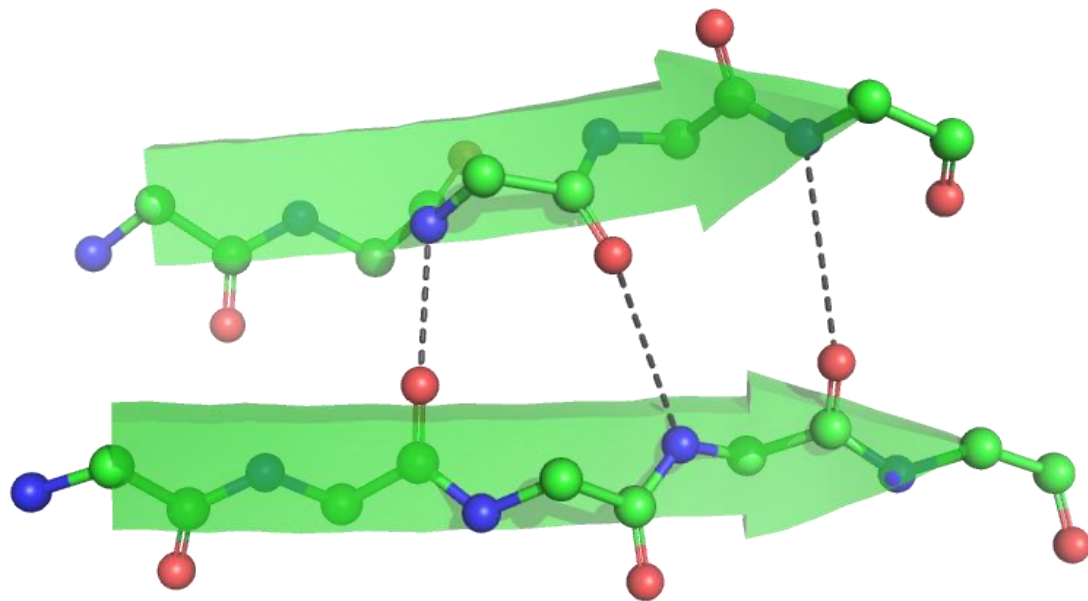


$\pi$  helix

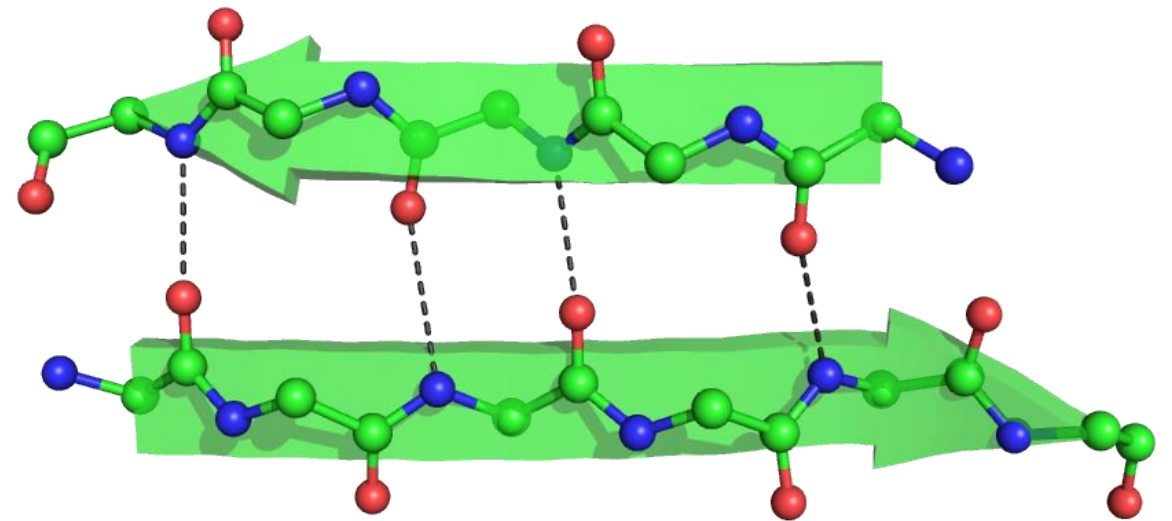
# Secondary Structure Restraints

---

## Sheets



parallel

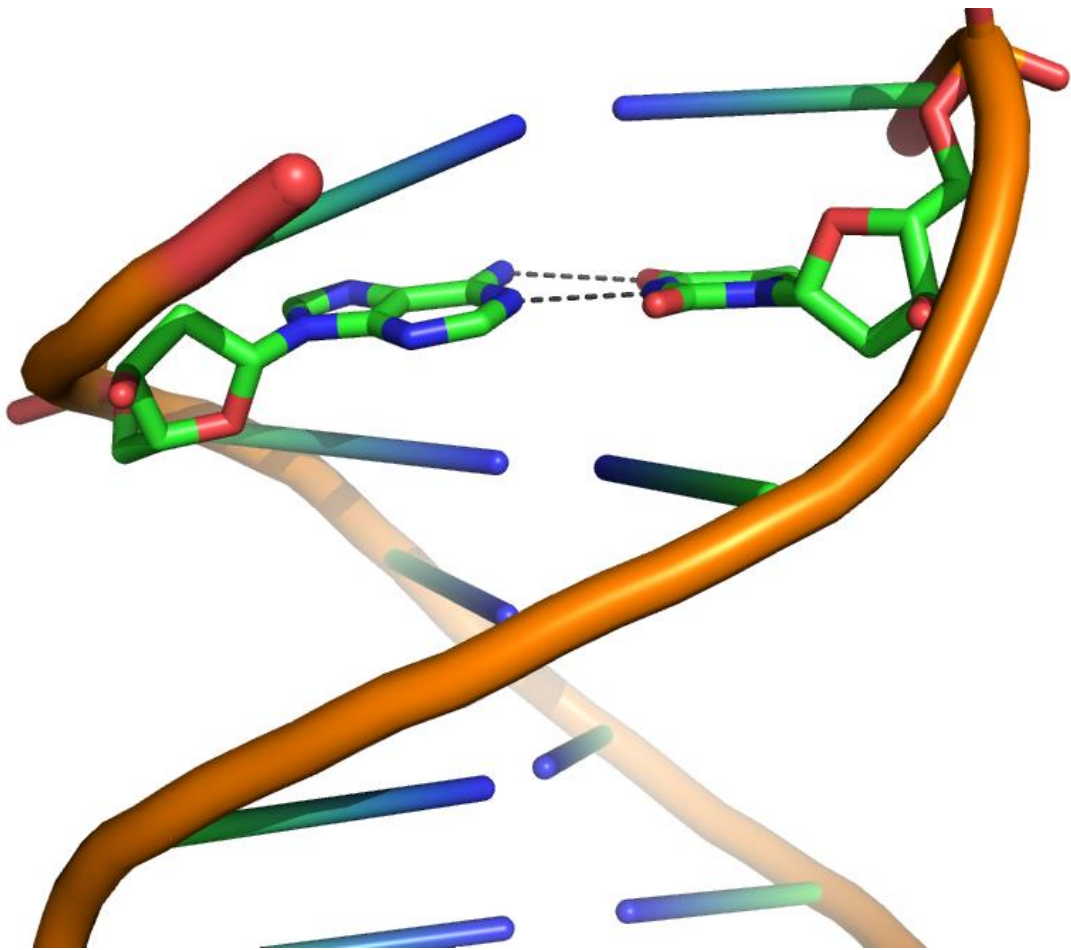


antiparallel

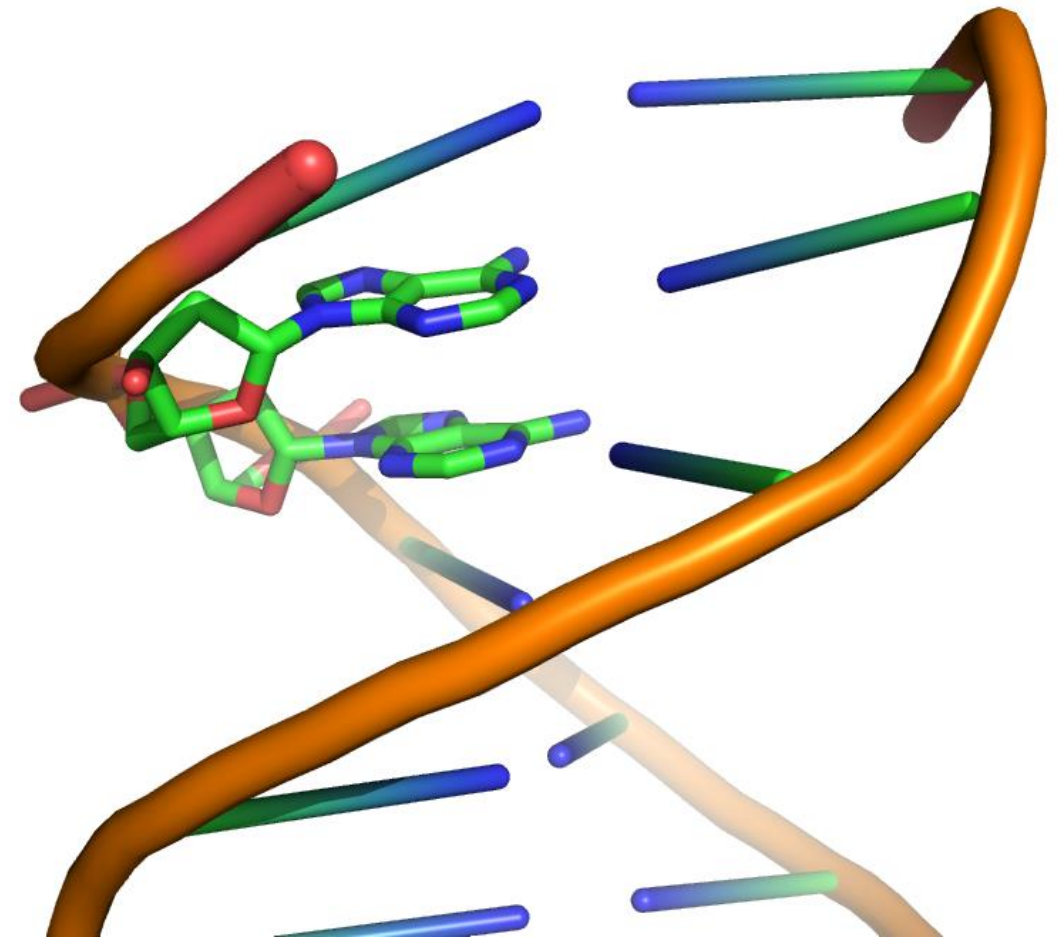
# Secondary Structure Restraints

---

**Base pairs**



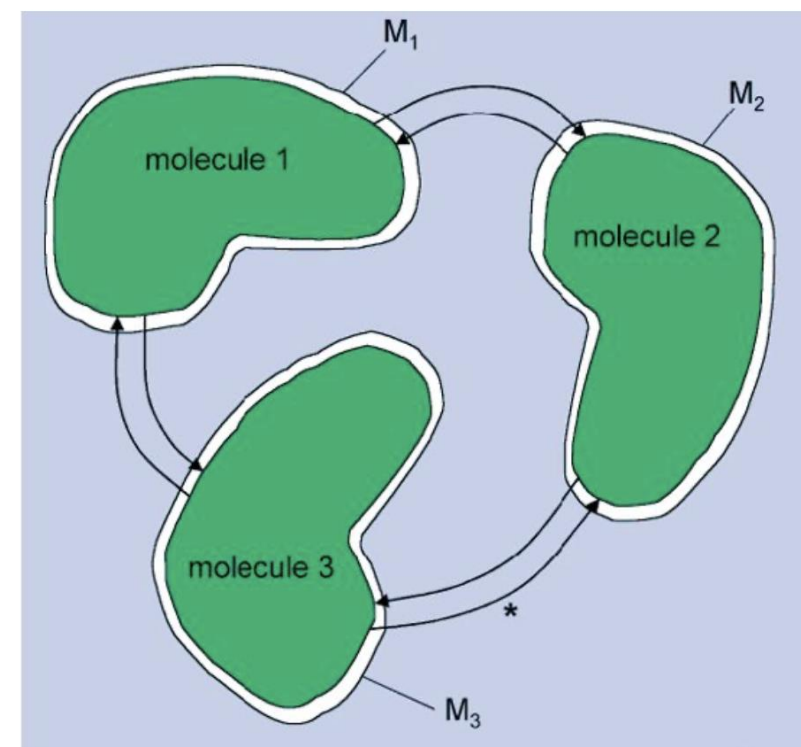
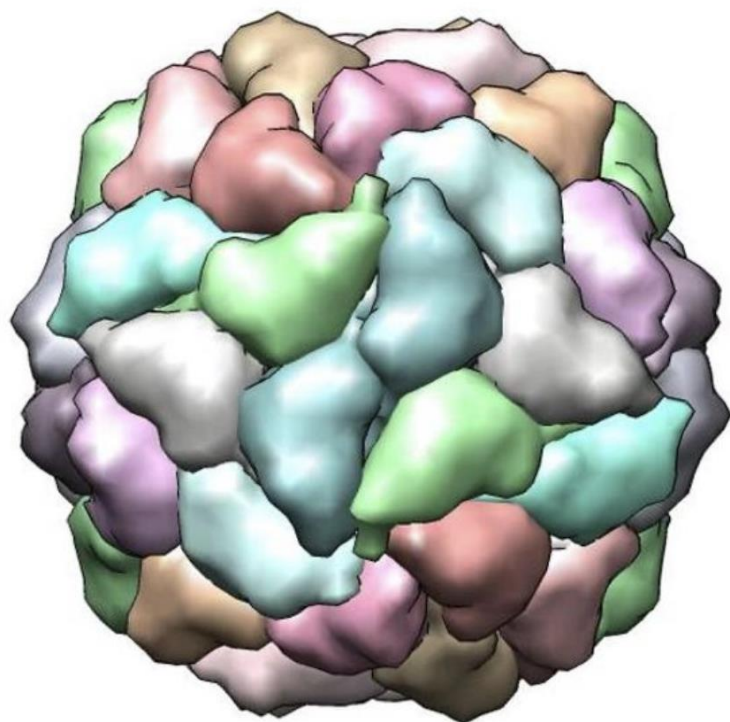
**Stacking pairs**





# NCS – non crystallographic symmetry

---



**Constrain** mols 1, 2 and 3 to be **identical**.

**Restrain** mols 1, 2 and 3 to be **similar**.

## **Cartesian restraints:**

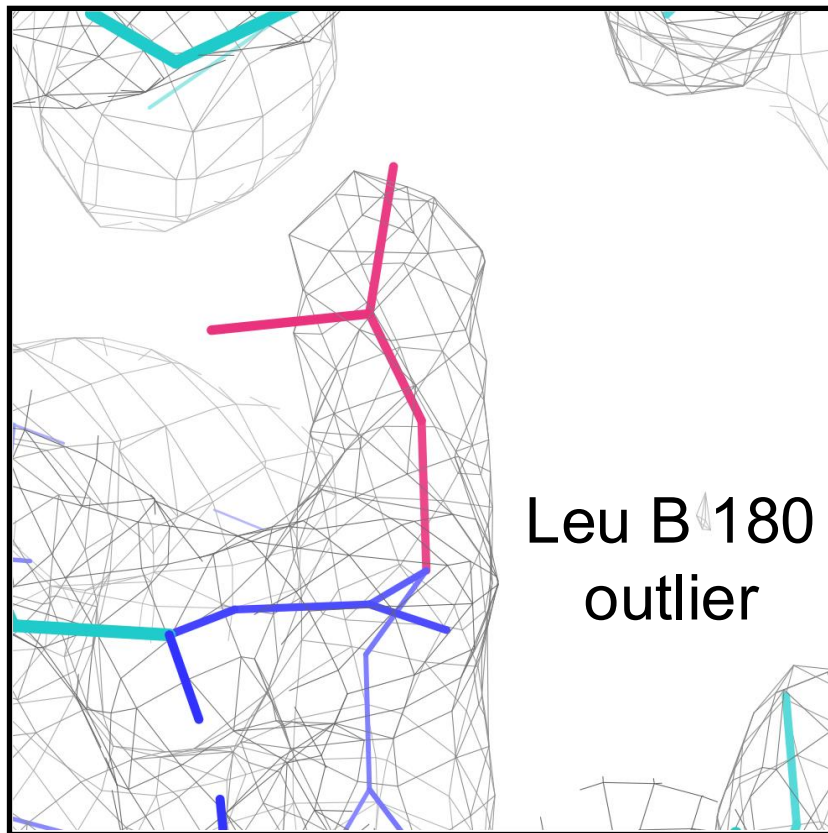
Atoms in NCS-related chains are restrained to the average xyz position.

# NCS restraints

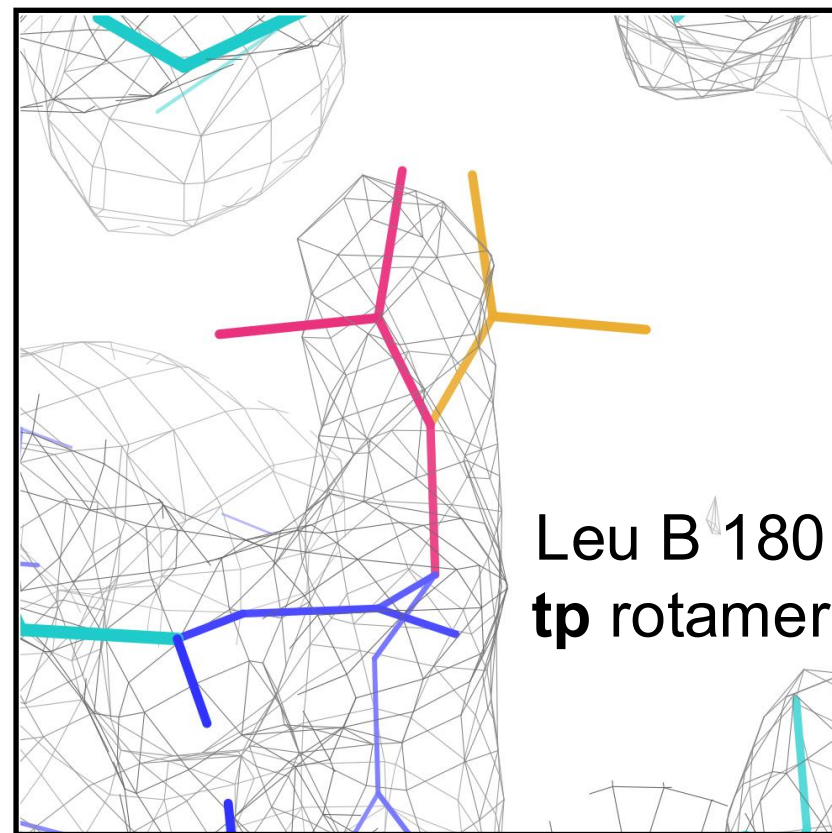
## Torsion restraints:

Restrain dihedral angles;

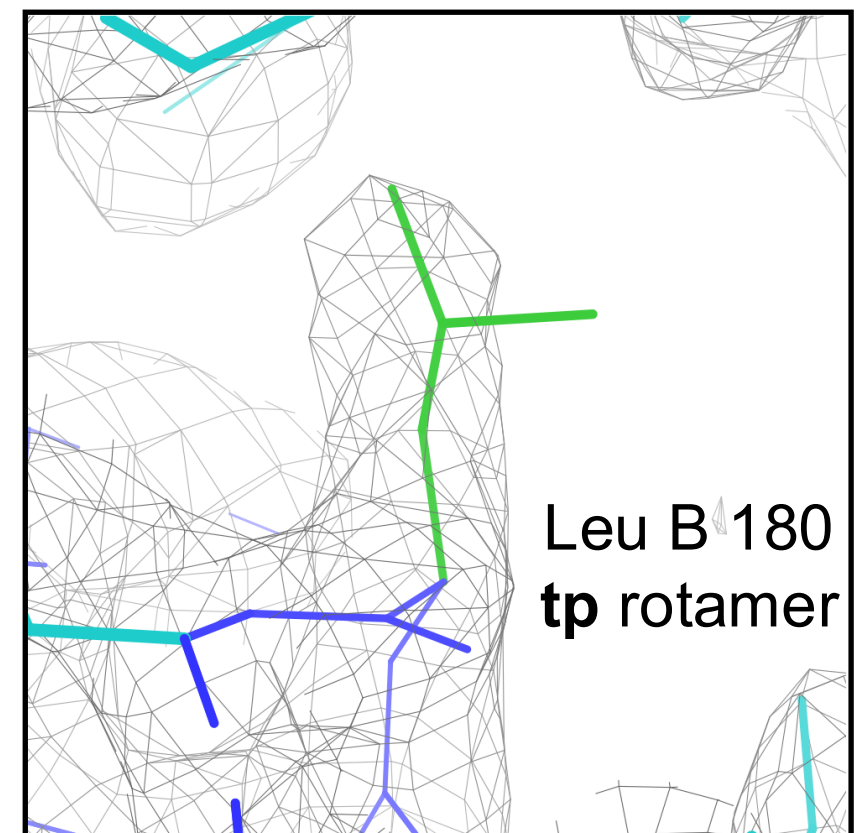
Allow them to be unrestrained if genuinely different.



1. Identify rotamer outlier



2. correct to corresponding  
rotamer in NCS-related chain  
by matching  $\chi$  angles



3. verify rotamer is still  
correct match

# NCS – which one to use?

---

Consider:

- Does my model have NCS?

Constraints vs. restraints:

- cryo-EM: Was my map symmetrized?
- Is my data good enough to reasonably expect to see difference in NCS copies?

Torsion restraints are generally preferable of Cartesian restraints.

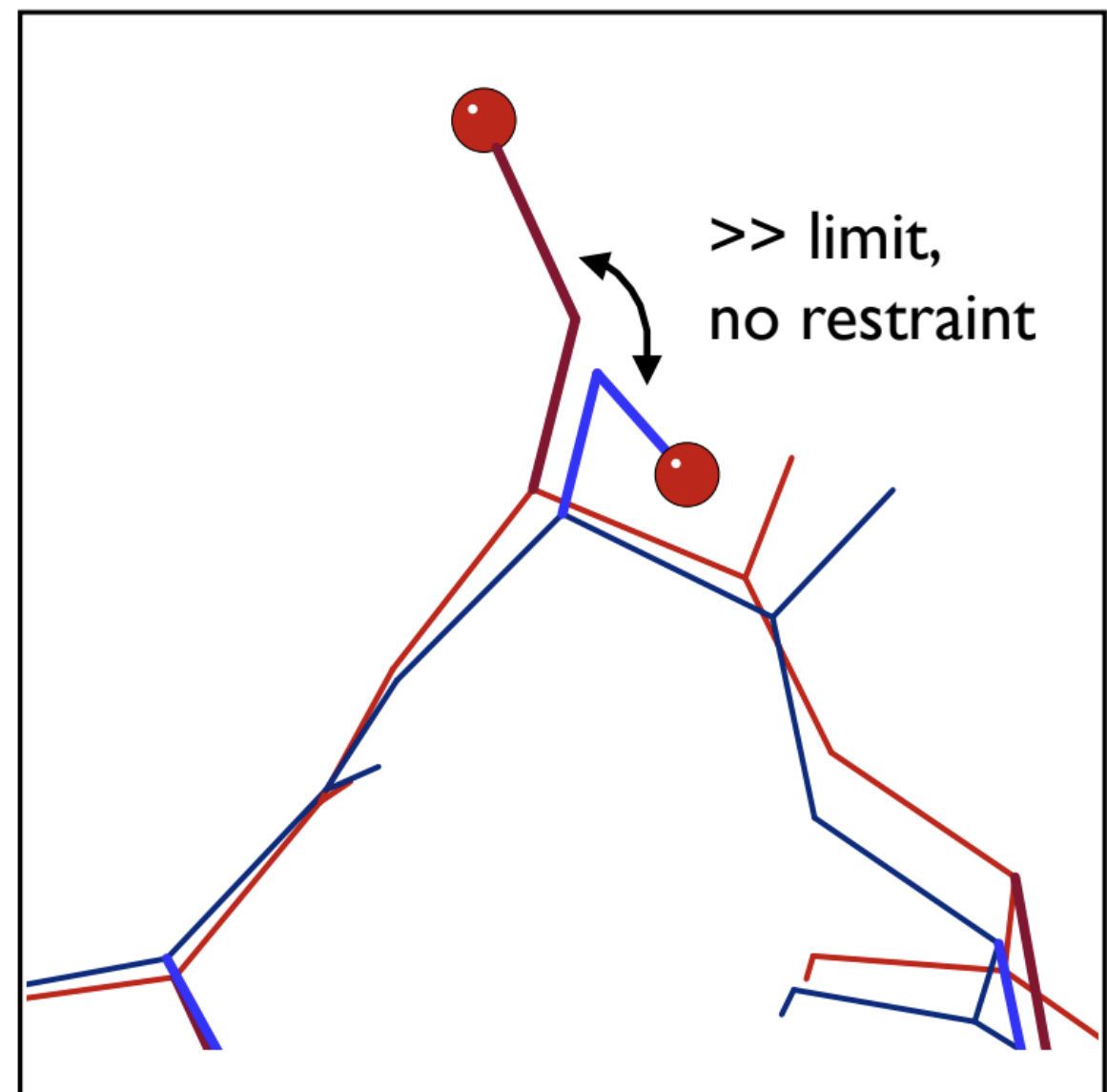
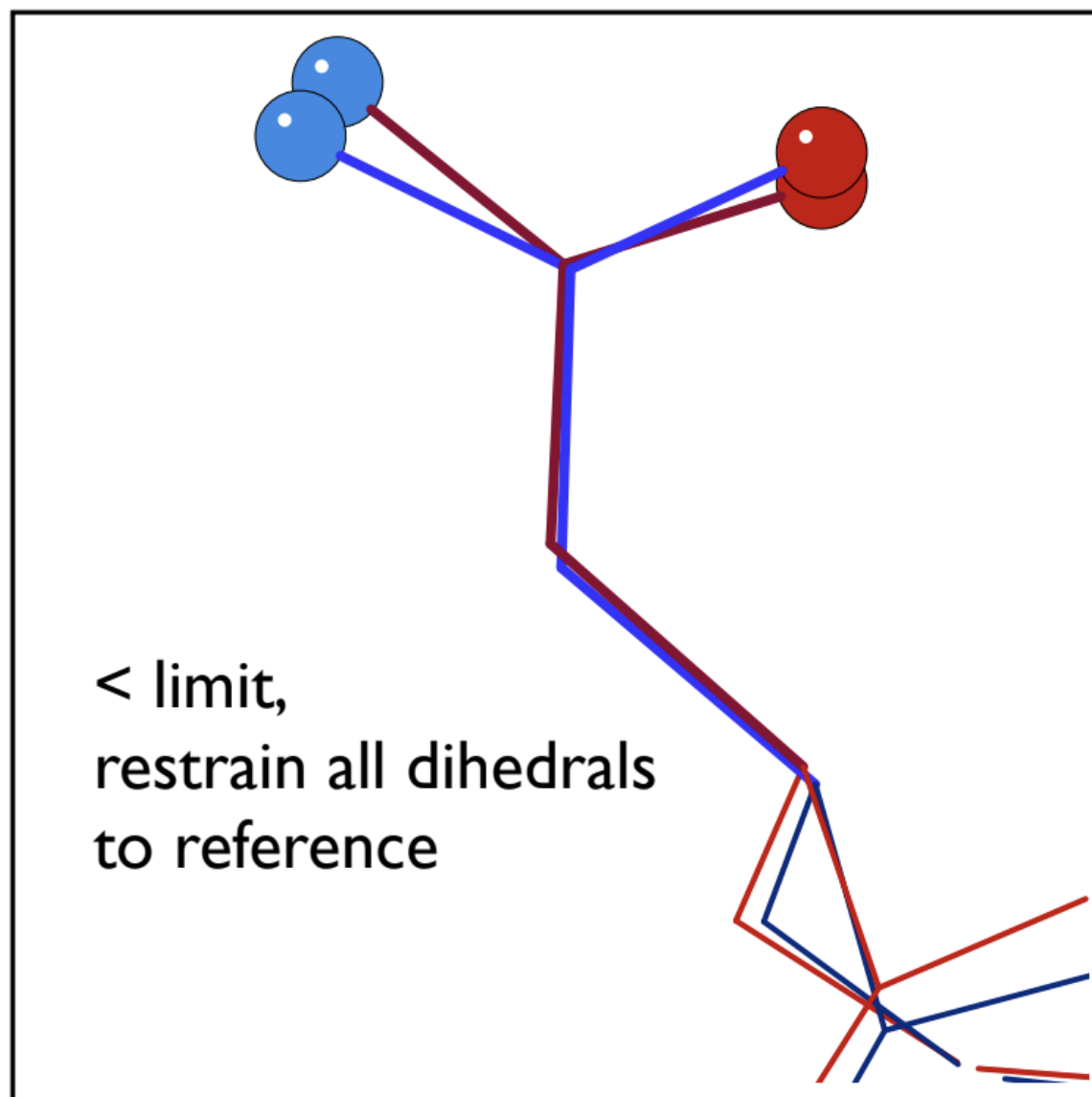
# Reference model Restraints

When to use:

The 'limit' parameter

default: limit = 15.0°

C  
F  
C  
A





# Reference model Restraints

---

**1GTX:** 3.0 Å

**1OHV:** 2.3 Å

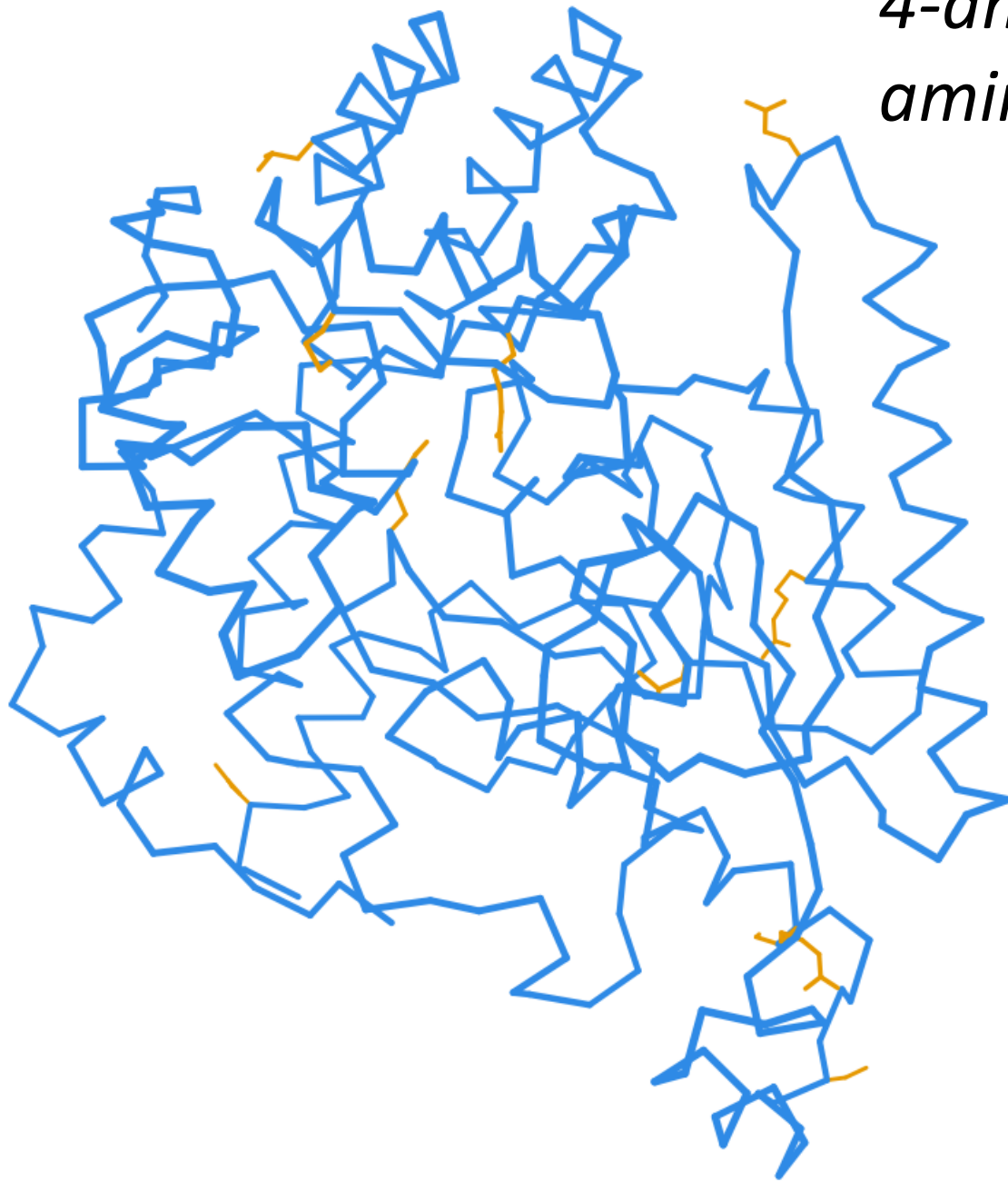


4-aminobutyrate-aminotransferase

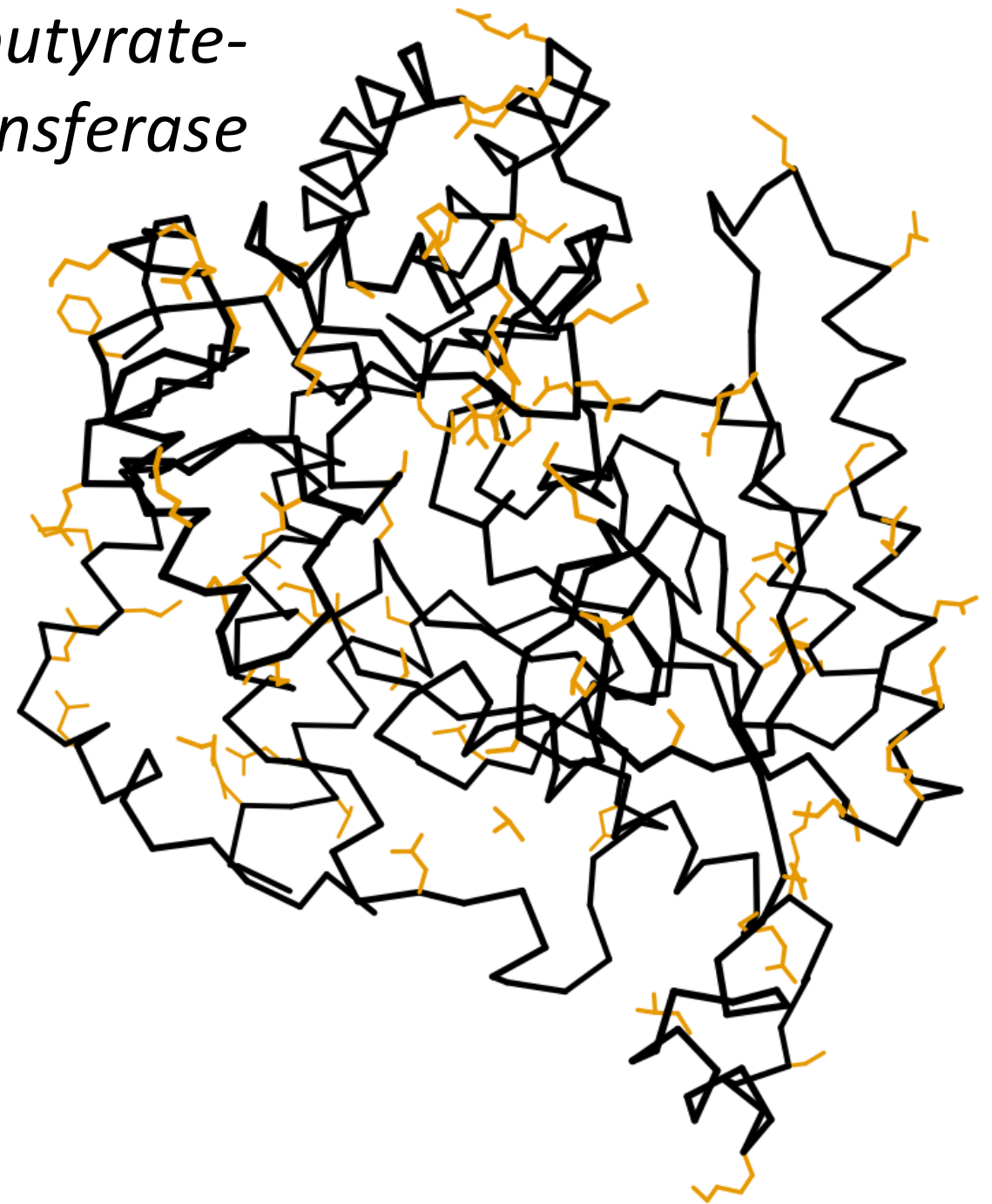
# Reference model Restraints

---

*4-aminobutyrate-  
aminotransferase*



**1OHV:** 2.3 Å



**1GTX:** 3.0 Å



# Ramachandran plot restraints

---

- The backbone dihedral angles can be restrained to stay in the allowed regions of the Ramachandran plot
- Prevent the model from degrading at low resolution when the conformation is approximately correct.

→ Don't use Ramachandran restraints to “fix” Ramachandran outliers.

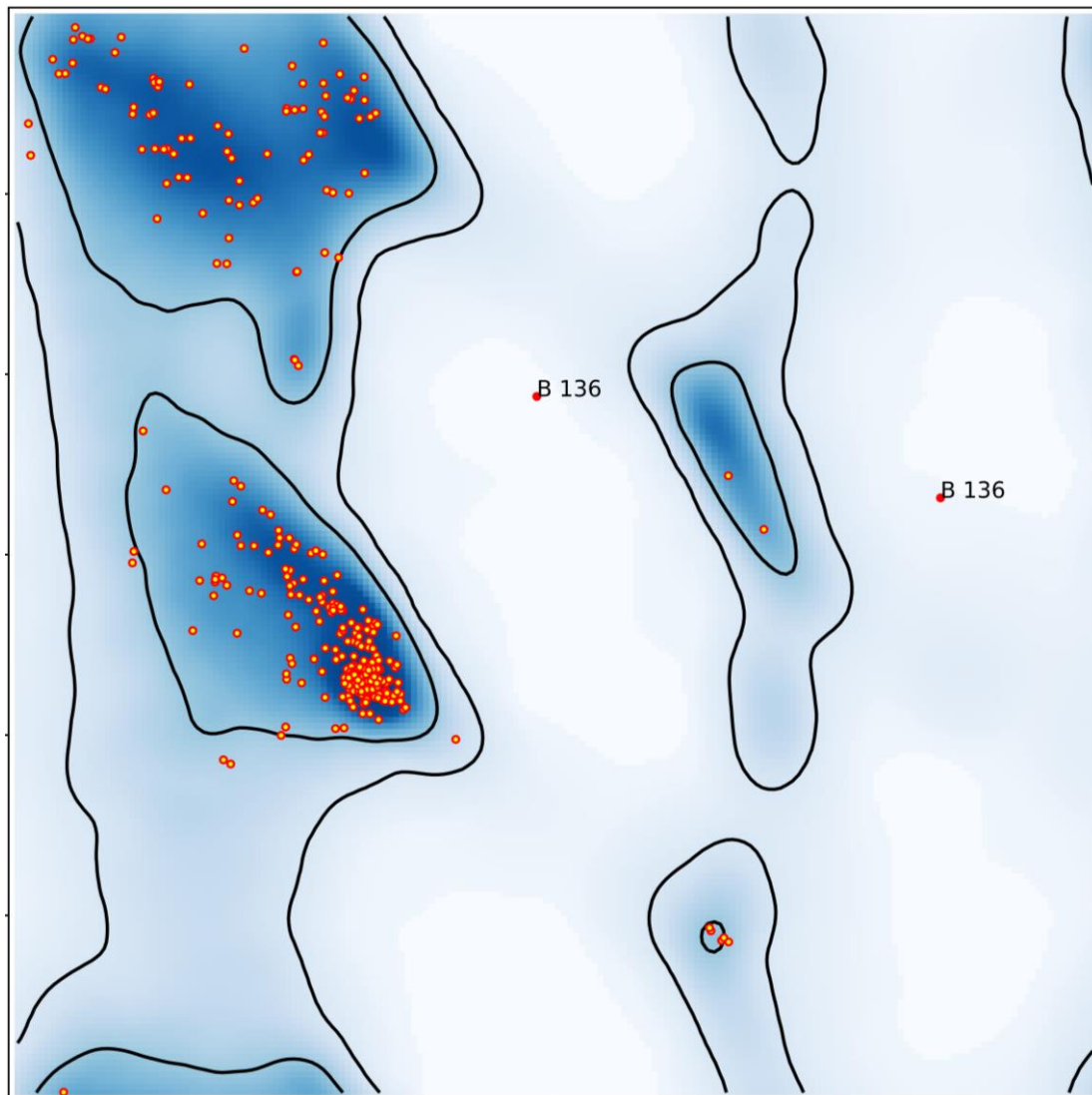
Keep in mind:

Don't rely on Ramachandran plot for validation.

# Two Ramachandran distributions

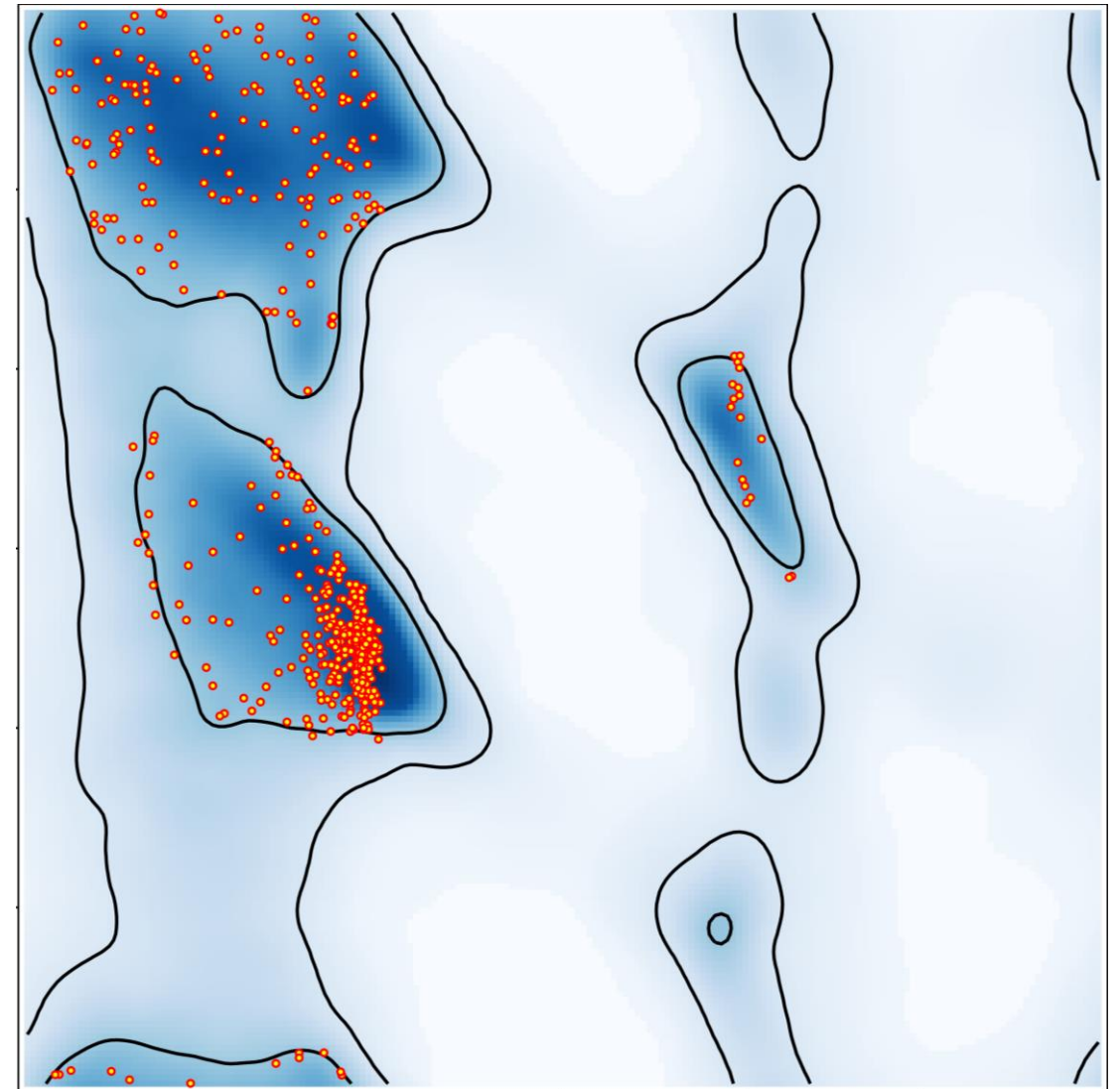
## Model A

Favored	97.8 %
Allowed	1.95 %
Outliers	0.25 %



## Model B

Favored	96.2 %
Allowed	3.8 %
Outliers	0.0 %



# Global Ramachandran Score

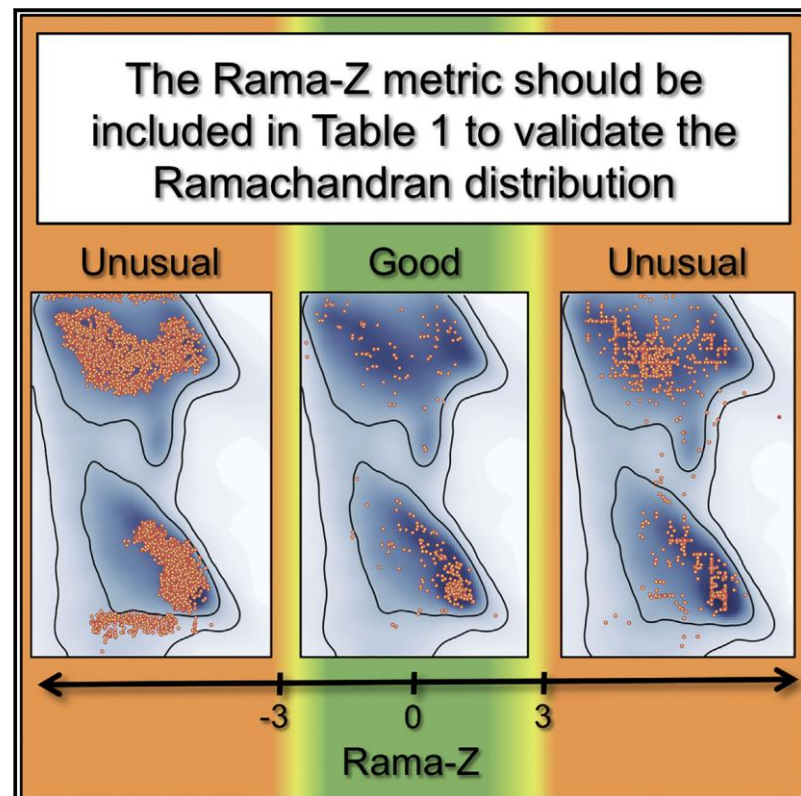
## Structure

Resource

*Structure*, 28. 1249-1258.

### A Global Ramachandran Score Identifies Protein Structures with Unlikely Stereochemistry

#### Graphical Abstract



#### Authors

Oleg V. Sobolev, Pavel V. Afonine,  
Nigel W. Moriarty,  
Maarten L. Hekkelman,  
Robbie P. Joosten,  
Anastassis Perrakis, Paul D. Adams

#### Correspondence

osobolev@lbl.gov (O.V.S.),  
r.joosten@nki.nl (R.P.J.)

#### In Brief

Counting the number of Ramachandran outliers is not sufficient for protein backbone validation. Sobolev et al. revisited the underutilized Ramachandran Z score. The authors describe its reimplementation in Phenix and PDB-REDO and showcase its utility. They advocate including it in the validation reports provided by the Protein Data Bank.

Initially proposed in 1997!

**CABIOS**

Vol. 13 no. 4 1997  
Pages 425-430

***Objectively judging the quality of a protein structure from a Ramachandran plot***

Rob W.W.Hooft, Chris Sander and Gerrit Vriend



# Global Ramachandran Score

Model A

Favored	97.8
Allowed	1.95
Outliers	0.25

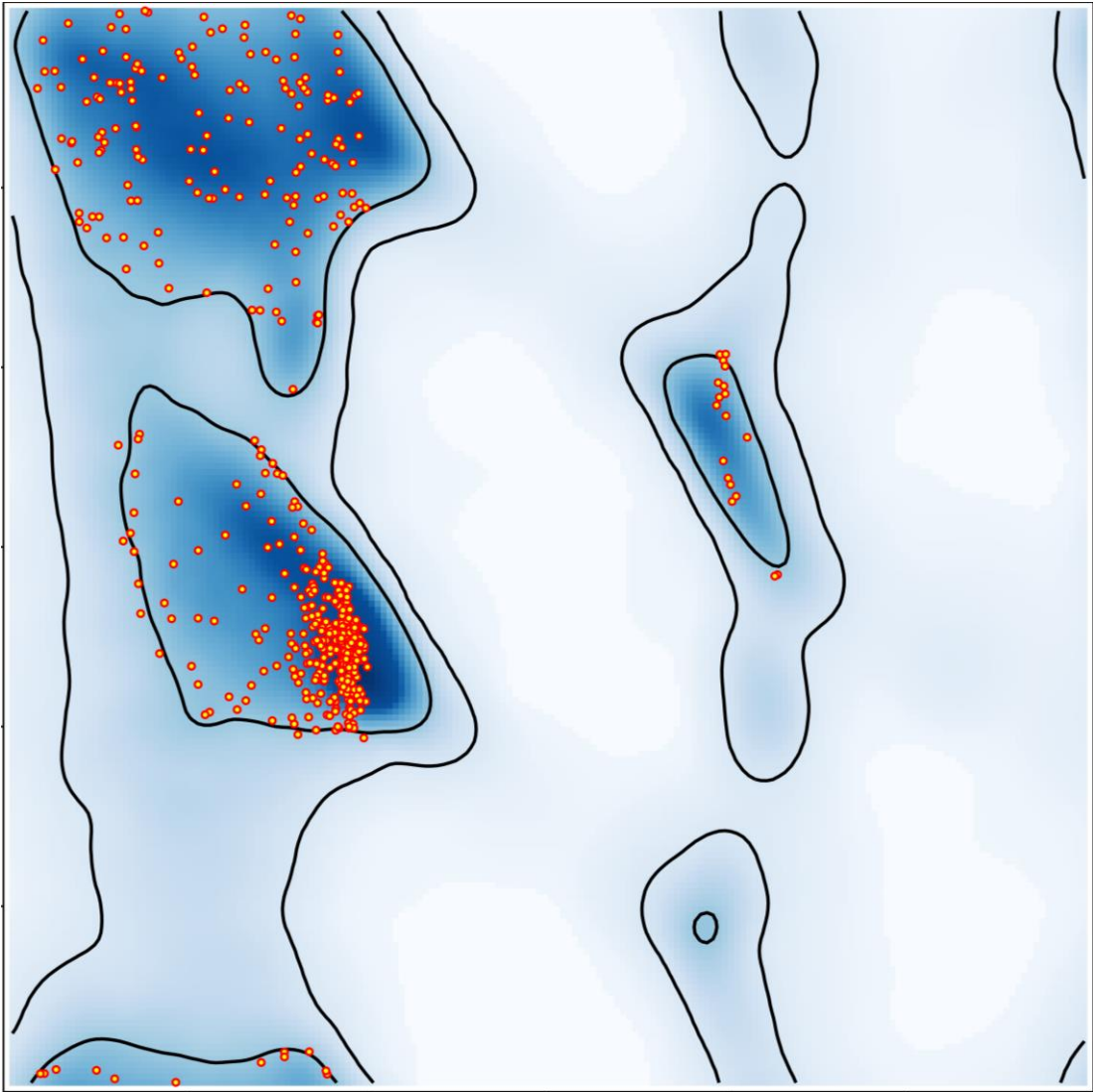
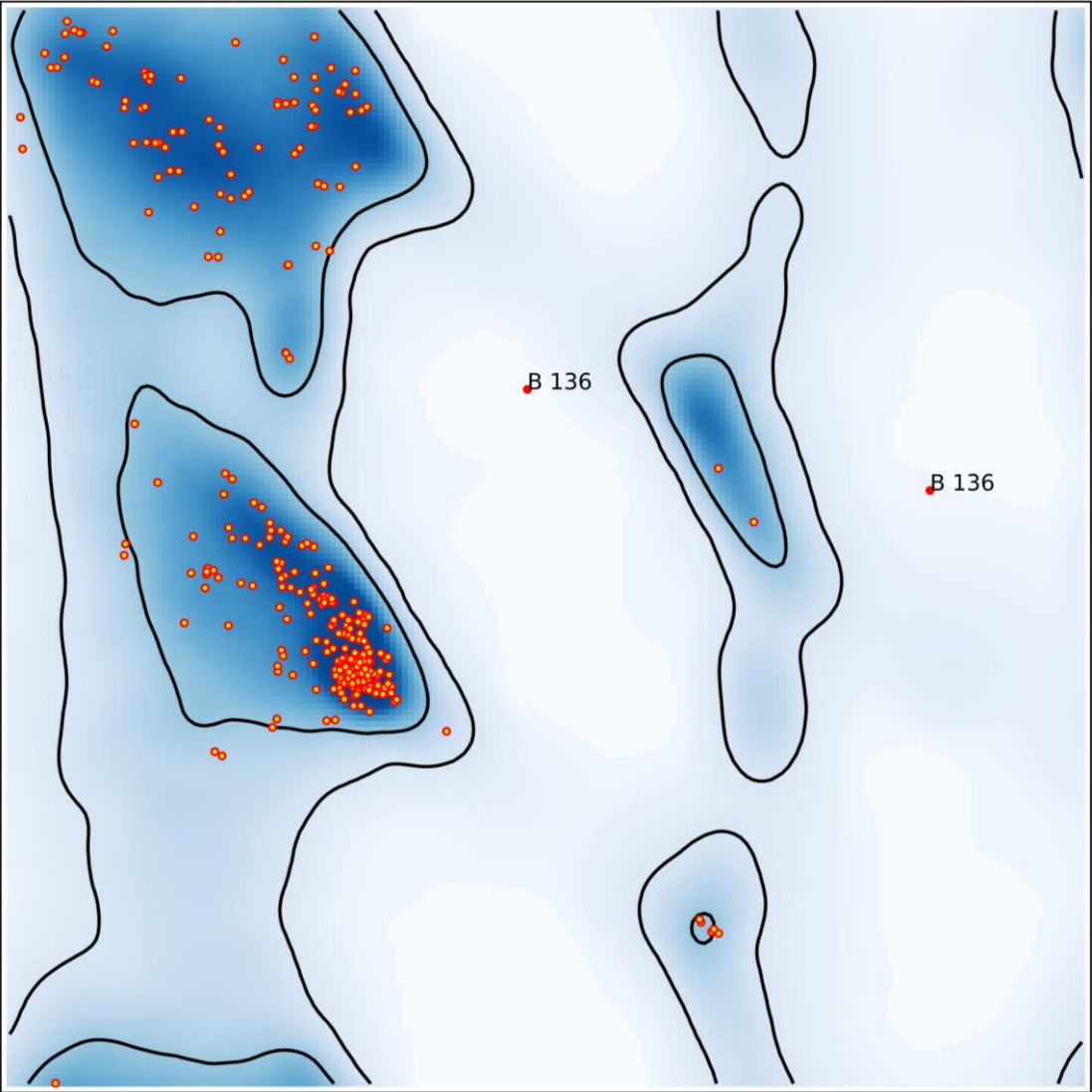
Model B

Favored	96.2
Allowed	3.8
Outliers	0.0

**Rama z-score**

-0.19

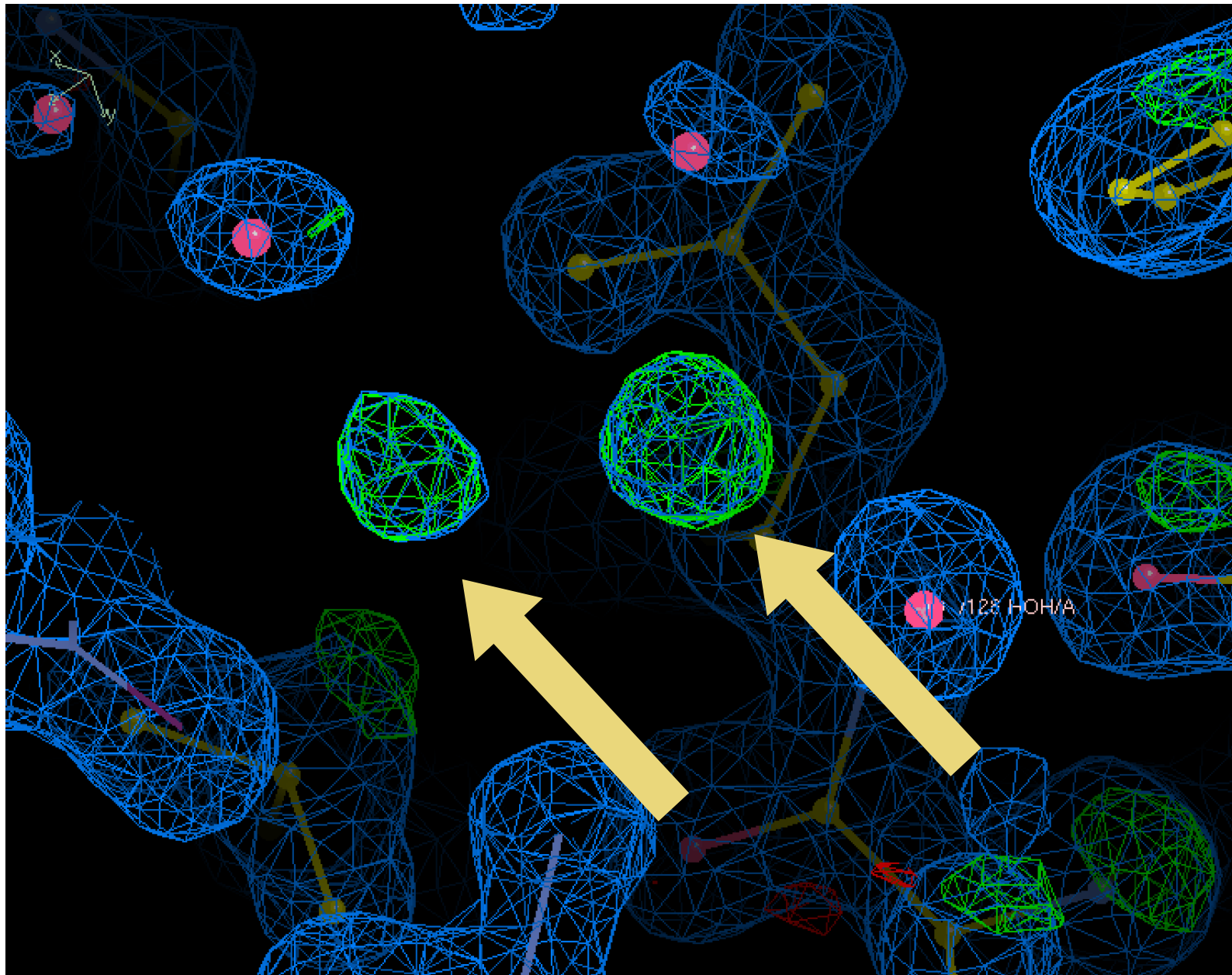
-4.08



# Automated water picking

---

Phenix.refine can build waters automatically.



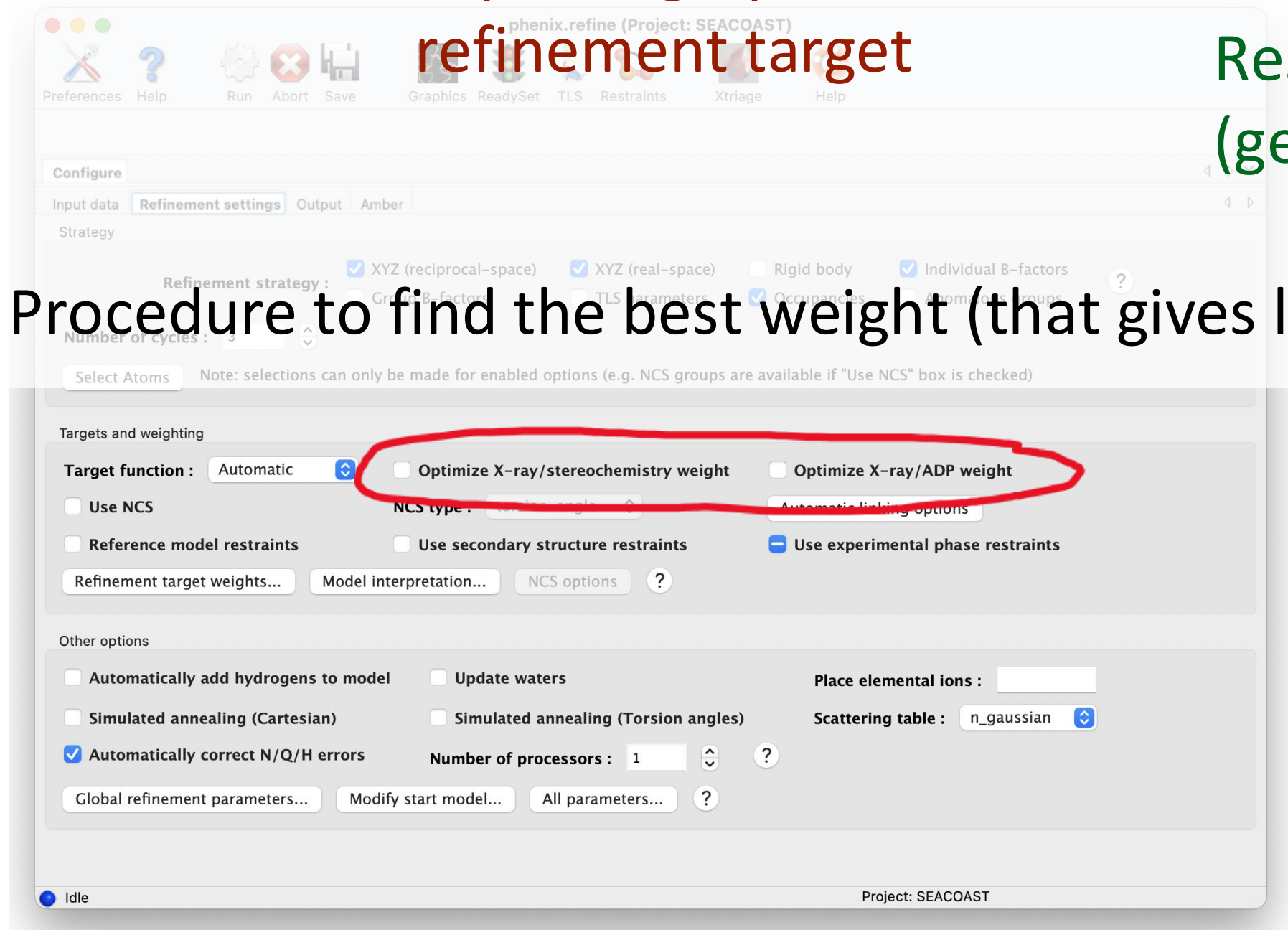
# Weight optimization

$$T = w_1 T_{Data}(F_{obs}, F_{Model}) + w_2 T_{Restrains}$$

Crystallographic  
refinement target

Restrains target  
(geometry, ADP)

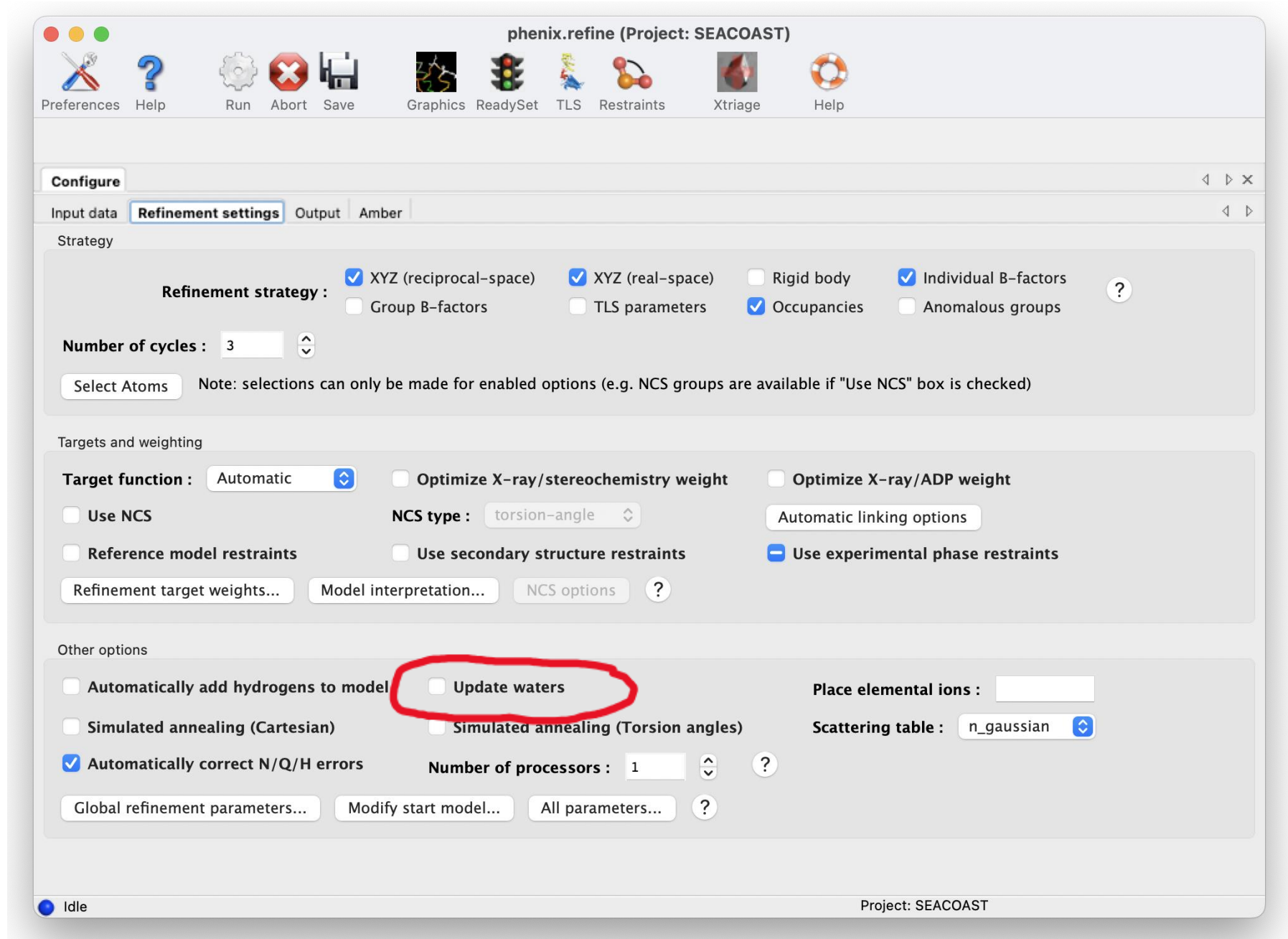
Procedure to find the best weight (that gives lowest  $R_{free}$ )





# Automated water picking

Phenix.refine can build waters automatically.



You can then check them in a molecular viewer.

# Deciding about a particular parameterization

Strategy

Refinement strategy : ☒ XYZ (reciprocal-space) ☒ XYZ (real-space) ☐ Rigid body ☒ Individual B-factors  
☐ Group B-factors ☐ TLS parameters ☒ Occupancies ☐ Anomalous groups ?

Number of cycles : 3

Select Atoms Note: selections can only be made for enabled options (e.g. NCS groups are available if "Use NCS" box is checked)

Targets and weighting

Target function : Automatic ☐ Optimize X-ray/stereochemistry weight ☐ Optimize X-ray/ADP weight  
☐ Use NCS NCS type : torsion-angle Automatic linking options  
☐ Reference model restraints ☐ Use secondary structure restraints ☒ Use experimental phase restraints  
Refinement target weights... Model interpretation... NCS options ?

Other options

☐ Automatically add hydrogens to model ☐ Update waters Place elemental ions :  
☐ Simulated annealing (Cartesian) ☐ Simulated annealing (Torsion angles) Scattering table : n\_gaussian  
☒ Automatically correct N/Q/H errors Number of processors : 1 ?  
Global refinement parameters... Modify start model... All parameters... ?

There are no easy recipes:

- “Activate all boxes: the more options, the better.”
- “Always turn on TLS after 10 rounds of refinement/Coot model building.”

# Deciding about a particular parameterization

The screenshot displays the 'Strategy' panel of the Coot software, which is used for macromolecular structure refinement. The panel is organized into three main sections: 'Refinement strategy', 'Targets and weighting', and 'Other options'.

**Refinement strategy:** This section contains checkboxes for various refinement methods. 'XYZ (reciprocal-space)' and 'XYZ (real-space)' are both checked. 'Rigid body' is unchecked, while 'Individual B-factors' is checked. 'Group B-factors' and 'TLS parameters' are unchecked. 'Occupancies' is checked, and 'Anomalous groups' is unchecked. A 'Select Atoms' button is located below these options, with a note stating: 'Note: selections can only be made for enabled options (e.g. NCS groups are available if "Use NCS" box is checked)'. The 'Number of cycles' is set to 3.

**Targets and weighting:** This section includes a 'Target function' dropdown menu set to 'Automatic'. There are checkboxes for 'Optimize X-ray/stereochemistry weight' (unchecked) and 'Optimize X-ray/ADP weight' (unchecked). 'Use NCS' is unchecked, and 'NCS type' is set to 'torsion-angle'. 'Reference model restraints' and 'Use secondary structure restraints' are both unchecked. 'Automatic linking options' is a button. 'Use experimental phase restraints' is checked. At the bottom of this section are buttons for 'Refinement target weights...', 'Model interpretation...', and 'NCS options'.

**Other options:** This section contains checkboxes for 'Automatically add hydrogens to model' (unchecked), 'Update waters' (unchecked), 'Simulated annealing (Cartesian)' (unchecked), and 'Simulated annealing (Torsion angles)' (unchecked). 'Automatically correct N/Q/H errors' is checked. 'Place elemental ions' is a text input field. 'Scattering table' is set to 'n\_gaussian'. 'Number of processors' is set to 1. At the bottom are buttons for 'Global refinement parameters...', 'Modify start model...', and 'All parameters...'.

Does it make sense to introduce this parameterization (now)?

Gradually increase the complexity of the model.

Using the same input model, try different parameterizations, then compare the results: don't rely only on R-factors, but also check validation metrics.

# The Phenix Project

## Lawrence Berkeley Laboratory

Paul Adams, Pavel Afonine,  
Dorothee Liebschner, Nigel  
Moriarty, Billy Poon,, Oleg  
Sobolev



## University of Cambridge

Randy Read, Airlie McCoy



## Los Alamos National Laboratory New Mexico Consortium

Tom Terwilliger, Li-Wei Hung



## UTHealth

Matt Baker



## Duke University

Jane Richardson,  
Vincent Chen



An NIH/NIGMS funded  
Program Project

Liebschner D, *et al.*, Macromolecular structure determination using X-rays, neutrons and electrons: recent developments in *Phenix*.  
Acta Cryst. 2019 **D75**:861–877